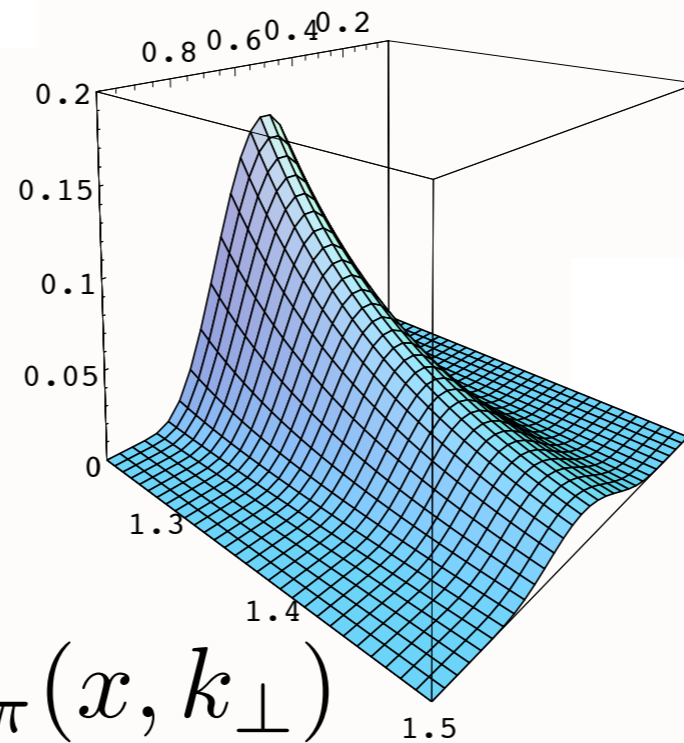
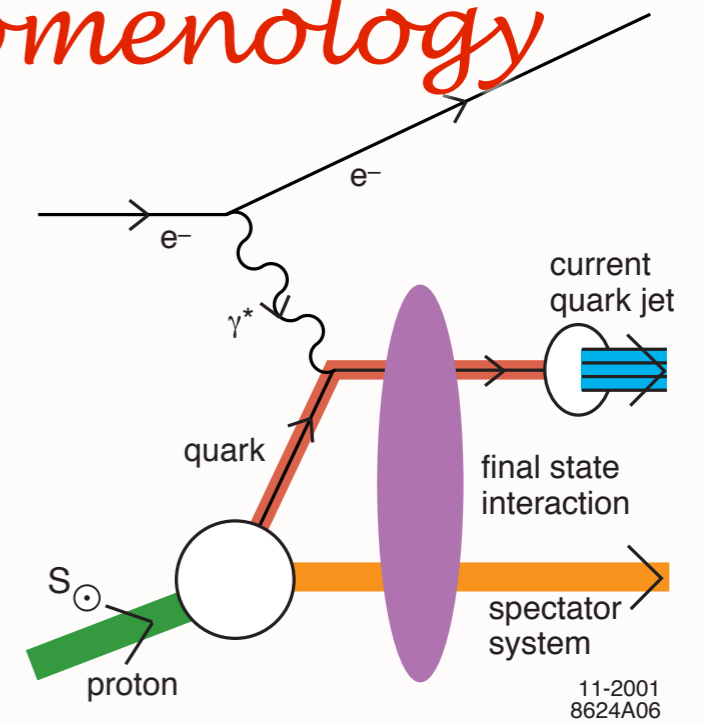
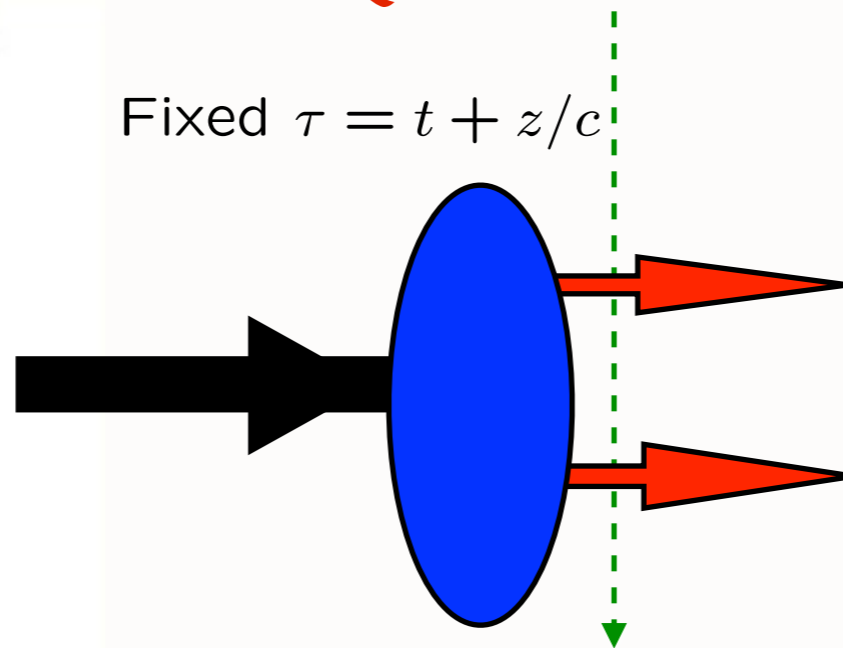
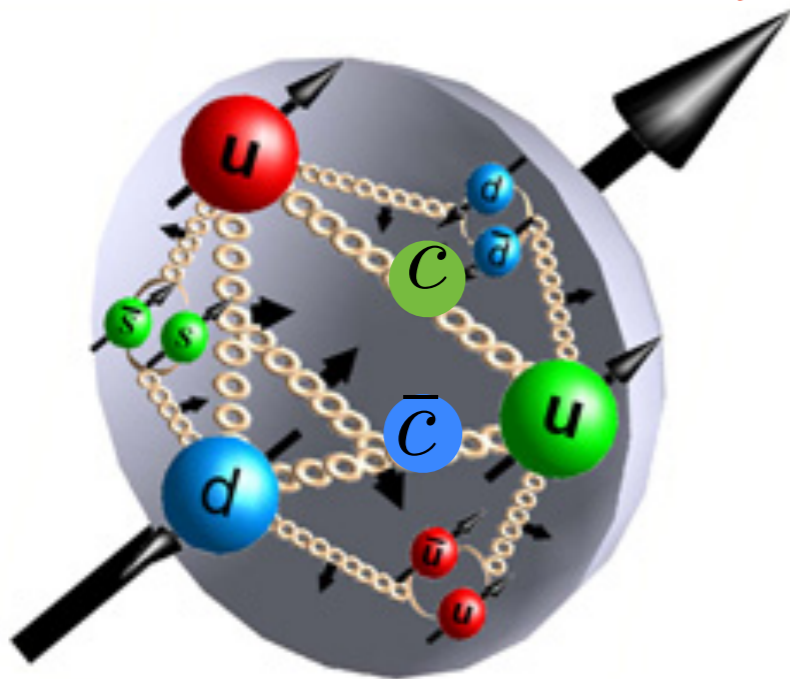


# Hadrons, AdS/QCD Duality, and the Physics of the Vacuum

## University of Warsaw Workshop, July 3-6, 2012

### Hot Topics in QCD Phenomenology



Stan Brodsky



NATIONAL  
ACCELERATOR  
LABORATORY



# *Hot Topics in QCD*

- *Intrinsic Heavy Quarks*
- *Breakdown of pQCD Leading-Twist Factorization*
- *Top/anti-Top asymmetry*
- *Non-universal antishadowing*
- *Demise of QCD Vacuum Condensates*
- *Elimination of the QCD Renormalization Scale Ambiguity*
- *AdS/QCD and Light-Front Holography*

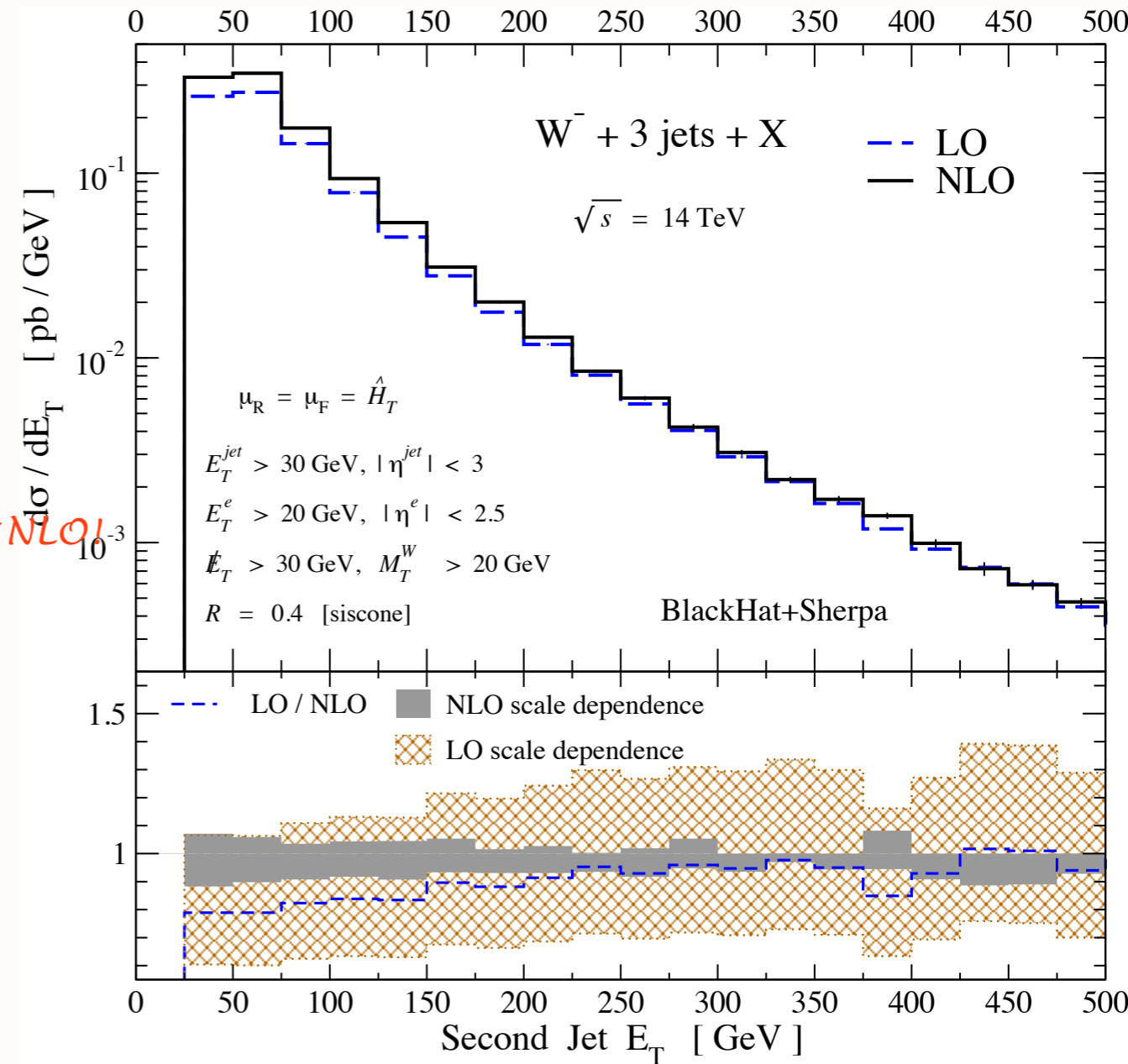
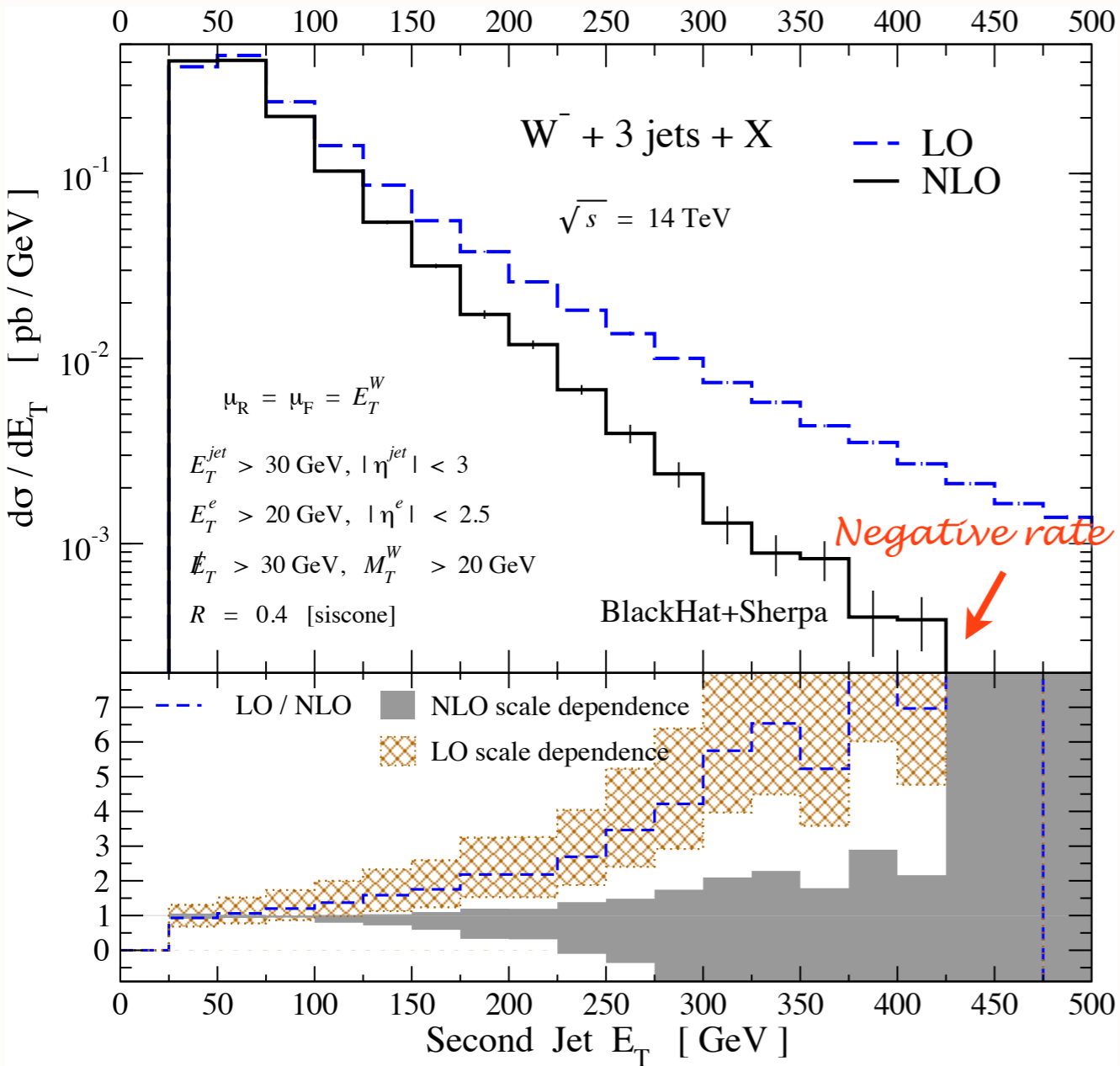
*Crucial to Understand QCD to High Precision to  
Illuminate New Physics*

# Next-to-Leading Order QCD Predictions for W + 3-Jet Distributions at Hadron Colliders

**Black Hat**

$$\mu_R = \mu_F = E_T^W$$

$$\mu_R = \mu_F = \hat{H}_T$$



C. F. Berger, Z. Bern, L. J. Dixon, F. Febres Cordero, D. Forde, T. Gleisberg, H. Ita, D. A. Kosower, and D. Maitre

Warsaw  
 July 6, 2012

Hot Topics in QCD Phenomenology

Stan Brodsky

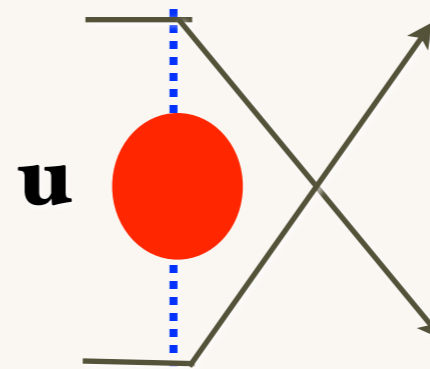
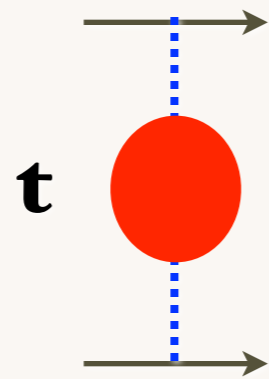


# Goals

- Test QCD to maximum precision
- High precision determination of  $\alpha_s(Q^2)$  at all scales
- Relate observable to observable --no scheme or scale ambiguity
- Eliminate renormalization scale ambiguity in a scheme-independent manner
- Relate renormalization schemes without ambiguity
- Maximize sensitivity to new physics at the colliders

# Electron-Electron Scattering in QED

$$\mathcal{M}_{ee \rightarrow ee}(++;++) = \frac{8\pi s}{t} \alpha(t) + \frac{8\pi s}{u} \alpha(u)$$



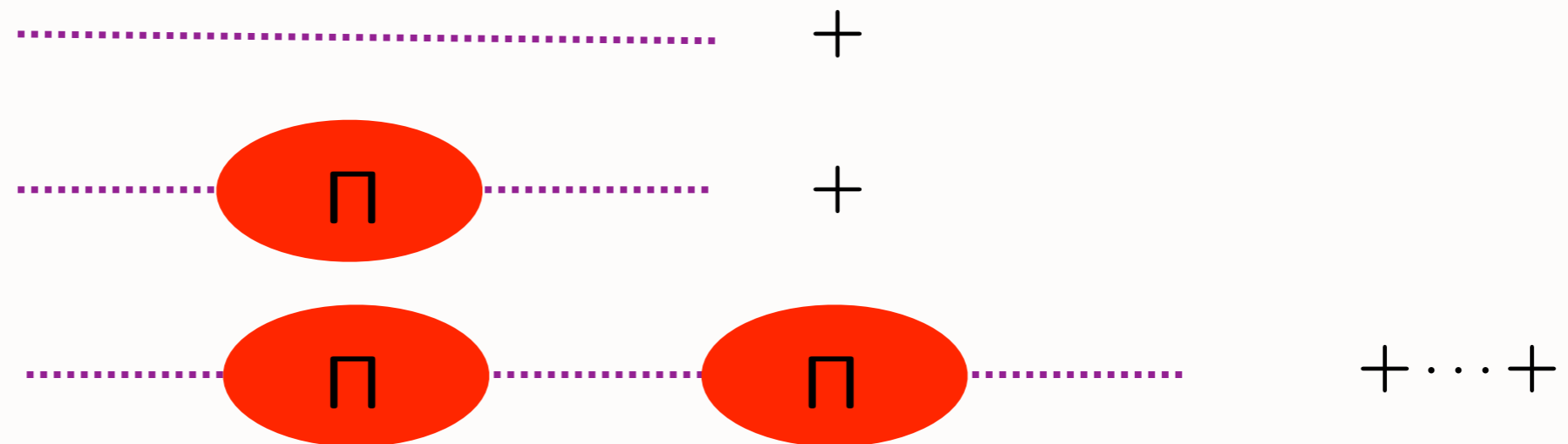
$$\alpha(t) = \frac{\alpha(0)}{1 - \Pi(t)}$$

**Gell-Mann--Low Effective Charge**

# QED Effective Charge

$$\alpha(t) = \frac{\alpha(0)}{1 - \Pi(t)}$$

*All-orders lepton-loop corrections to dressed photon propagator*



$$\alpha(t) = \frac{\alpha(t_0)}{1 - \Pi(t, t_0)} \quad \Pi(t, t_0) = \frac{\Pi(t) - \Pi(t_0)}{1 - \Pi(t_0)}$$

***Initial scale  $t_0$  is arbitrary -- Variation gives RGE Equations  
Physical renormalization scale  $t$  not arbitrary!***

## Relation between scales of the Gell-Mann-Low and $\overline{\text{MS}}$ schemes

$$\log \frac{\mu_0^2}{m_\ell^2} = 6 \int_0^1 x(1-x) \log \frac{m_\ell^2 + Q_0^2 x(1-x)}{m_\ell^2}$$

$$\log \frac{\mu_0^2}{m_\ell^2} = \log \frac{Q_0^2}{m_\ell^2} - 5/3$$

$$\mu_0^2 = Q_0^2 e^{-5/3} \quad \text{when } Q_0^2 \gg m_\ell^2$$

D. S. Hwang, sjb

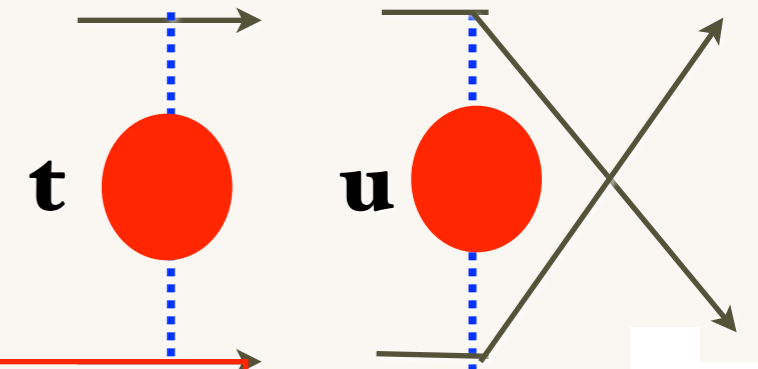
M. Binger

*Can use  $\overline{\text{MS}}$  scheme in QED; answers are scheme independent  
Analytic extension: coupling is complex for timelike argument*

# Electron-Electron Scattering in QED

$$\mathcal{M}_{ee \rightarrow ee}(++; ++) = \frac{8\pi s}{t} \alpha(t) + \frac{8\pi s}{u} \alpha(u)$$

- Two separate physical scales:  $t, u =$  photon virtuality
- Gauge Invariant. Dressed photon propagator
- Sums all vacuum polarization, non-zero beta terms into running coupling. This is the purpose of the running coupling!
- If one chooses a different initial scale, one must sum an infinite number of graphs -- but always recover same result!
- Number of active leptons correctly set
- Analytic: reproduces correct behavior at lepton mass thresholds
- No renormalization scale ambiguity!





# Features of BLM Scale Setting

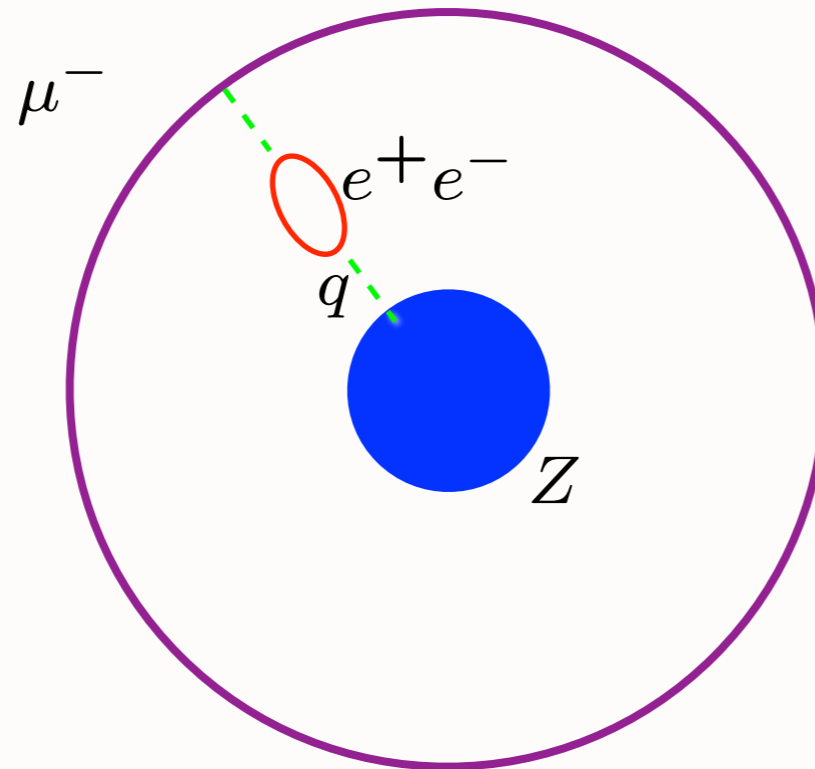
On The Elimination Of Scale Ambiguities In Perturbative Quantum Chromodynamics.

Lepage, Mackenzie, sjb

Phys.Rev.D28:228,1983

- **“Principle of Maximum Conformality”** Di Giustino, Wu, sjb
- **All terms associated with nonzero beta function summed into running coupling**
- **Standard procedure in QED**
- **Resulting series identical to conformal series**
- **Renormalon  $n!$  growth of PQCD coefficients from beta function eliminated!**
- *Scheme Independent !!!*
- **In general, BLM/PMC scales depend on all invariants**
- **Single Effective PMC scale at NLO**

# Another Example in QED: Muonic Atoms



$$V(q^2) = -\frac{Z\alpha_{QED}(q^2)}{q^2}$$

$$\mu_R^2 \equiv q^2$$

$$\alpha_{QED}(q^2) = \frac{\alpha_{QED}(0)}{1-\Pi(q^2)}$$

**Scale is unique: Tested to ppm**

Gyulassy: Higher Order VP verified to  
0.1% precision in  $\mu$  Pb

# QCD Observables

$$\mathcal{O} = C(\alpha_s(\mu_0^2)) + B(\beta \log \frac{Q^2}{\mu_0^2}) + D(\frac{m_q^2}{Q^2}) + E(\frac{\Lambda_{QCD}^2}{Q^2}) + F(\frac{\Lambda_{QCD}^2}{m_Q^2}) + G(\frac{m_q^2}{m_Q^2})$$

↑  
**Scale-Free  
Conformal Series**

↖  
**Running Coupling  
Effects**

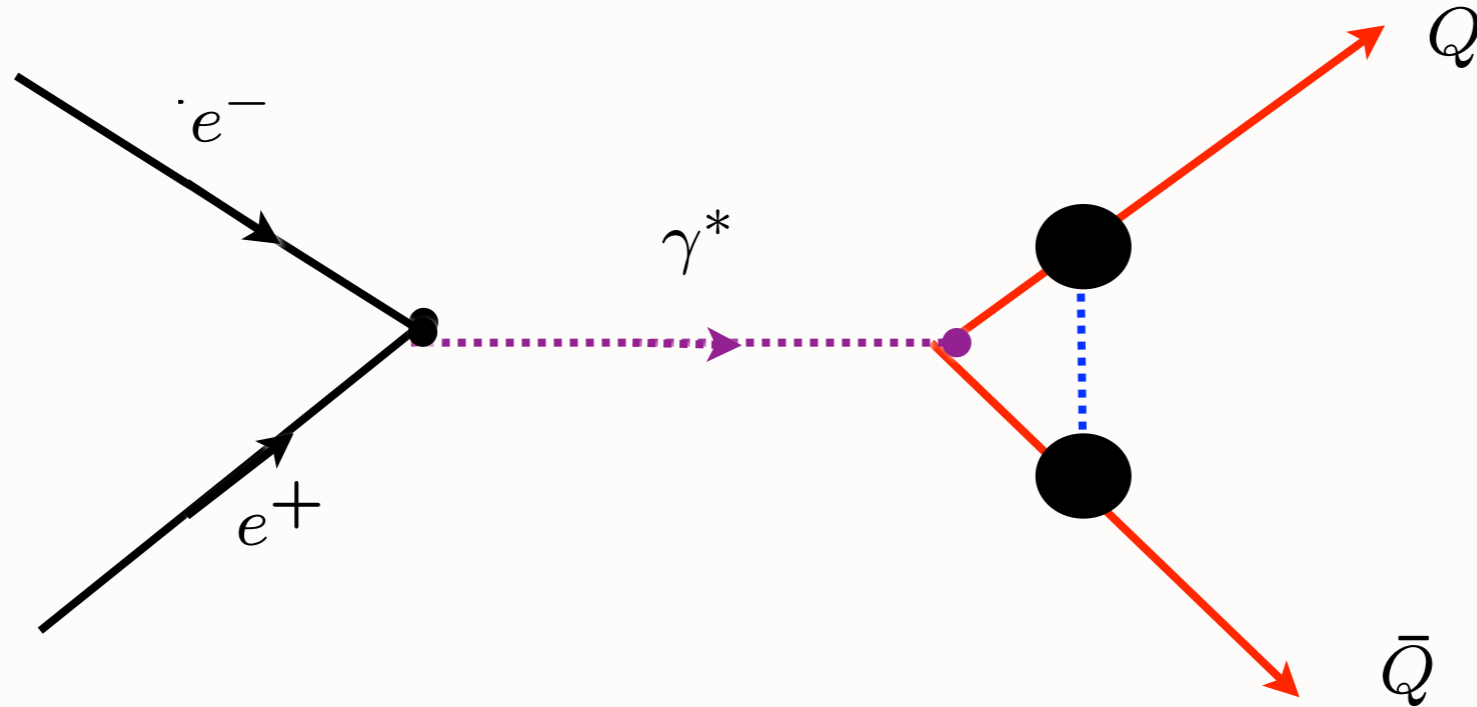
↖  
**Higher Twist from  
Hadron Dynamics**

↖  
**Intrinsic Heavy  
Quarks**

↑  
**Light by Light  
Loops**

***BLM/PMC: Absorb  $\beta$ -terms into running coupling***

$$\mathcal{O} = C(\alpha_s(Q^{*2})) + D(\frac{m_q^2}{Q^2}) + E(\frac{\Lambda_{QCD}^2}{Q^2}) + F(\frac{\Lambda_{QCD}^2}{m_Q^2}) + G(\frac{m_q^2}{m_Q^2})$$



Hoang, Kuhn, Teubner, sjb

$$F_1 + F_2 = \left[ 1 - 2 \frac{\alpha_s (se^{3/4}/4)}{\pi} \right] \times \left[ 1 + \frac{\pi \alpha_s (sv^2)}{4v} \right]$$

Angular distributions of massive quarks close to threshold.

*Example of Multiple BLM Scales*

**Need QCD coupling at small scales at low relative velocity v**

# Need to set multiple renormalization scales -- Lensing, DGLAP, ERBL Evolution ...

*PMC/BLM*

**No renormalization scale ambiguity**

**Result is independent of  
Renormalization scheme  
and initial scale**

**Apply to Evolution kernels,  
hard subprocesses**

**Eliminates unnecessary systematic  
uncertainty**

*Xing-Gang Wu*

*Leonardo di Giustino, SfB*

*Choose renormalization scheme; e.g.  $\alpha_s^R(\mu_R^{\text{init}})$*

*Choose  $\mu_R^{\text{init}}$ ; arbitrary initial renormalization scale*

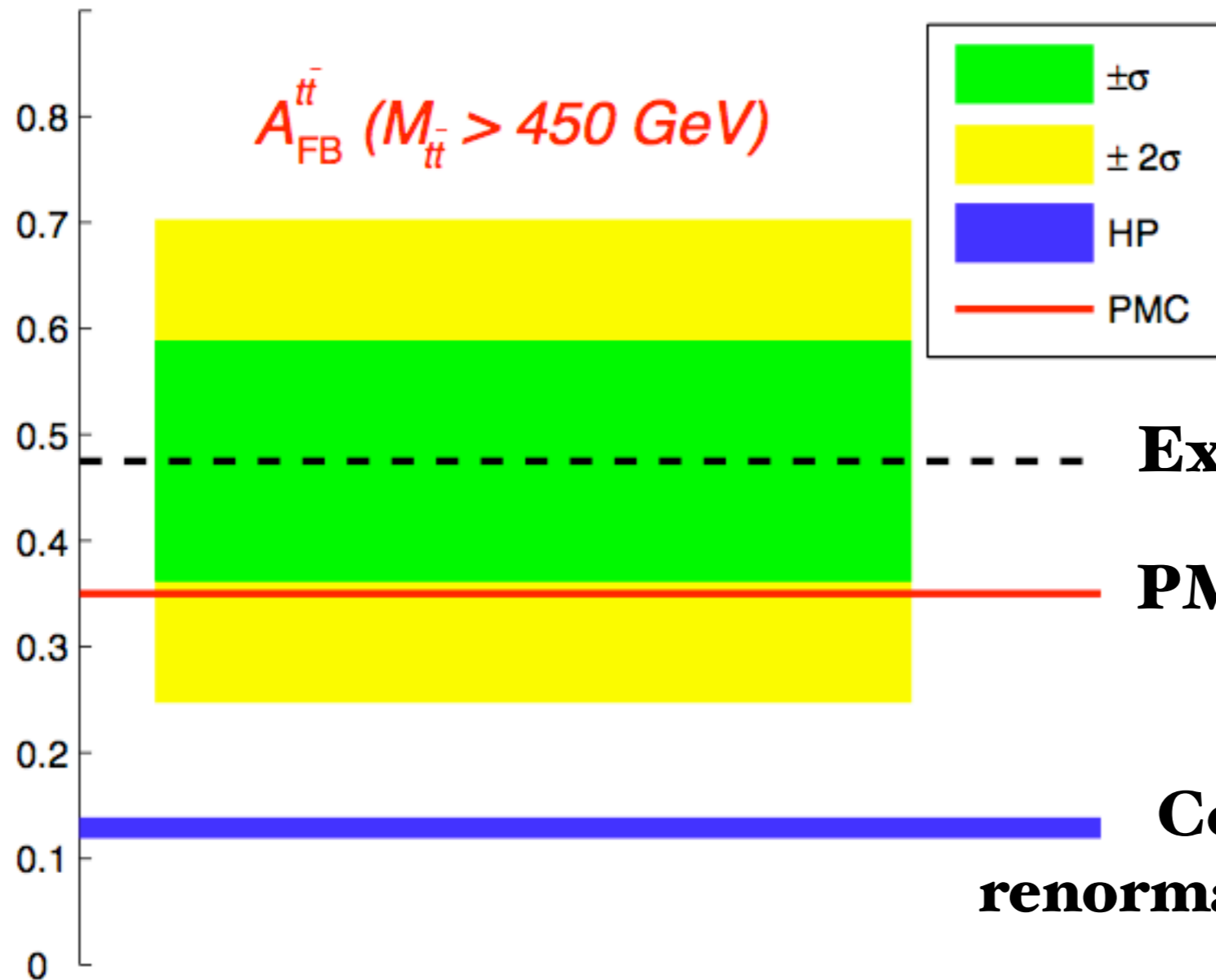
*Identify  $\{\beta_i^R\}$  – terms using  $n_f$  – terms  
through the PMC – BLM correspondence principle*

*Shift scale of  $\alpha_s$  to  $\mu_R^{\text{PMC}}$  to eliminate  $\{\beta_i^R\}$  – terms*

*Conformal Series*

*Result is independent of  $\mu_R^{\text{init}}$  and scheme at fixed order*

***Principle of Maximum Conformality***



**Experimental asymmetry**

**PMC Prediction**

**Conventional: guess  
renormalization scale and range**

$t\bar{t}$  asymmetry predicted by pQCD NNLO within  
 $1\sigma$  of CDF/D0 measurements using PMC/BLM scale setting

# The Renormalization Scale Problem

- **No renormalization scale ambiguity in QED**
- **Gell Mann-Low QED Coupling defined from physical observable**
- **Sums all Vacuum Polarization Contributions**
- **Recover conformal series**
- **Renormalization Scale in QED scheme: Identical to Photon Virtuality**
- **Analytic: Reproduces lepton-pair thresholds -- number of active leptons set**
- **Examples: muonic atoms,  $g-2$ , Lamb Shift**
- **Time-like and Space-like QED Coupling related by analyticity**
- **Uses Dressed Skeleton Expansion**
- **Results are scheme independent!**
- *Predictions for physical observables cannot be scheme dependent*

# Define QCD Coupling from Observables

Grunberg

**Effective Charges: analytic at quark mass thresholds, finite at small momenta**

$$R_{e^+e^- \rightarrow X}(s) \equiv 3 \sum_q e_q^2 \left[ 1 + \frac{\alpha_R(s)}{\pi} \right]$$

$$\Gamma(\tau \rightarrow X e \nu)(m_\tau^2) \equiv \Gamma_0(\tau \rightarrow u \bar{d} e \nu) \times \left[ 1 + \frac{\alpha_\tau(m_\tau^2)}{\pi} \right]$$

**Commensurate scale relations:**

**Relate observable to observable at commensurate scales**

**H.Lu, Rathsmann, sjb**



## Relate Observables to Each Other

- Eliminate intermediate scheme
- No scale ambiguity
- Transitive!
- Commensurate Scale Relations
- Conformal Template
- Example: Generalized Crewther Relation

$$R_{e^+e^-}(Q^2) \equiv 3 \sum_{\text{flavors}} e_q^2 \left[ 1 + \frac{\alpha_R(Q)}{\pi} \right].$$

$$\int_0^1 dx [g_1^{ep}(x, Q^2) - g_1^{en}(x, Q^2)] \equiv \frac{1}{3} \left| \frac{g_A}{g_V} \right| \left[ 1 - \frac{\alpha_{g_1}(Q)}{\pi} \right]$$

# *Generalized Crewther Relation*

$$\left[1 + \frac{\alpha_R(s^*)}{\pi}\right] \left[1 - \frac{\alpha_{g_1}(q^2)}{\pi}\right] = 1$$

$$\sqrt{s^*} \simeq 0.52Q$$

*Conformal relation true to all orders in  
perturbation theory*

*No radiative corrections to axial anomaly*

*Nonconformal terms set relative scales (BLM)*

*No renormalization scale ambiguity!*

**Both observables go through new quark thresholds  
at commensurate scales!**

$$\begin{aligned}
\frac{\alpha_R(Q)}{\pi} = & \frac{\alpha_{\overline{\text{MS}}}(Q)}{\pi} + \left( \frac{\alpha_{\overline{\text{MS}}}(Q)}{\pi} \right)^2 \left[ \left( \frac{41}{8} - \frac{11}{3} \zeta_3 \right) C_A - \frac{1}{8} C_F + \left( -\frac{11}{12} + \frac{2}{3} \zeta_3 \right) f \right] \\
& + \left( \frac{\alpha_{\overline{\text{MS}}}(Q)}{\pi} \right)^3 \left\{ \left( \frac{90445}{2592} - \frac{2737}{108} \zeta_3 - \frac{55}{18} \zeta_5 - \frac{121}{432} \pi^2 \right) C_A^2 + \left( -\frac{127}{48} - \frac{143}{12} \zeta_3 + \frac{55}{3} \zeta_5 \right) C_A C_F - \frac{23}{32} C_F^2 \right. \\
& + \left[ \left( -\frac{970}{81} + \frac{224}{27} \zeta_3 + \frac{5}{9} \zeta_5 + \frac{11}{108} \pi^2 \right) C_A + \left( -\frac{29}{96} + \frac{19}{6} \zeta_3 - \frac{10}{3} \zeta_5 \right) C_F \right] f \\
& \left. + \left( \frac{151}{162} - \frac{19}{27} \zeta_3 - \frac{1}{108} \pi^2 \right) f^2 + \left( \frac{11}{144} - \frac{1}{6} \zeta_3 \right) \frac{d^{abc} d^{abc}}{C_F d(R)} \frac{\left( \sum_f Q_f \right)^2}{\sum_f Q_f^2} \right\}.
\end{aligned}$$

$$\begin{aligned}
\frac{\alpha_{g_1}(Q)}{\pi} = & \frac{\alpha_{\overline{\text{MS}}}(Q)}{\pi} + \left( \frac{\alpha_{\overline{\text{MS}}}(Q)}{\pi} \right)^2 \left[ \frac{23}{12} C_A - \frac{7}{8} C_F - \frac{1}{3} f \right] \\
& + \left( \frac{\alpha_{\overline{\text{MS}}}(Q)}{\pi} \right)^3 \left\{ \left( \frac{5437}{648} - \frac{55}{18} \zeta_5 \right) C_A^2 + \left( -\frac{1241}{432} + \frac{11}{9} \zeta_3 \right) C_A C_F + \frac{1}{32} C_F^2 \right. \\
& \left. + \left[ \left( -\frac{3535}{1296} - \frac{1}{2} \zeta_3 + \frac{5}{9} \zeta_5 \right) C_A + \left( \frac{133}{864} + \frac{5}{18} \zeta_3 \right) C_F \right] f + \frac{115}{648} f^2 \right\}.
\end{aligned}$$

**Eliminate MSbar,  
Find Amazing Simplification**

# Relate Observables to Each Other

- Eliminate intermediate scheme
- No scale ambiguity
- Transitive!
- Commensurate Scale Relations
- **Conformal Template**
- Example: Generalized Crewther Relation

$$R_{e^+e^-}(Q^2) \equiv 3 \sum_{\text{flavors}} e_q^2 \left[ 1 + \frac{\alpha_R(Q)}{\pi} \right].$$

$$\int_0^1 dx [g_1^{ep}(x, Q^2) - g_1^{en}(x, Q^2)] \equiv \frac{1}{3} \left| \frac{g_A}{g_V} \right| \left[ 1 - \frac{\alpha_{g_1}(Q)}{\pi} \right]$$

$$R_{e^+e^-}(Q^2) \equiv 3 \sum_{\text{flavors}} e_q^2 \left[ 1 + \frac{\alpha_R(Q)}{\pi} \right].$$

$$\int_0^1 dx [g_1^{ep}(x, Q^2) - g_1^{en}(x, Q^2)] \equiv \frac{1}{3} \left| \frac{g_A}{g_V} \right| \left[ 1 - \frac{\alpha_{g_1}(Q)}{\pi} \right]$$

$$\frac{\alpha_{g_1}(Q)}{\pi} = \frac{\alpha_R(Q^*)}{\pi} - \left( \frac{\alpha_R(Q^{**})}{\pi} \right)^2 + \left( \frac{\alpha_R(Q^{***})}{\pi} \right)^3$$

*Geometric Series in Conformal QCD*

*Generalized Crewther Relation*

Lu, Kataev, Gabadadze, Sjb

# Define QCD Coupling from Observables

Grunberg

**Effective Charges: analytic at quark mass thresholds, finite at small momenta**

$$R_{e^+e^- \rightarrow X}(s) \equiv 3 \sum_q e_q^2 \left[ 1 + \frac{\alpha_R(s)}{\pi} \right]$$

$$\Gamma(\tau \rightarrow X e \nu)(m_\tau^2) \equiv \Gamma_0(\tau \rightarrow u \bar{d} e \nu) \times \left[ 1 + \frac{\alpha_\tau(m_\tau^2)}{\pi} \right]$$

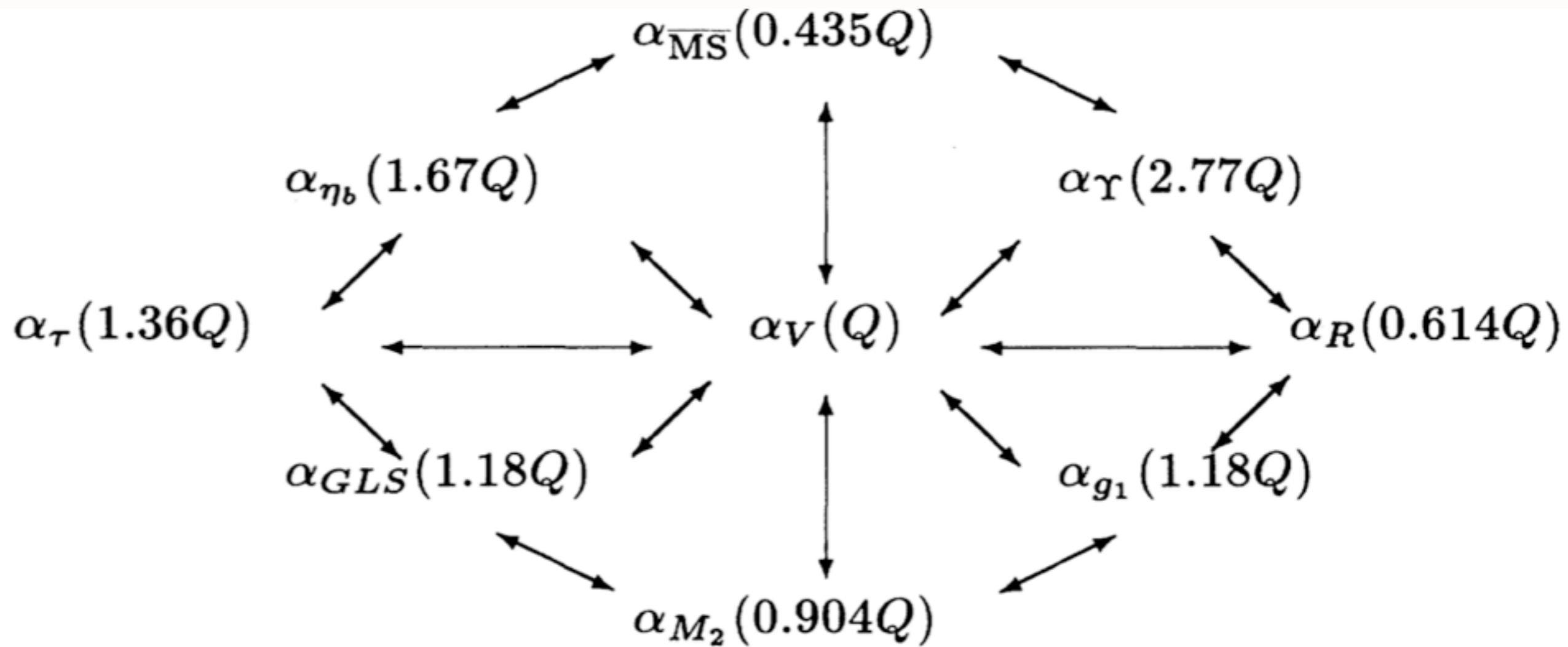
**Commensurate scale relations:**

**Relate observable to observable at commensurate scales**

**H.Lu, Rathsmann, sjb**

$$\frac{\alpha_{\tau}(M_{\tau})}{\pi} = \frac{\alpha_R(Q^*)}{\pi},$$

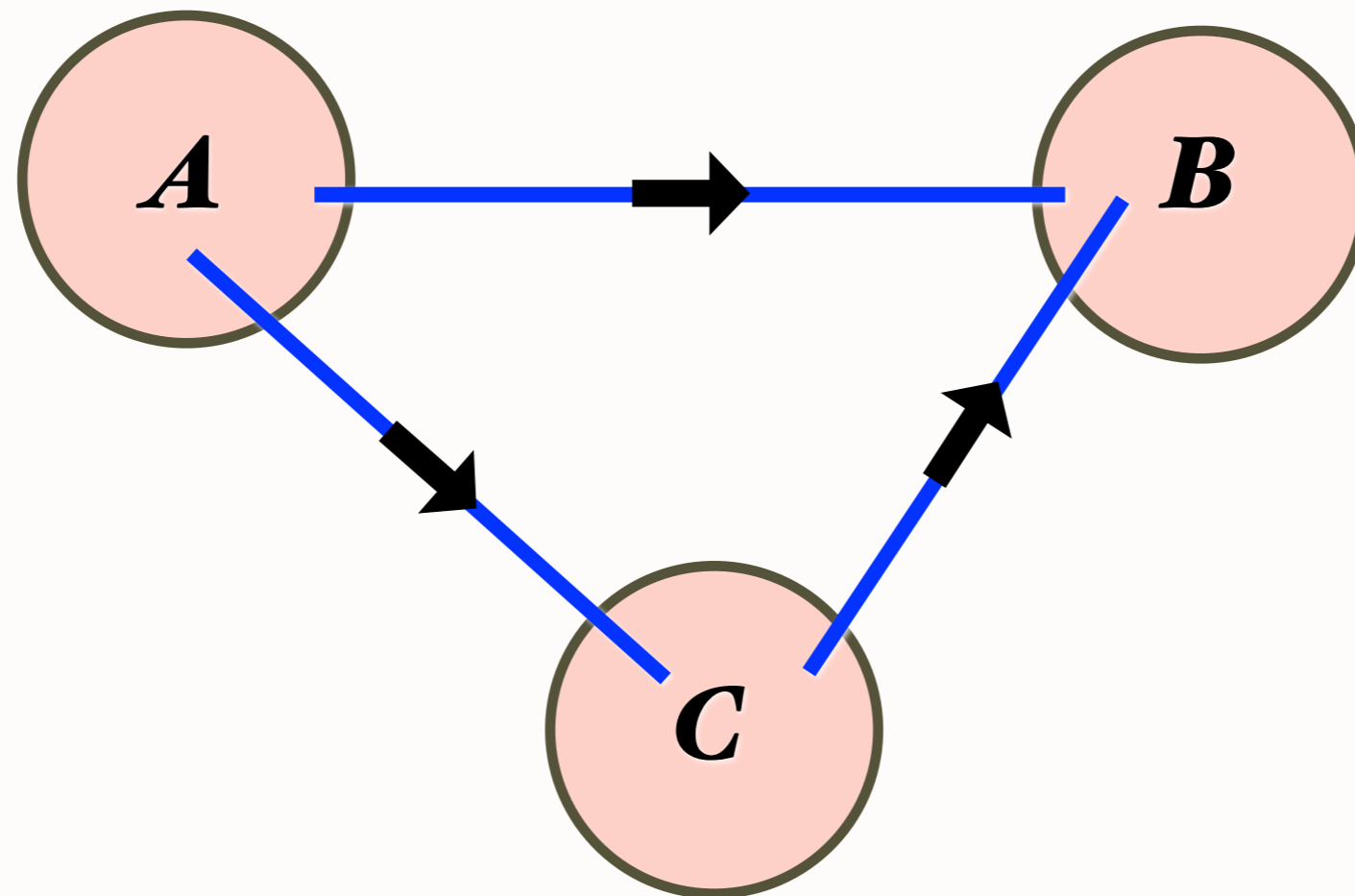
$$Q^* = M_{\tau} \exp \left[ -\frac{19}{24} - \frac{169}{128} \frac{\alpha_R(M_{\tau})}{\pi} \right]$$





# Transitivity Property of Renormalization Group

Relation of observables must be independent of intermediate scheme

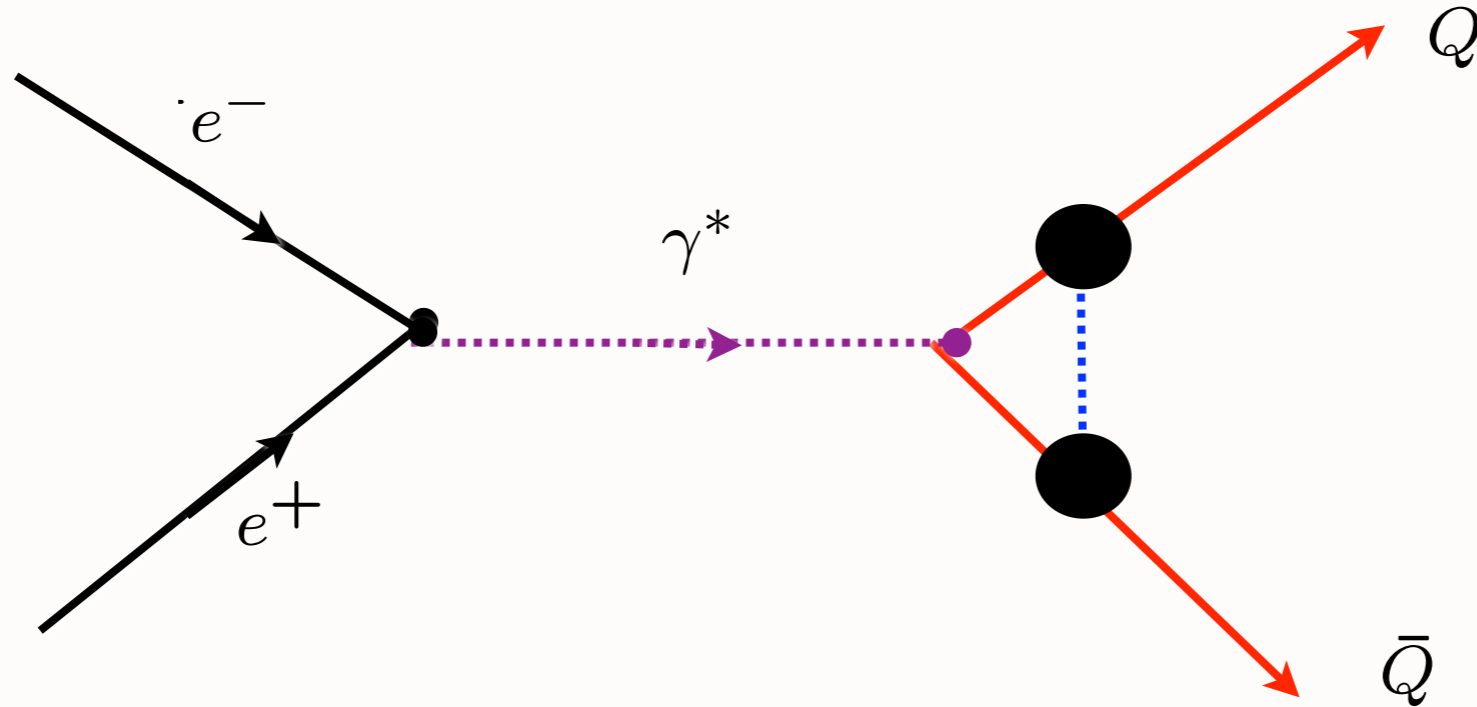


$A \rightarrow C$      $C \rightarrow B$     identical to     $A \rightarrow B$

*Violated by PMS!*

# Goals

- Test QCD to maximum precision
- High precision determination of  $\alpha_s(Q^2)$  at all scales
- Relate observable to observable --no scheme or scale ambiguity
- Eliminate renormalization scale ambiguity in a scheme-independent manner
- Relate renormalization schemes without ambiguity
- Maximize sensitivity to new physics at the colliders



Hoang, Kuhn, Teubner, sjb

$$F_1 + F_2 = \left[ 1 - 2 \frac{\alpha_s (s e^{3/4} / 4)}{\pi} \right] \times \left[ 1 + \frac{\pi \alpha_s (s v^2)}{4v} \right]$$

Angular distributions of massive quarks close to threshold.

## Example of Multiple BLM Scales

**Need QCD coupling at small scales at low relative velocity  $v$**

## *Myths concerning scale setting*

- Renormalization scale “unphysical”: No optimal physical scale
- Can ignore possibility of multiple physical scales
- Accuracy of PQCD prediction can be judged by taking arbitrary guess with an arbitrary range
- Factorization scale should be taken equal to renormalization scale

$$\mu_F = \mu_R$$

**Guessing the scale: Wrong in QED. Scheme dependent!**

$$R_{e^+e^-}(Q^2) \equiv 3 \sum_{\text{flavors}} e_q^2 \left[ 1 + \frac{\alpha_R(Q)}{\pi} \right].$$

$$\int_0^1 dx [g_1^{ep}(x, Q^2) - g_1^{en}(x, Q^2)] \equiv \frac{1}{3} \left| \frac{g_A}{g_V} \right| \left[ 1 - \frac{\alpha_{g_1}(Q)}{\pi} \right]$$

$$\frac{\alpha_{g_1}(Q)}{\pi} = \frac{\alpha_R(Q^*)}{\pi} - \left( \frac{\alpha_R(Q^{**})}{\pi} \right)^2 + \left( \frac{\alpha_R(Q^{***})}{\pi} \right)^3$$

*Geometric Series in Conformal QCD*

*Generalized Crewther Relation*

Lu, Kataev, Gabadadze, Sjb

# *Generalized Crewther Relation*

$$\left[1 + \frac{\alpha_R(s^*)}{\pi}\right] \left[1 - \frac{\alpha_{g_1}(q^2)}{\pi}\right] = 1$$

$$\sqrt{s^*} \simeq 0.52Q$$

*Conformal relation true to all orders in  
perturbation theory*

*No radiative corrections to axial anomaly*

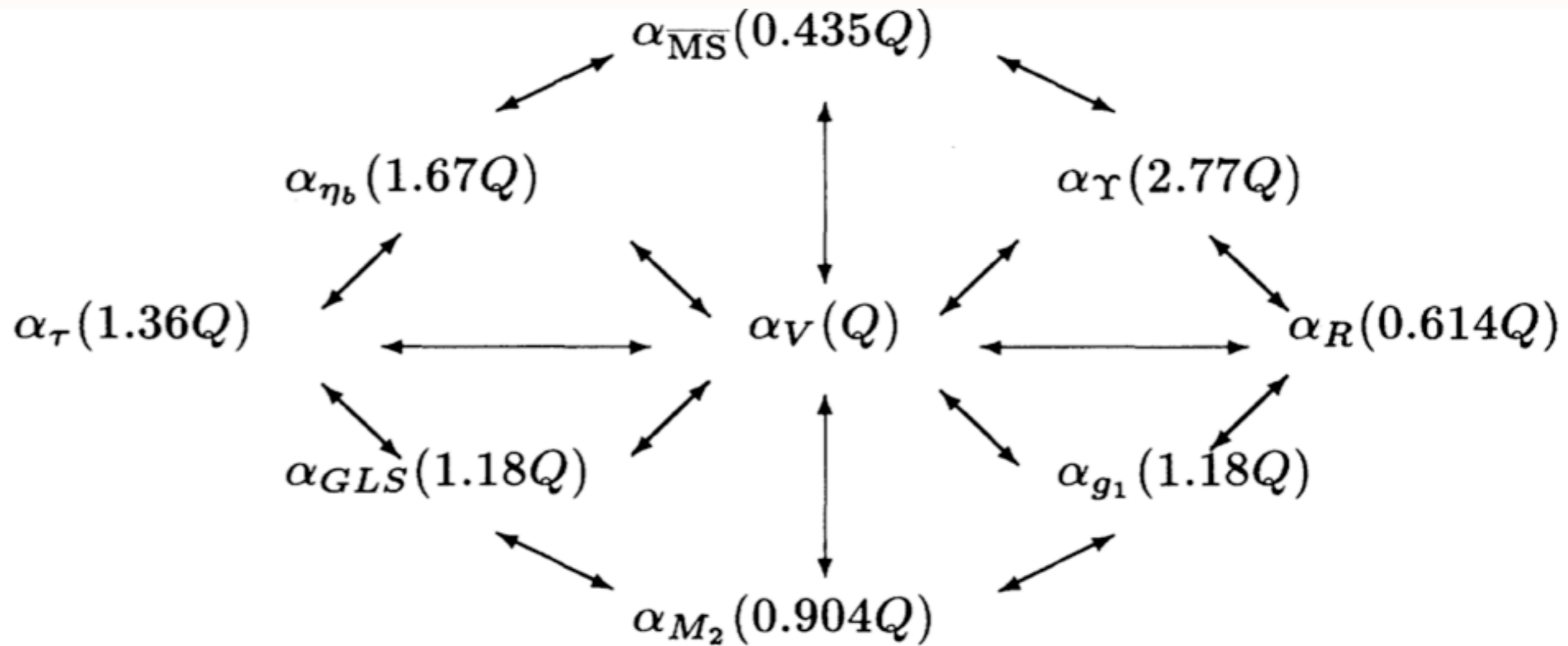
*Nonconformal terms set relative scales (BLM)*

*No renormalization scale ambiguity!*

**Both observables go through new quark thresholds  
at commensurate scales!**

$$\frac{\alpha_{\tau}(M_{\tau})}{\pi} = \frac{\alpha_R(Q^*)}{\pi},$$

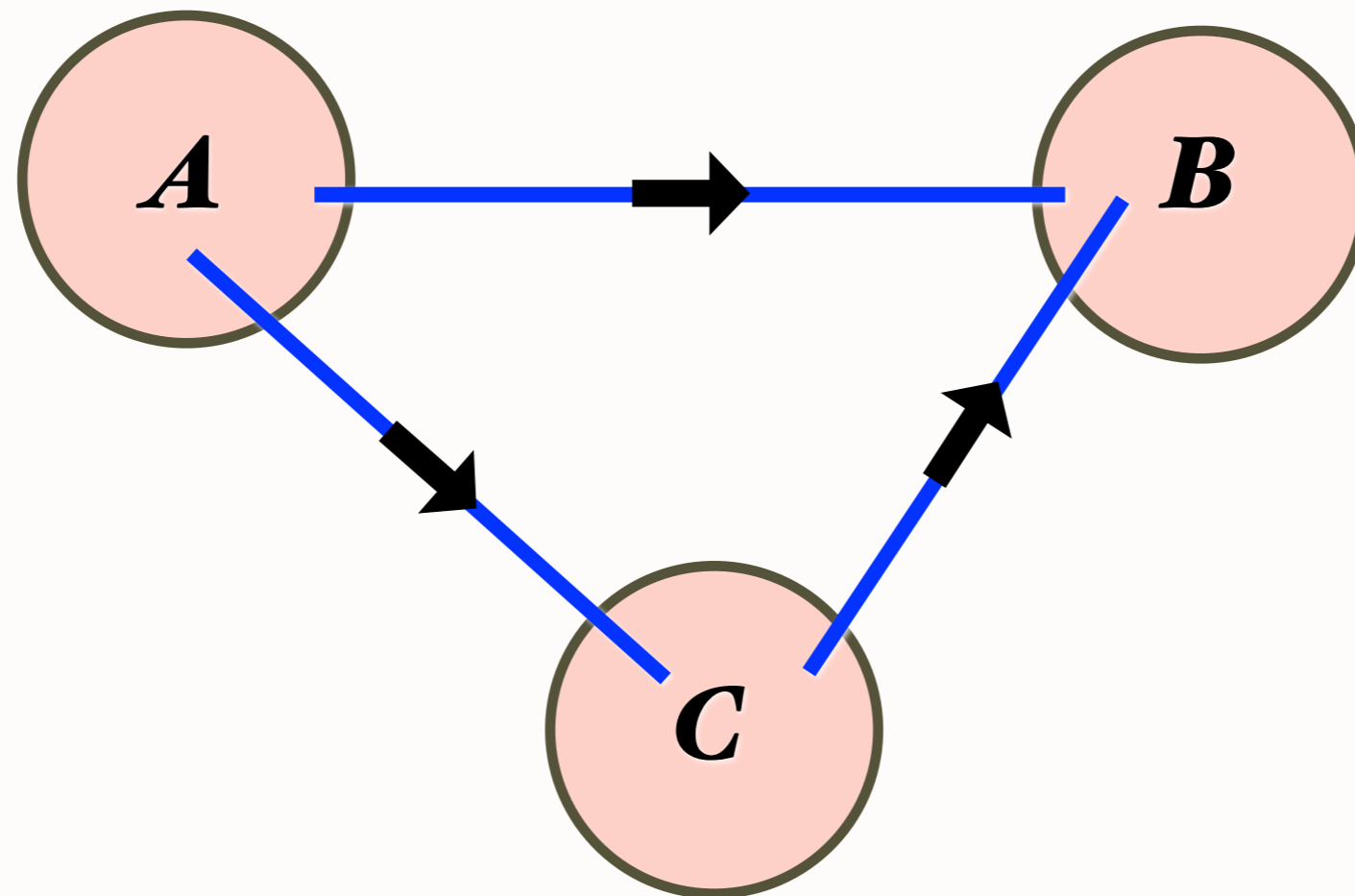
$$Q^* = M_{\tau} \exp \left[ -\frac{19}{24} - \frac{169}{128} \frac{\alpha_R(M_{\tau})}{\pi} \right]$$





# Transitivity Property of Renormalization Group

Relation of observables must be independent of intermediate scheme



$A \rightarrow C$      $C \rightarrow B$     identical to     $A \rightarrow B$

*Violated by PMS!*

# *Hot Topics in QCD*

- *Intrinsic Heavy Quarks*
- *Breakdown of pQCD Leading-Twist Factorization*
- *Top/anti-Top asymmetry*
- *Non-universal antishadowing*
- *Demise of QCD Vacuum Condensates*
- *Elimination of the QCD Renormalization Scale Ambiguity*
- *AdS/QCD and Light-Front Holography*

*Crucial to Understand QCD to High Precision to  
Illuminate New Physics*

*Each element of  
flash photograph  
illuminated  
at same LF time*

$$\tau = t + z/c$$

*Evolve in LF time*

$$P^- = i \frac{d}{d\tau}$$

*Eigenstate -- independent of  $\tau$*

**Measurements  
never at fixed time  $t$**



Exact frame-independent formulation of nonperturbative QCD!

$$L^{QCD} \rightarrow H_{LF}^{QCD}$$

$$H_{LF}^{QCD} = \sum_i \left[ \frac{m^2 + k_{\perp}^2}{x} \right]_i + H_{LF}^{int}$$

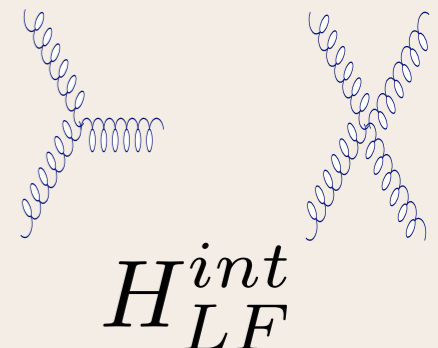
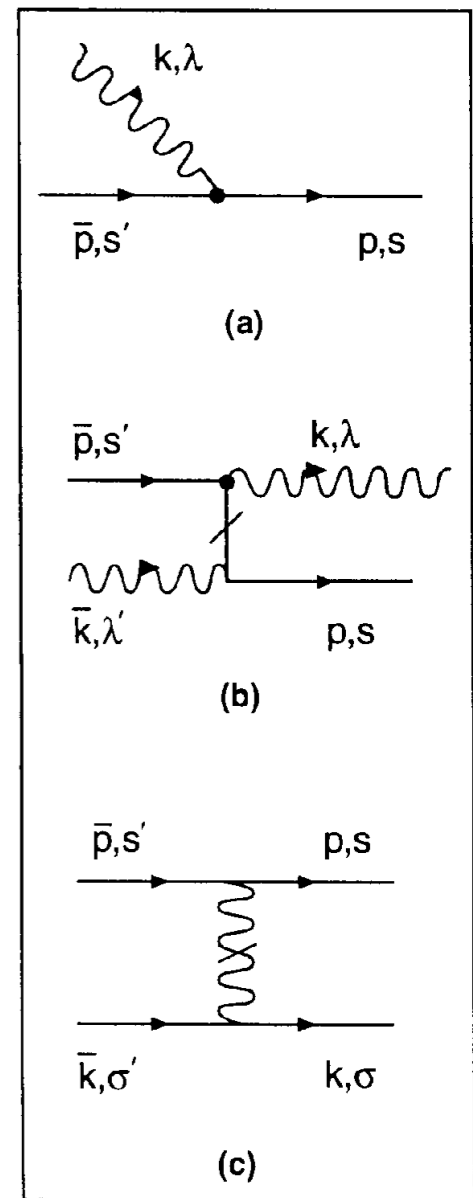
$H_{LF}^{int}$ : Matrix in Fock Space

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

$$|p, S_z\rangle = \sum_{n=3} \psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; x_i, \vec{k}_{\perp i}, \lambda_i\rangle$$

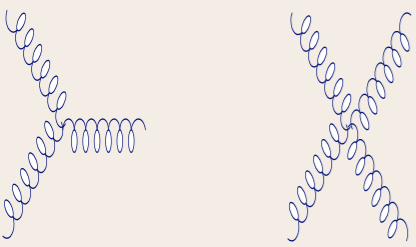
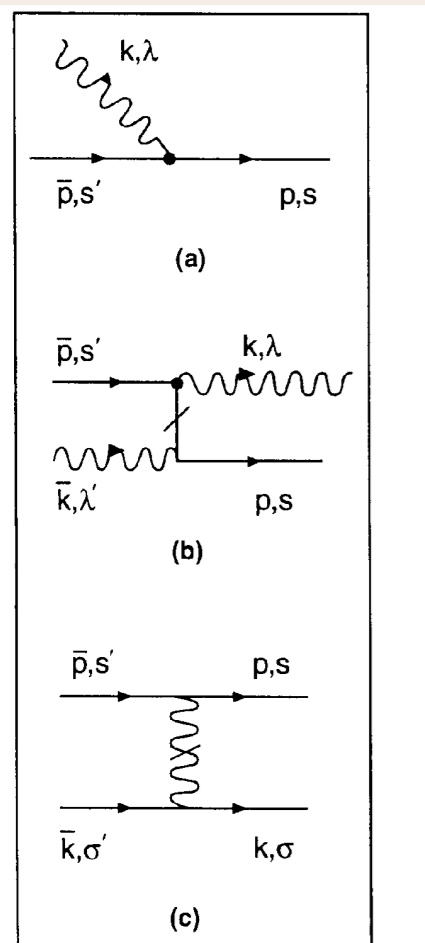
Eigenvalues and Eigensolutions give Hadronic Spectrum and Light-Front wavefunctions

**LFWFs: Off-shell in P- and invariant mass**



# Light-Front QCD

## Heisenberg Matrix Formulation



$$H_{LC}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

# DLCQ

## Discretized Light-Cone Quantization

n	Sector	1 q $\bar{q}$	2 gg	3 q $\bar{q}$ g	4 q $\bar{q}$ q $\bar{q}$	5 gg g	6 q $\bar{q}$ gg	7 q $\bar{q}$ q $\bar{q}$ g	8 q $\bar{q}$ q $\bar{q}$ q $\bar{q}$	9 gg gg	10 q $\bar{q}$ gg g	11 q $\bar{q}$ q $\bar{q}$ gg	12 q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ g	13 q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ q $\bar{q}$
1	q $\bar{q}$	[Diagram]	[Diagram]	[Diagram]	[Diagram]	.	[Diagram]	.	.	.	.	.	.	.
2	gg	[Diagram]	[Diagram]	[Diagram]	.	[Diagram]	[Diagram]	.	.	[Diagram]	.	.	.	.
3	q $\bar{q}$ g	[Diagram]	[Diagram]	[Diagram]	[Diagram]	[Diagram]	[Diagram]	[Diagram]	.	.	[Diagram]	.	.	.
4	q $\bar{q}$ q $\bar{q}$	[Diagram]	.	[Diagram]	[Diagram]	.	[Diagram]	[Diagram]	[Diagram]	.	.	[Diagram]	.	.
5	gg g	.	[Diagram]	[Diagram]	.	[Diagram]	[Diagram]	.	.	[Diagram]	[Diagram]	.	.	.
6	q $\bar{q}$ gg	[Diagram]	[Diagram]	[Diagram]	[Diagram]	[Diagram]	[Diagram]	.	.	[Diagram]	[Diagram]	[Diagram]	.	.
7	q $\bar{q}$ q $\bar{q}$ g	.	.	[Diagram]	[Diagram]	.	[Diagram]	[Diagram]	[Diagram]	.	[Diagram]	[Diagram]	[Diagram]	.
8	q $\bar{q}$ q $\bar{q}$ q $\bar{q}$	.	.	.	[Diagram]	.	.	[Diagram]	[Diagram]	.	.	[Diagram]	[Diagram]	[Diagram]
9	gg gg	.	[Diagram]	.	.	[Diagram]	[Diagram]	.	.	[Diagram]	[Diagram]	.	.	.
10	q $\bar{q}$ gg g	.	.	[Diagram]	.	[Diagram]	[Diagram]	[Diagram]	.	[Diagram]	[Diagram]	[Diagram]	.	.
11	q $\bar{q}$ q $\bar{q}$ gg	.	.	.	[Diagram]	.	[Diagram]	[Diagram]	[Diagram]	.	[Diagram]	[Diagram]	[Diagram]	.
12	q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ g	.	.	.	.	.	[Diagram]	[Diagram]	.	.	[Diagram]	[Diagram]	[Diagram]	[Diagram]
13	q $\bar{q}$ q $\bar{q}$ q $\bar{q}$ q $\bar{q}$	.	.	.	.	.	.	[Diagram]	.	.	.	[Diagram]	[Diagram]	[Diagram]

Eigenvalues and Eigensolutions give Hadron Spectrum and Light-Front wavefunctions

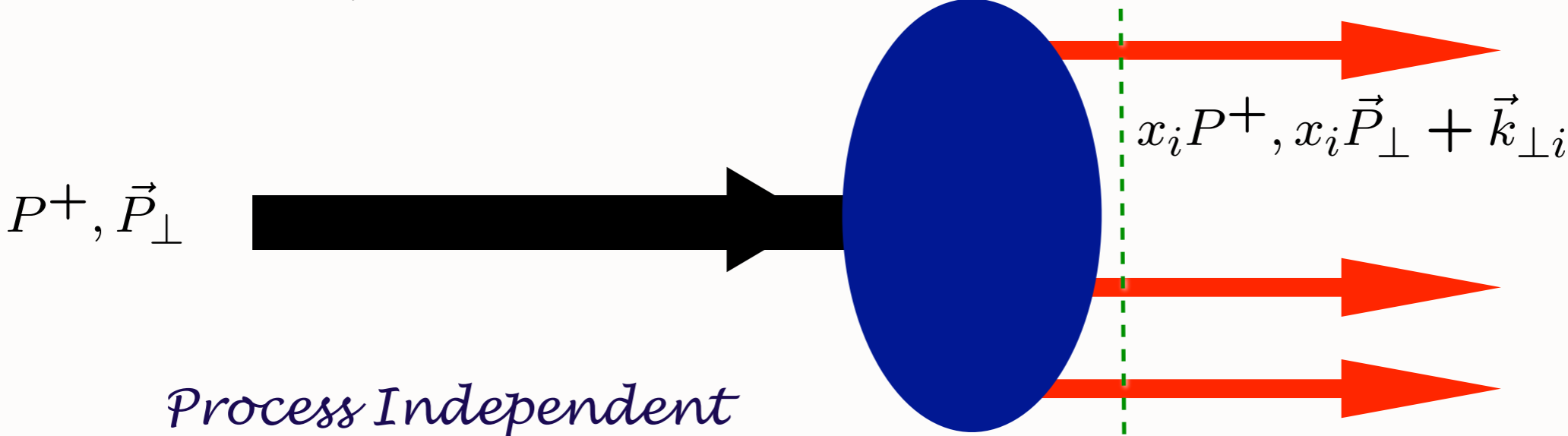
Pauli, Hornbostel & sjb

e.g. solve QCD(1+1): arbitrary color, flavor, quark mass

# Light-Front Wavefunctions: rigorous representation of composite systems in quantum field theory. Eigenstates of QCD Light-Front Hamiltonian

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

Fixed  $\tau = t + z/c$



*Process Independent  
Direct Link to QCD Lagrangian!*

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_{\perp}$$

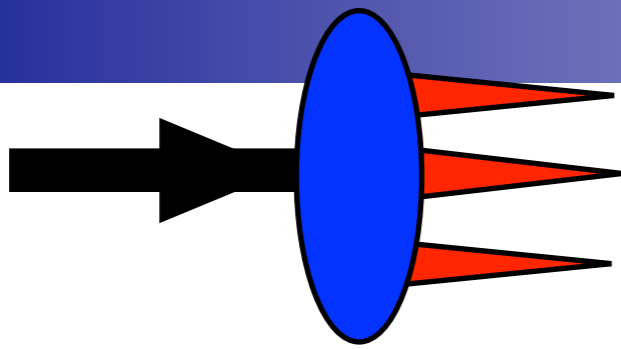
*Invariant under boosts! Independent of  $P^\mu$*

• *Light Front Wavefunctions:*

Lorce

$$\xi = 0$$

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$



Momentum space  $\vec{k}_{\perp} \leftrightarrow \vec{z}_{\perp}$  Position space  
 $\vec{\Delta}_{\perp} \leftrightarrow \vec{b}_{\perp}$

Transverse density in momentum space

Transverse density in position space

GTMDs

$$x, \vec{k}_{\perp}, \vec{b}_{\perp}$$

TMDs

$$x, \vec{k}_{\perp}$$

TMFFs

$$\vec{k}_{\perp}, \vec{b}_{\perp}$$

GPDs

$$x, \vec{b}_{\perp}$$

TMSDs

$$\vec{k}_{\perp}$$

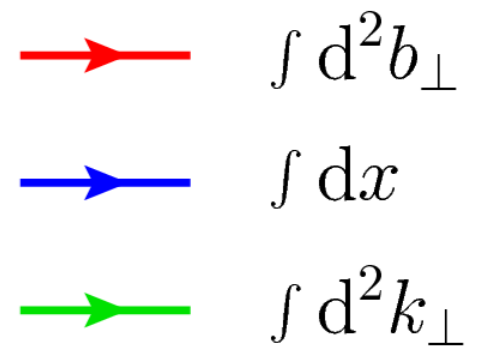
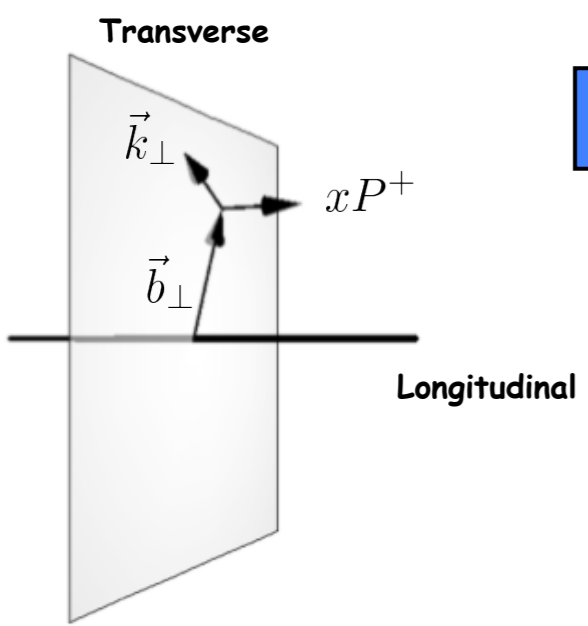
PDFs

$$x,$$

FFs

$$\vec{b}_{\perp}$$

Charges



# Angular Momentum on the Light-Front

$$J^z = \sum_{i=1}^n s_i^z + \sum_{j=1}^{n-1} l_j^z.$$

**Conserved in each  
LF Fock state**

$$l_j^z = -i \left( k_j^1 \frac{\partial}{\partial k_j^2} - k_j^2 \frac{\partial}{\partial k_j^1} \right)$$

**n-1 orbital angular  
momenta**

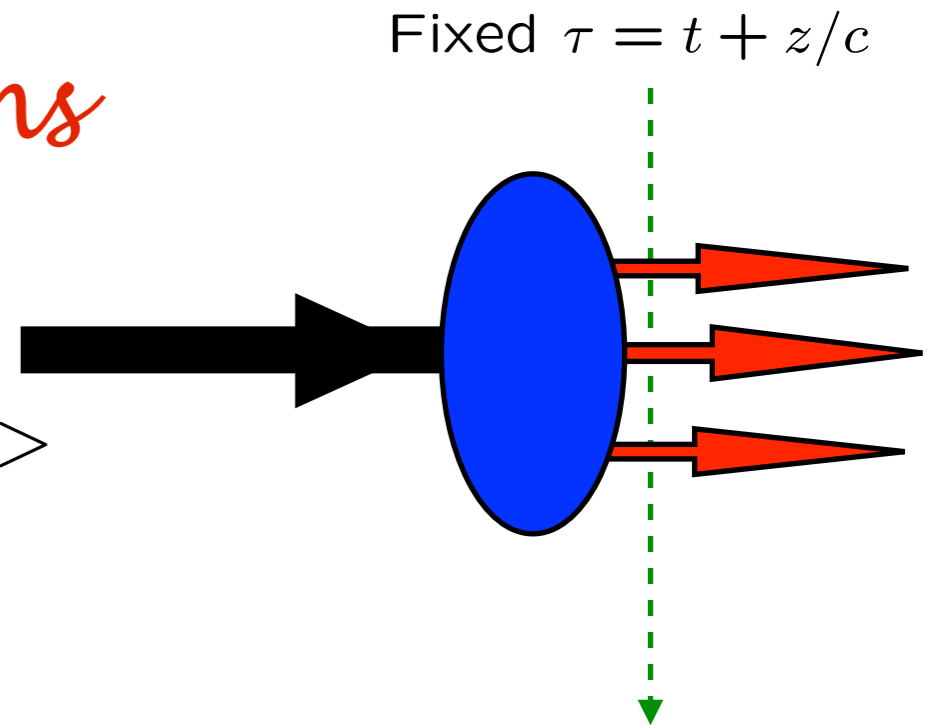
*Nonzero Anomalous Moment --> Nonzero orbital angular momentum*



# Light-Front Wavefunctions

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

$$|p, S_z\rangle = \sum_{n=3} \psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; x_i, \vec{k}_{\perp i}, \lambda_i\rangle$$

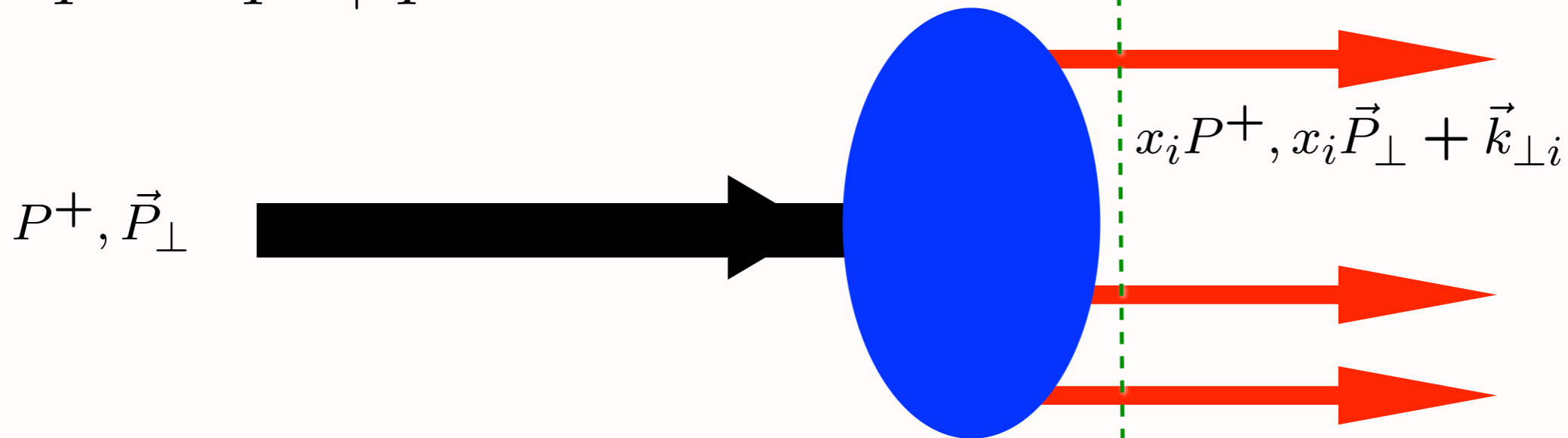


- **Eigenfunctions of the exact QCD LF Hamiltonian**
- **Boost invariant! Independent of  $P^+$ ,  $P_{\perp}$**
- **Compute all observables intrinsic to hadron from LFWFs**
- **Form factors, structure functions, GPDs, transverse momentum distributions**
- **DGLAP and ERBL Evolution Built In**
- **No renormalization scale ambiguity: “Principle of Maximal Conformality”**
- **LF Vacuum Trivial: In-Hadron Condensates -- Eliminate  $10^{45}$  discrepancy with cosmological constant**
- **Pseudo-T-odd observables from Lensing**
- **Angular Momentum Sum Rule for each Fock state**

# Light-Front Wavefunctions: rigorous representation of composite systems in quantum field theory

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

Fixed  $\tau = t + z/c$



*Light-Front Wavefunctions: off invariant mass-shell, infinite # components*

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_{\perp}$$

*Invariant under boosts! Independent of  $p^\mu$*

# Eigensolutions of the LF Hamiltonian:

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

*sum over states with  $n=3, 4, \dots$  constituents*

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

are boost invariant; they are independent of the hadron's energy and momentum  $P^\mu$ .

The light-cone momentum fraction

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

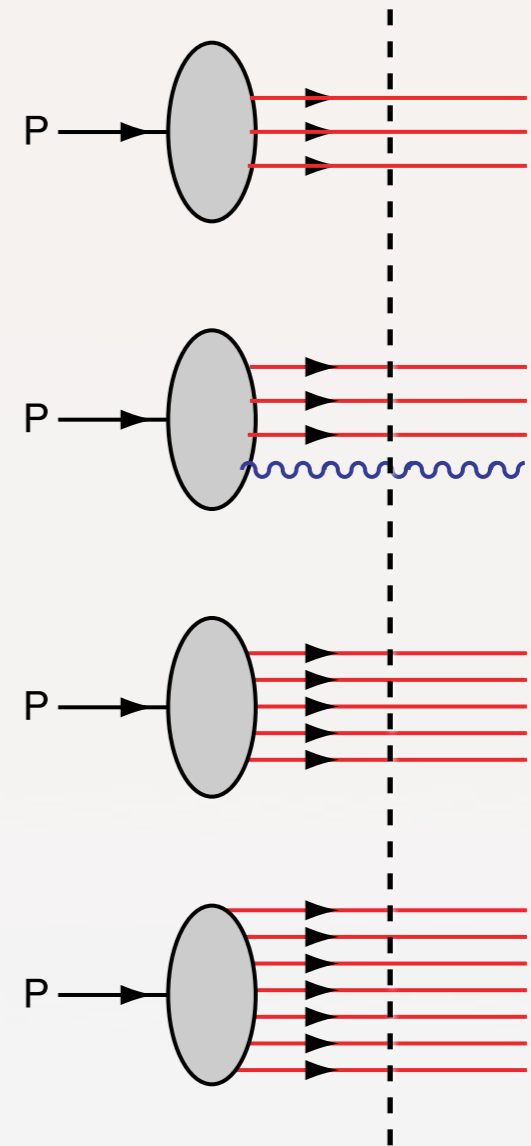
are boost invariant.

$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_i^\perp = \vec{0}^\perp.$$

*Intrinsic heavy quarks*  
 **$s(x), c(x), b(x)$  at high  $x$ !**

$\bar{s}(x) \neq s(x)$   
 $\bar{u}(x) \neq \bar{d}(x)$

**Mueller: gluonic Fock states  $\gg$  BFKL**



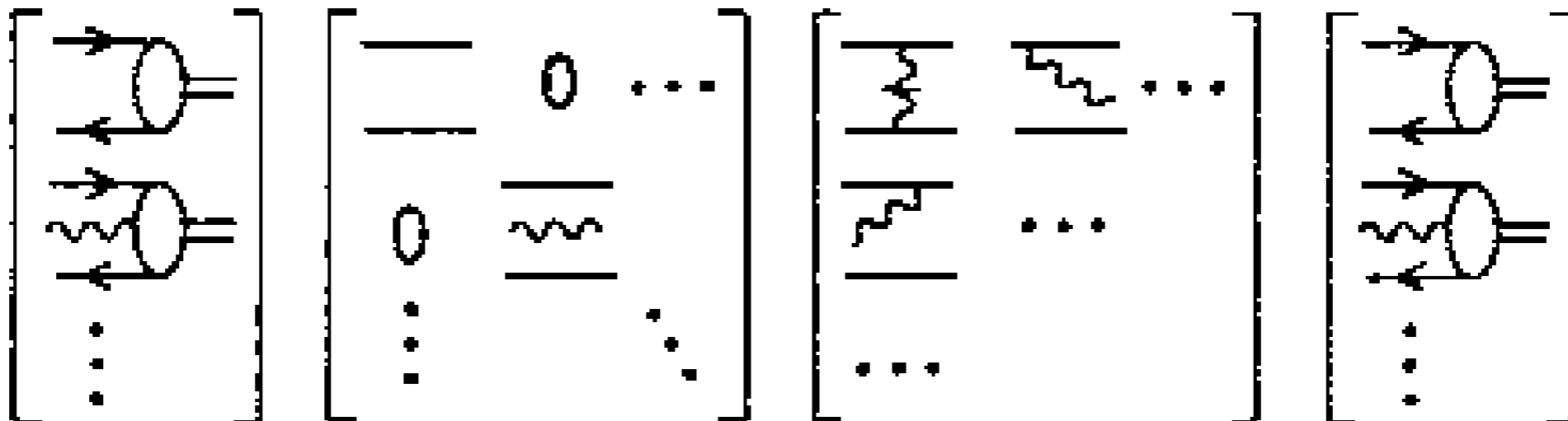
*Fixed LF time*  
*Coupled, infinite set*

**Nuclei: Hidden Color**

# LIGHT-FRONT SCHRODINGER EQUATION

*Direct connection to QCD Lagrangian*

$$\left( M_\pi^2 - \sum_i \frac{\vec{k}_{\perp i}^2 + m_i^2}{x_i} \right) \begin{bmatrix} \psi_{q\bar{q}/\pi} \\ \psi_{q\bar{q}g/\pi} \\ \vdots \end{bmatrix} = \begin{bmatrix} \langle q\bar{q} | V | q\bar{q} \rangle & \langle q\bar{q} | V | q\bar{q}g \rangle & \cdots \\ \langle q\bar{q}g | V | q\bar{q} \rangle & \langle q\bar{q}g | V | q\bar{q}g \rangle & \cdots \\ \vdots & \vdots & \ddots \end{bmatrix} \begin{bmatrix} \psi_{q\bar{q}/\pi} \\ \psi_{q\bar{q}g/\pi} \\ \vdots \end{bmatrix}$$



$$A^+ = 0$$

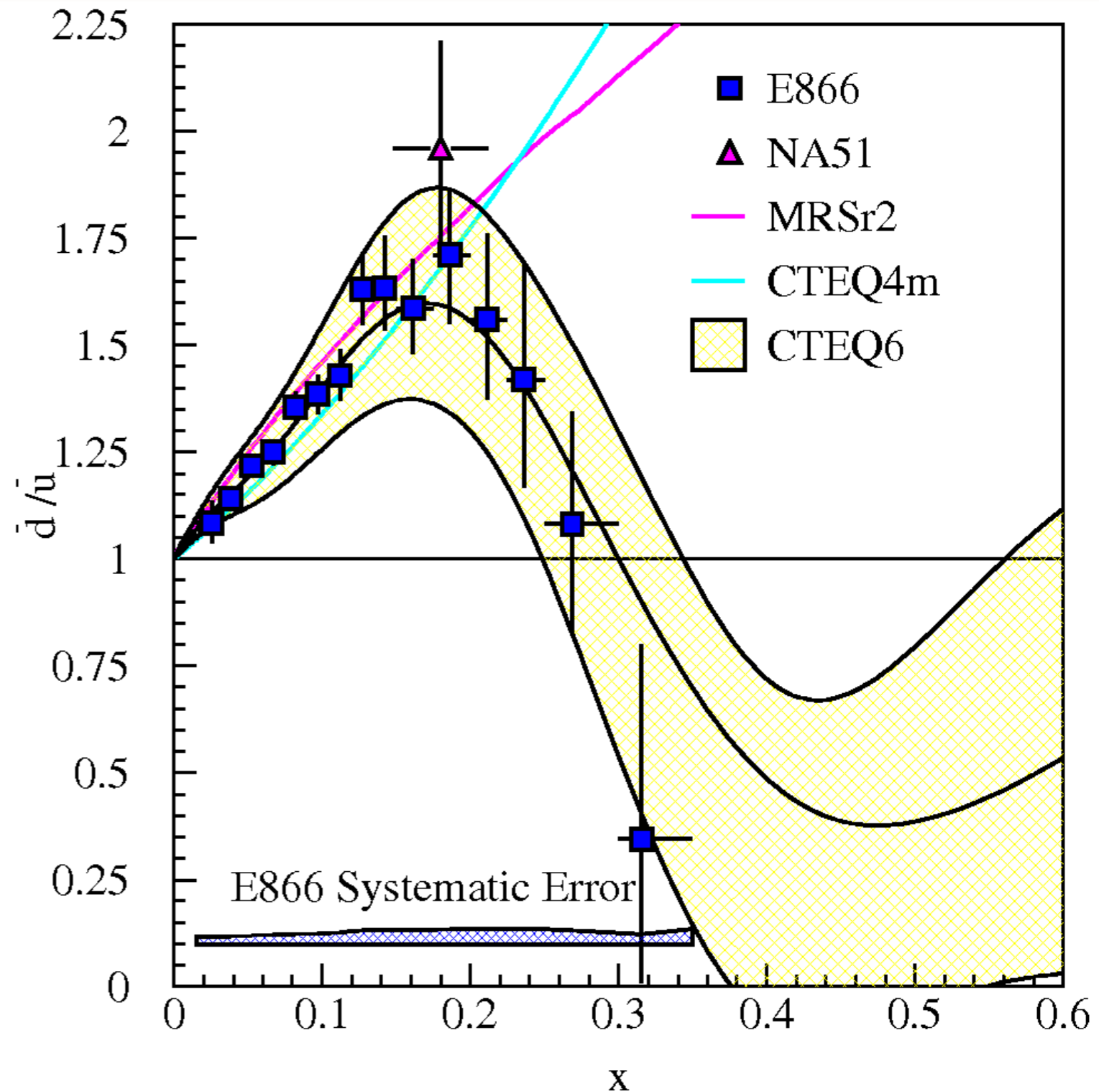
**G.P. Lepage, sjb**

$\bar{d}(x)/\bar{u}(x)$  for  $0.015 \leq x \leq 0.35$

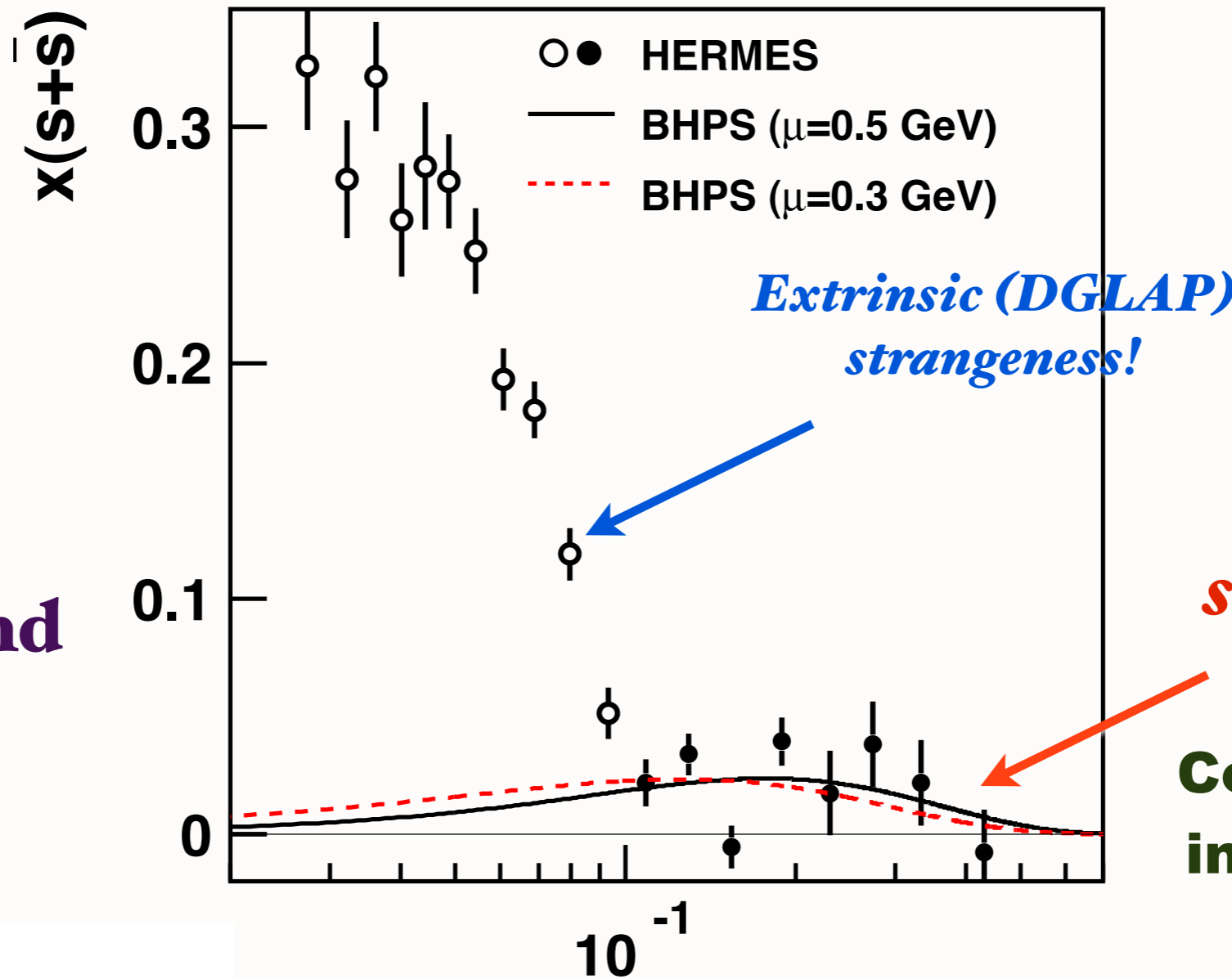
■ E866/NuSea (Drell-Yan)

$$\bar{d}(x) \neq \bar{u}(x)$$

*Intrinsic glue, sea,  
heavy quarks*



# HERMES: Two components to $s(x, Q^2)$ !



**Consistent with intrinsic charm data**

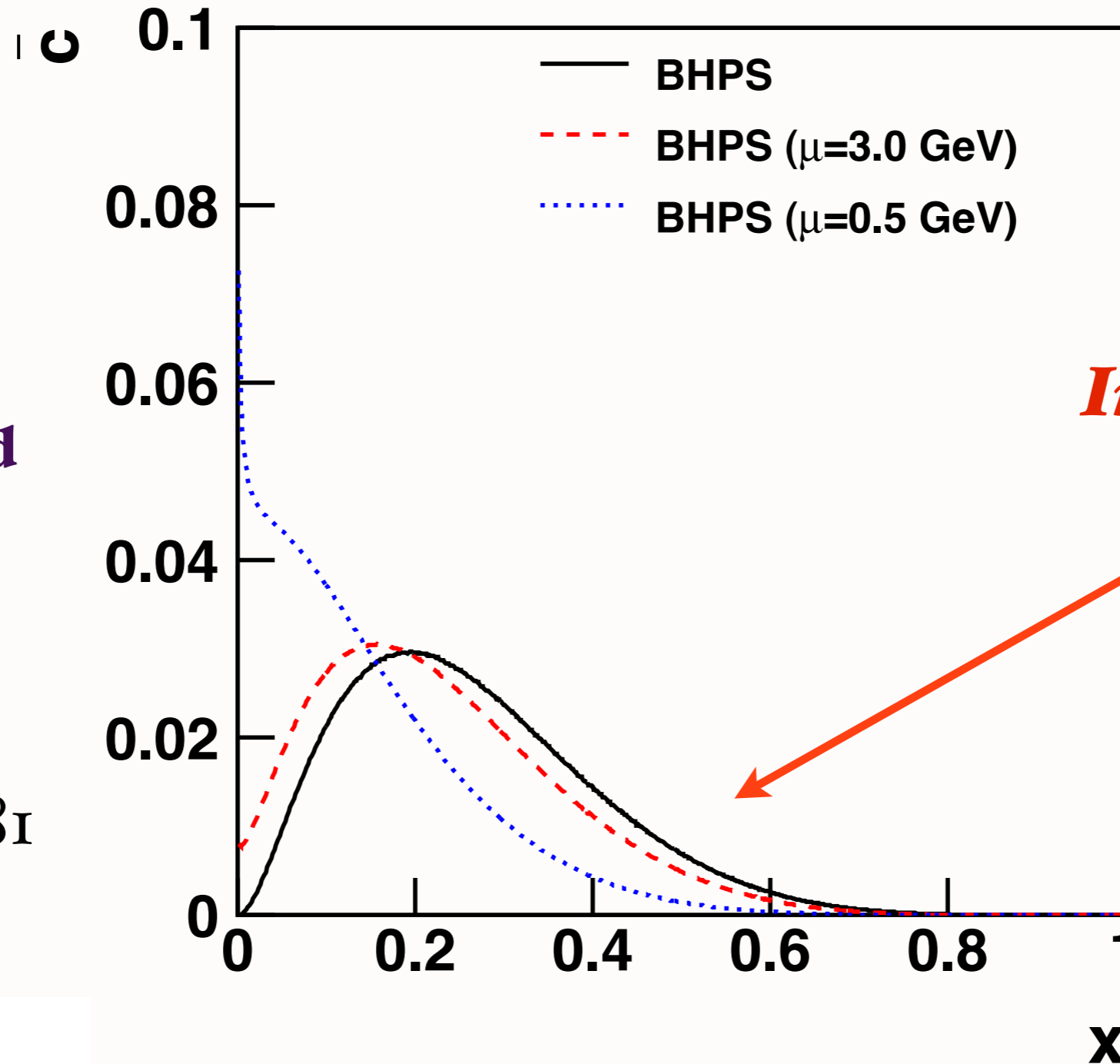
QCD:  $\frac{1}{M_Q^2}$  scaling

Comparison of the HERMES  $x(s(x) + \bar{s}(x))$  data with the calculations based on the BHPs model. The solid and dashed curves are obtained by evolving the BHPs result to  $Q^2 = 2.5 \text{ GeV}^2$  using  $\mu = 0.5 \text{ GeV}$  and  $\mu = 0.3 \text{ GeV}$ , respectively. The normalizations of the calculations are adjusted to fit the data at  $x > 0.1$  with statistical errors only, denoted by solid circles.

**W. C. Chang and J.-C. Peng**  
arXiv:1105.2381

$$s(x, Q^2) = s(x, Q^2)_{\text{extrinsic}} + s(x, Q^2)_{\text{intrinsic}}$$

# QCD ( $1/m_Q^2$ ) scaling: predict IC



W. C. Chang and  
J.-C. Peng

arXiv:1105.2381

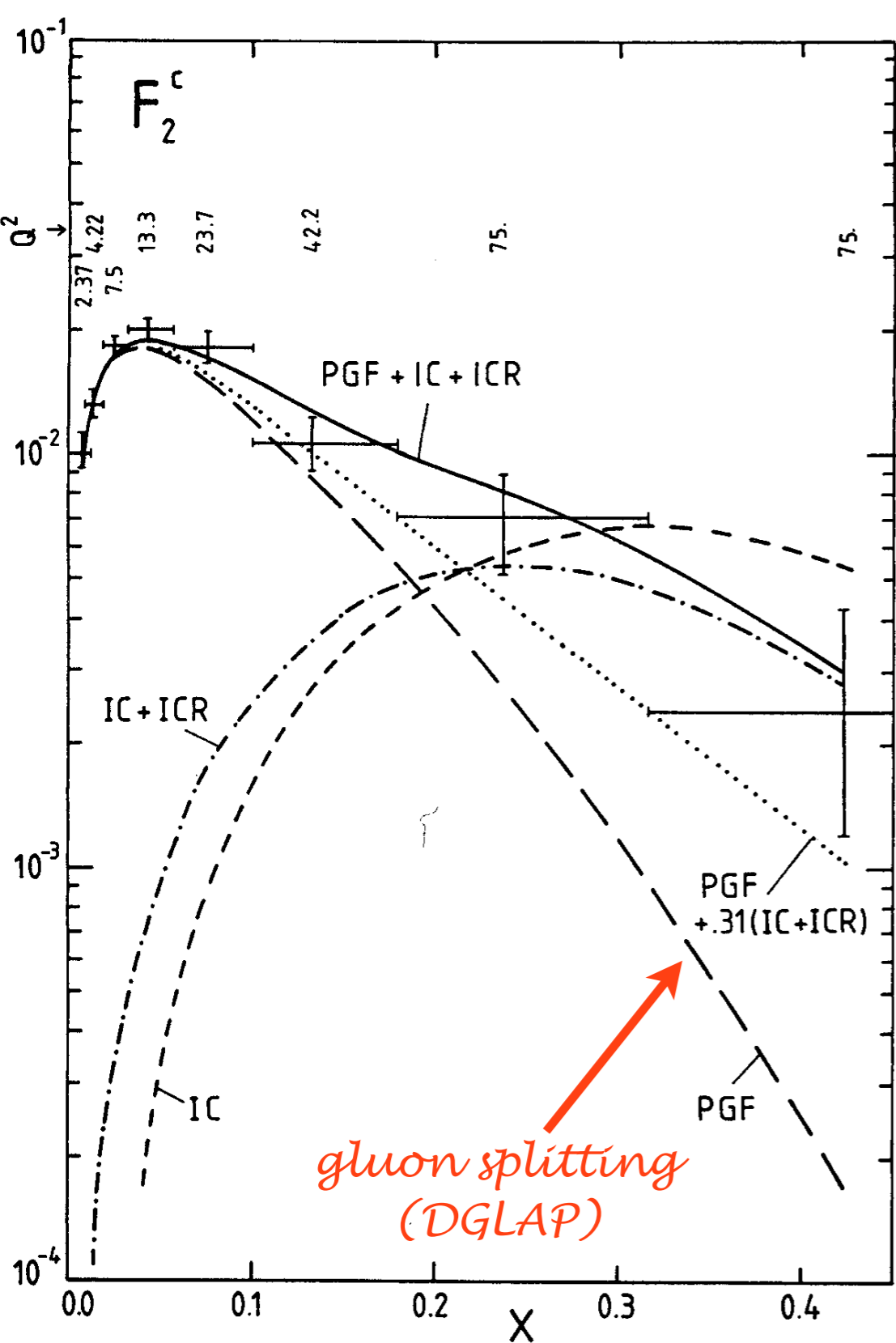
FIGURE 1. Calculations of the  $\bar{c}(x)$  distributions based on the BHPS model. The solid curve corresponds to the calculation using Eq. 1 and the dashed and dotted curves are obtained by evolving the BHPS result to  $Q^2 = 75 \text{ GeV}^2$  using  $\mu = 3.0 \text{ GeV}$ , and  $\mu = 0.5 \text{ GeV}$ , respectively. The normalization is set at  $\mathcal{P}_5^{c\bar{c}} = 0.01$ .

**Consistent with EMC**

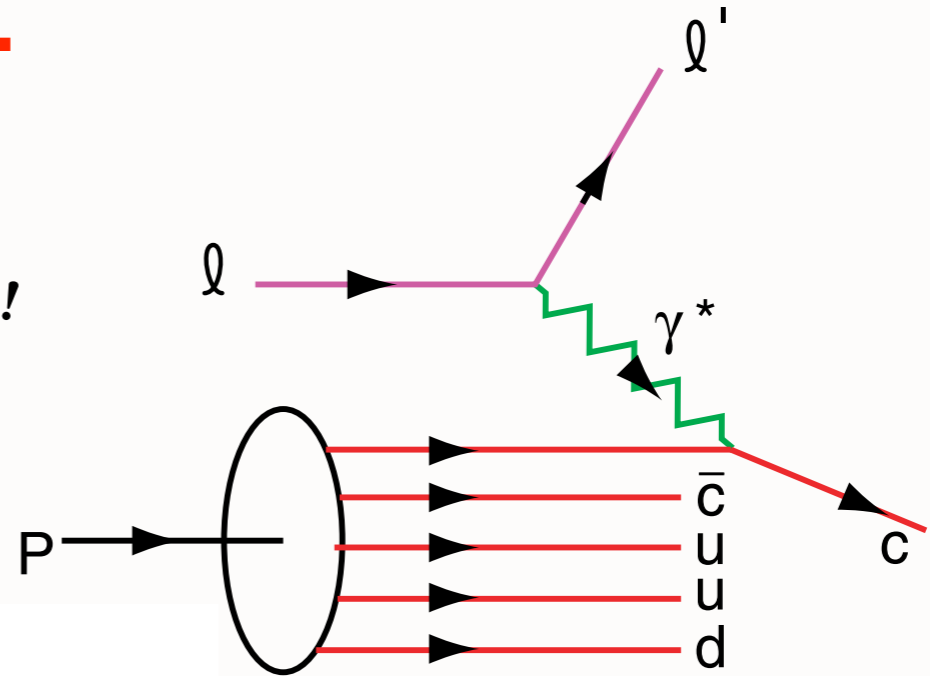
# Measurement of Charm Structure Function

J. J. Aubert et al. [European Muon Collaboration], "Production Of Charmed Particles In 250-GeV Mu+ - Iron Interactions," Nucl. Phys. B 213, 31 (1983).

## First Evidence for Intrinsic Charm



factor of 30!



**DGLAP / Photon-Gluon Fusion: factor of 30 too small**

*Two Components (separate evolution):*

$$c(x, Q^2) = c(x, Q^2)_{\text{extrinsic}} + c(x, Q^2)_{\text{intrinsic}}$$



***Do heavy quarks exist in the proton at high  $x$ ?***

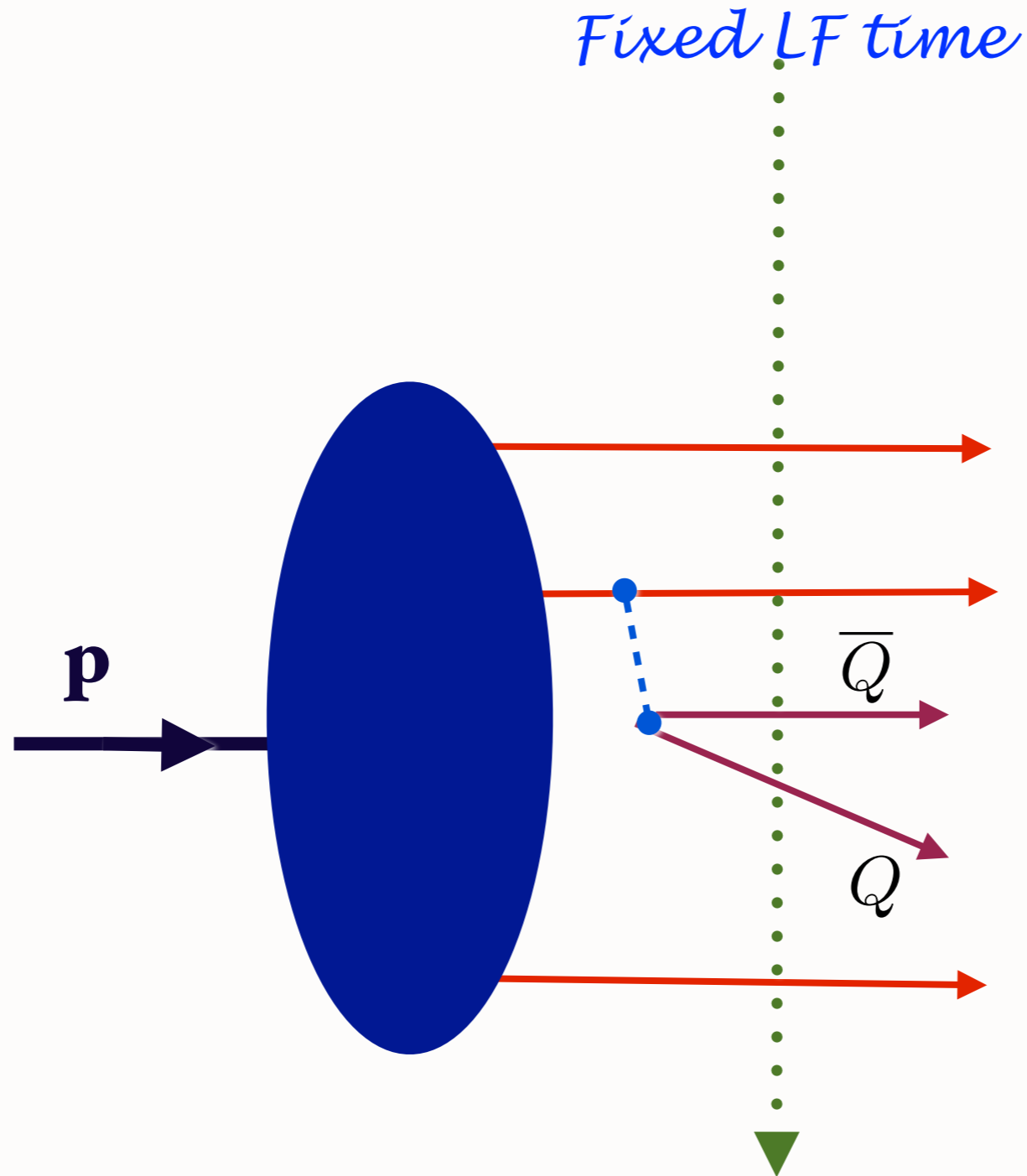
***Conventional wisdom: impossible!***

***Heavy quarks generated only at low  $x$   
via DGLAP evolution  
from gluon splitting***

$$s(x, \mu_F^2) = c(x, \mu_F^2) = b(x, \mu_F^2) \equiv 0$$

at starting scale  $\mu_F^2$

***Conventional wisdom is wrong even in QED!***



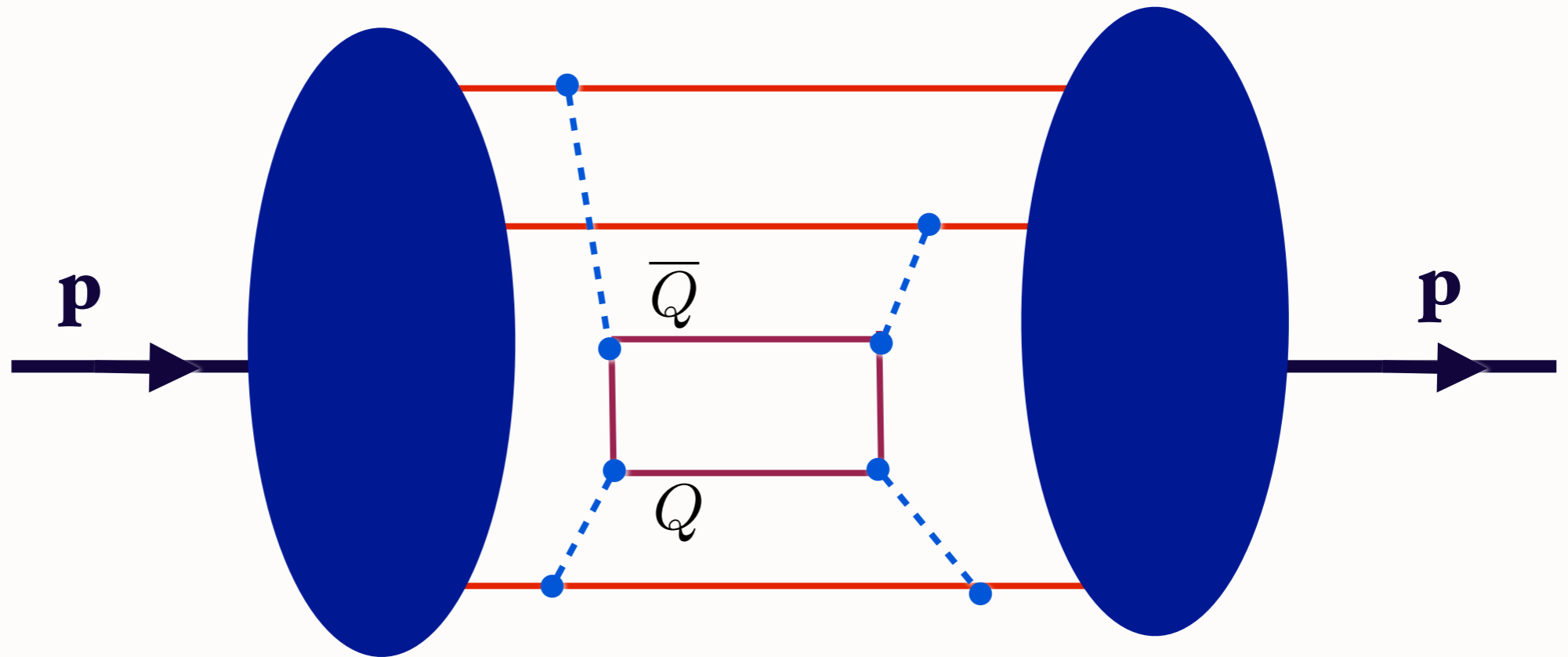
*Proton's 5-quark Fock State from gluon splitting  
 "Extrinsic" Heavy Quarks*

$$s(x, Q^2)_{\text{extrinsic}} \sim (1-x)g(x, Q^2) \sim (1-x)^5$$

# Proton Self Energy from gluon-gluon scattering

*QCD predicts Intrinsic Heavy Quarks!*

$$x_Q \propto (m_Q^2 + k_{\perp}^2)^{1/2}$$



Probability (QED)  $\propto \frac{1}{M_{\ell}^4}$

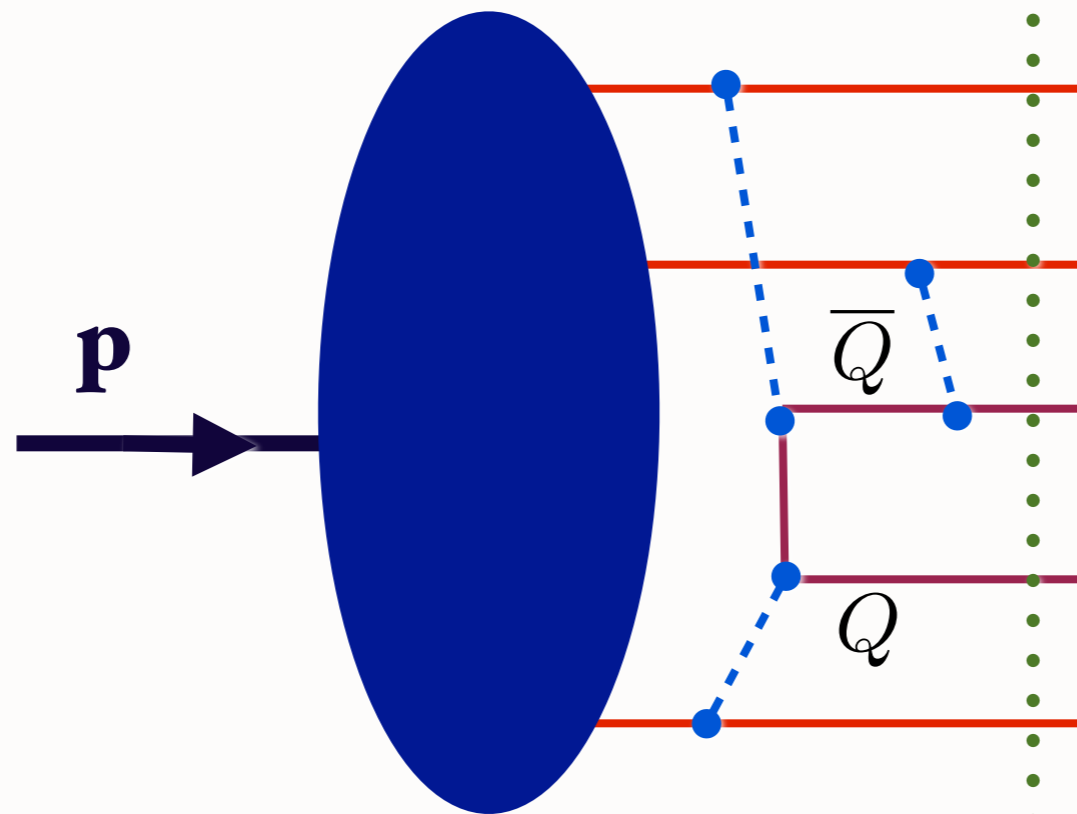
Probability (QCD)  $\propto \frac{1}{M_Q^2}$

$$(g - 2)_{\mu} \propto \frac{\alpha^3}{\pi^3} \log \frac{m_{\mu}^2}{m_e^2}$$

**Collins, Ellis, Gunion, Mueller, sjb**  
**M. Polyakov, et al.**

*from light-by-light scattering*

*Proton 5-quark Fock State:  
Intrinsic Heavy Quarks*



*QCD predicts  
Intrinsic Heavy  
Quarks at high  $x$ !*

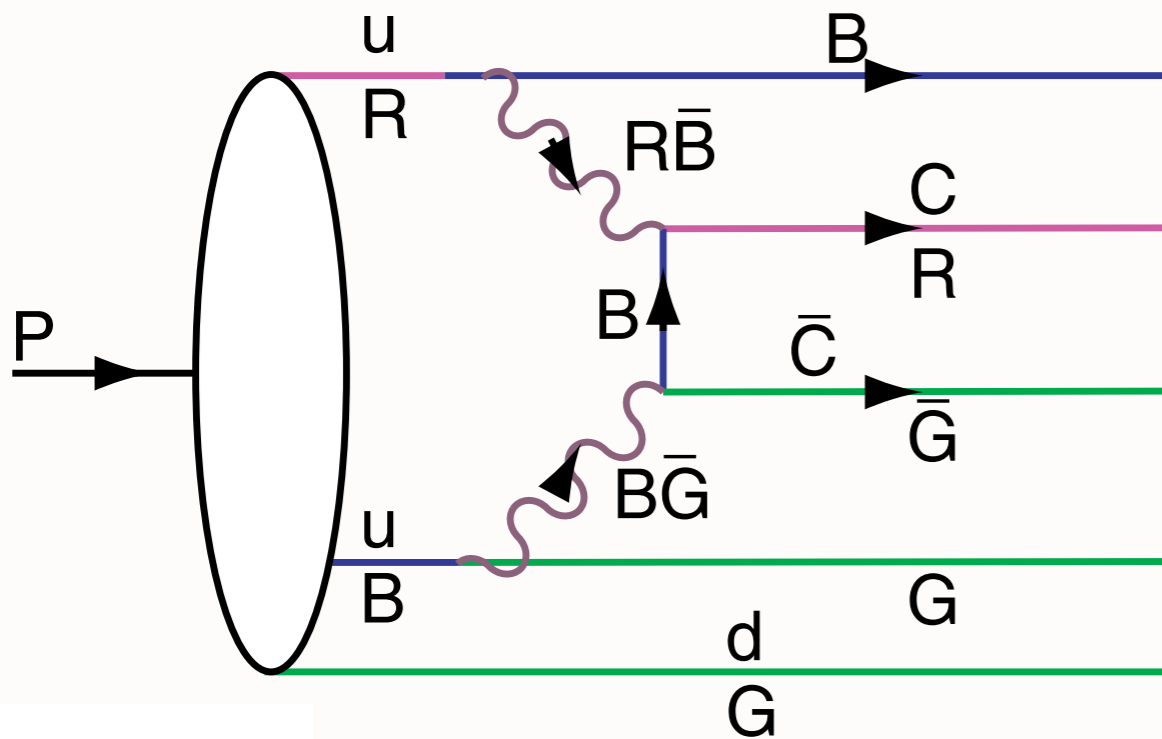
**Minimal off-shellness**

$$x_Q \propto (m_Q^2 + k_{\perp}^2)^{1/2}$$

Probability (QED)  $\propto \frac{1}{M_{\ell}^4}$

Probability (QCD)  $\propto \frac{1}{M_Q^2}$

**Collins, Ellis, Gunion, Mueller, sjb  
M. Polyakov**



$|uudcc\rangle$  Fluctuation in Proton

QCD: Probability  $\frac{\sim \Lambda_{QCD}^2}{M_Q^2}$

$|e^+e^-l^+l^-\rangle$  Fluctuation in Positronium

QED: Probability  $\frac{\sim (m_e\alpha)^4}{M_\ell^4}$

OPE derivation - M.Polyakov et al.

$$\langle p | \frac{G_{\mu\nu}^3}{m_Q^2} | p \rangle \text{ vs. } \langle p | \frac{F_{\mu\nu}^4}{m_\ell^4} | p \rangle$$

$cc$  in Color Octet

$$\hat{x}_i = \frac{m_{\perp i}}{\sum_j^n m_{\perp j}}$$

$$x_Q \propto (m_Q^2 + k_\perp^2)^{1/2}$$

Distribution peaks at equal rapidity (velocity)

Therefore heavy particles carry the largest momentum fractions

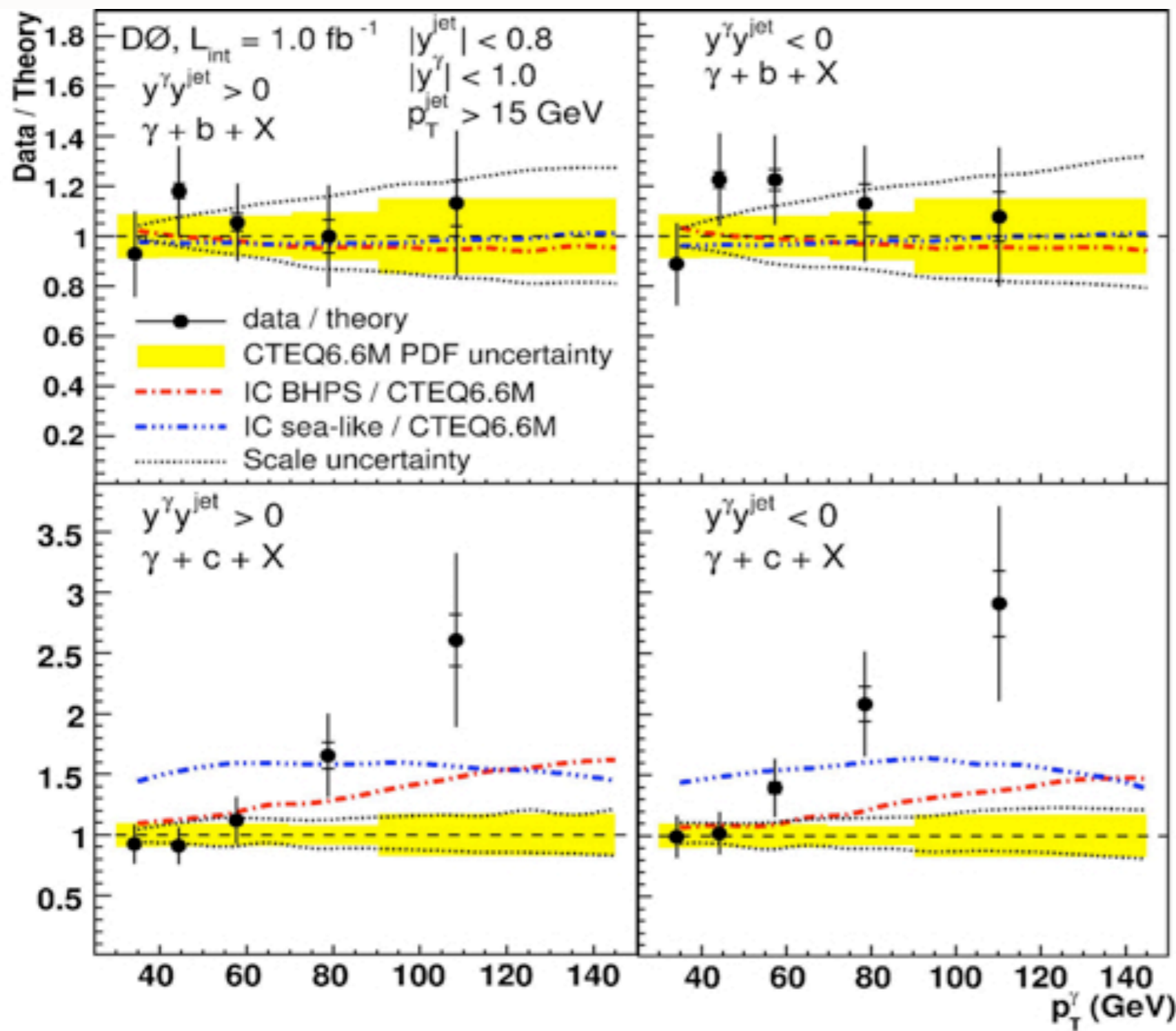
*High x charm!*      *JLab: Charm at Threshold*

**Action Principle: Minimum KE, maximal potential**

**D0**

Measurement of  $\gamma + b + X$  and  $\gamma + c + X$  Production Cross Sections  
in  $p\bar{p}$  Collisions at  $\sqrt{s} = 1.96$  TeV

$$p\bar{p} \rightarrow \gamma + Q + X$$

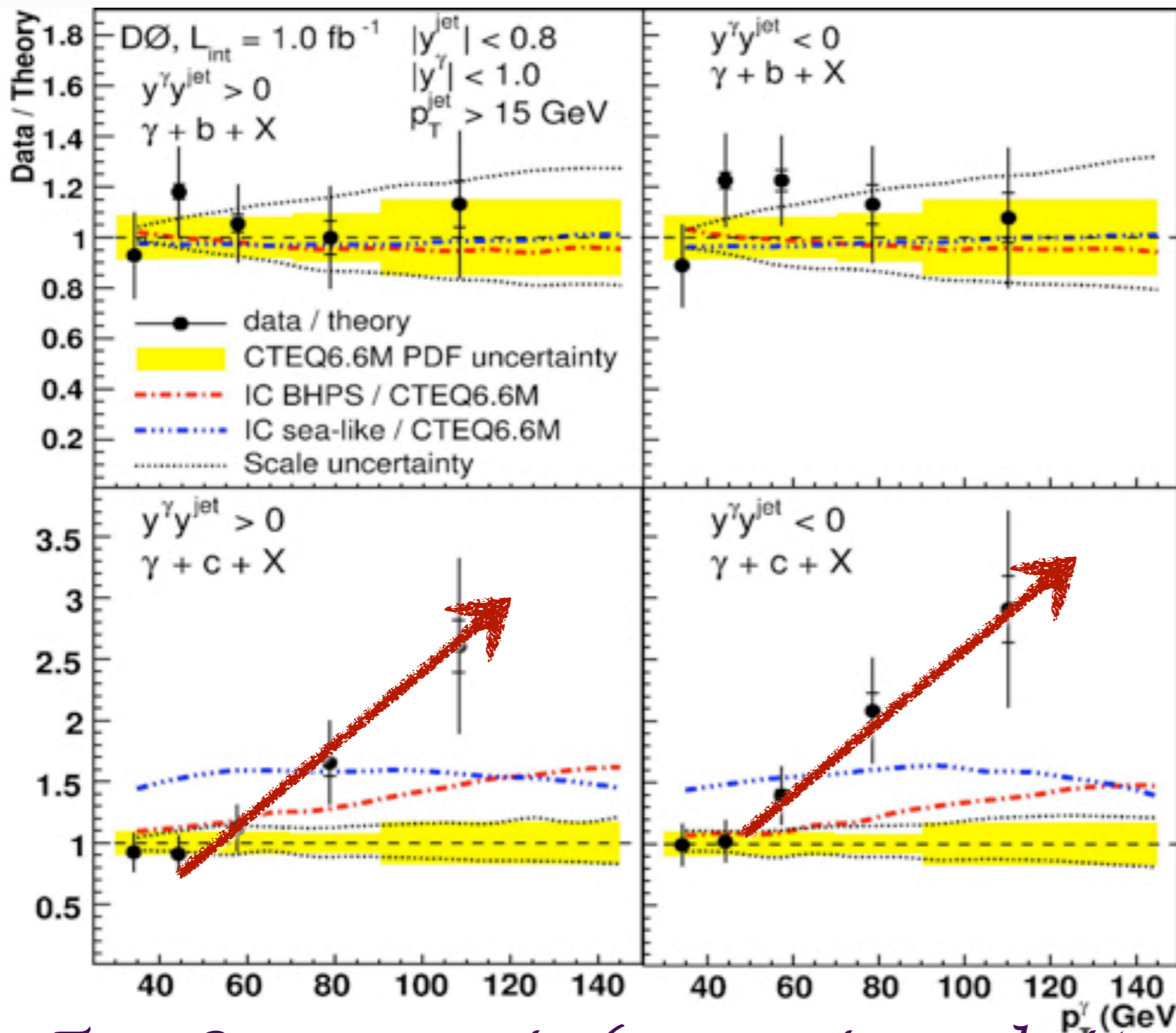


$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma c X)}{\Delta\sigma(\bar{p}p \rightarrow \gamma b X)}$$
**Ratio is insensitive  
to gluon PDF,  
scales**

# D0

## Measurement of $\gamma + b + X$ and $\gamma + c + X$ Production Cross Sections in $p\bar{p}$ Collisions at $\sqrt{s} = 1.96$ TeV

$$p\bar{p} \rightarrow \gamma + Q + X$$



$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma c X)}{\Delta\sigma(\bar{p}p \rightarrow \gamma b X)}$$
**Ratio is insensitive to gluon PDF, scales**

$$gc \rightarrow \gamma c$$

**Signal for significant intrinsic charm at  $x > 0.1$  ?**

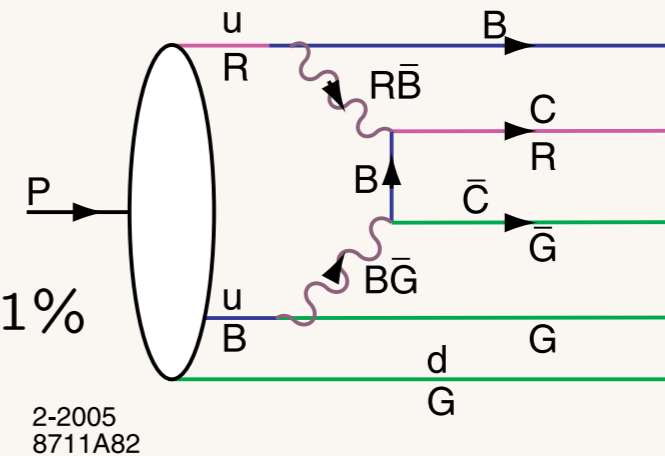
*Two Components (separate evolution):*

$$c(x, Q^2) = c(x, Q^2)_{\text{extrinsic}} + c(x, Q^2)_{\text{intrinsic}}$$

**(Need to evolve IC with nonzero quark mass)**

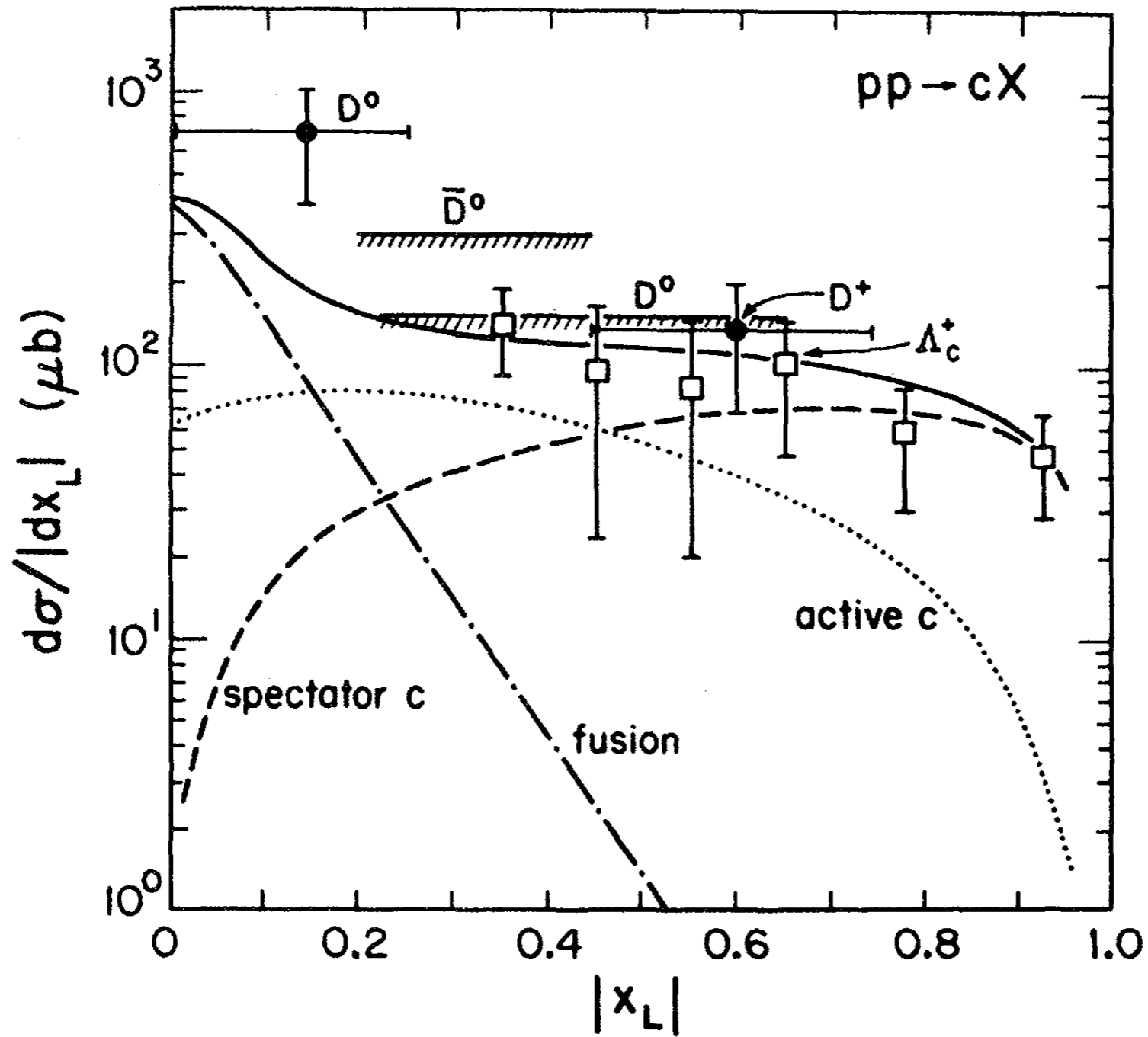
# Intrinsic Heavy-Quark Fock States

- **Rigorous** prediction of QCD, OPE
- Color-Octet Color-Octet Fock State!
- Probability  $P_{Q\bar{Q}} \propto \frac{1}{M_Q^2}$   $P_{Q\bar{Q}Q\bar{Q}} \sim \alpha_s^2 P_{Q\bar{Q}}$   $P_{c\bar{c}/p} \simeq 1\%$



- **Large Effect at high  $x$  and at threshold!**
- Greatly increases kinematics of colliders such as Higgs production (**Kopeliovich, Schmidt, Soffer, Goldhaber, sjb**)
- Severely underestimated in conventional parameterizations of heavy quark distributions (**Except CTEQ**)
- Important corrections to penguin contributions to B-meson weak decays (**Gardner, sjb**)
- Slow evolution compared to extrinsic quarks from gluon splitting!
- Many empirical tests at JLAB 12, COMPASS





**Barger, Halzen, Keung**

*More evidence for charm at large  $x$*

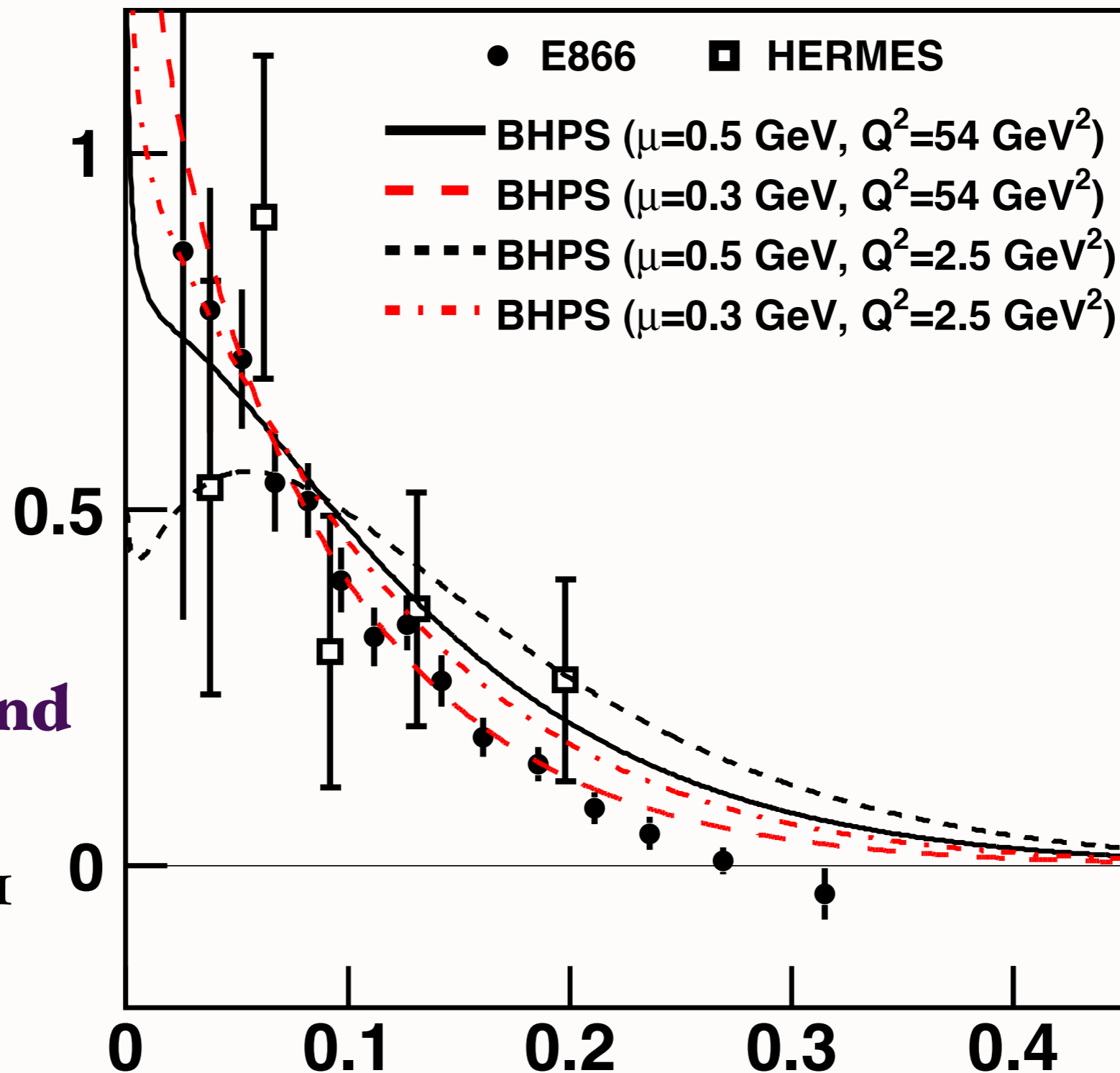
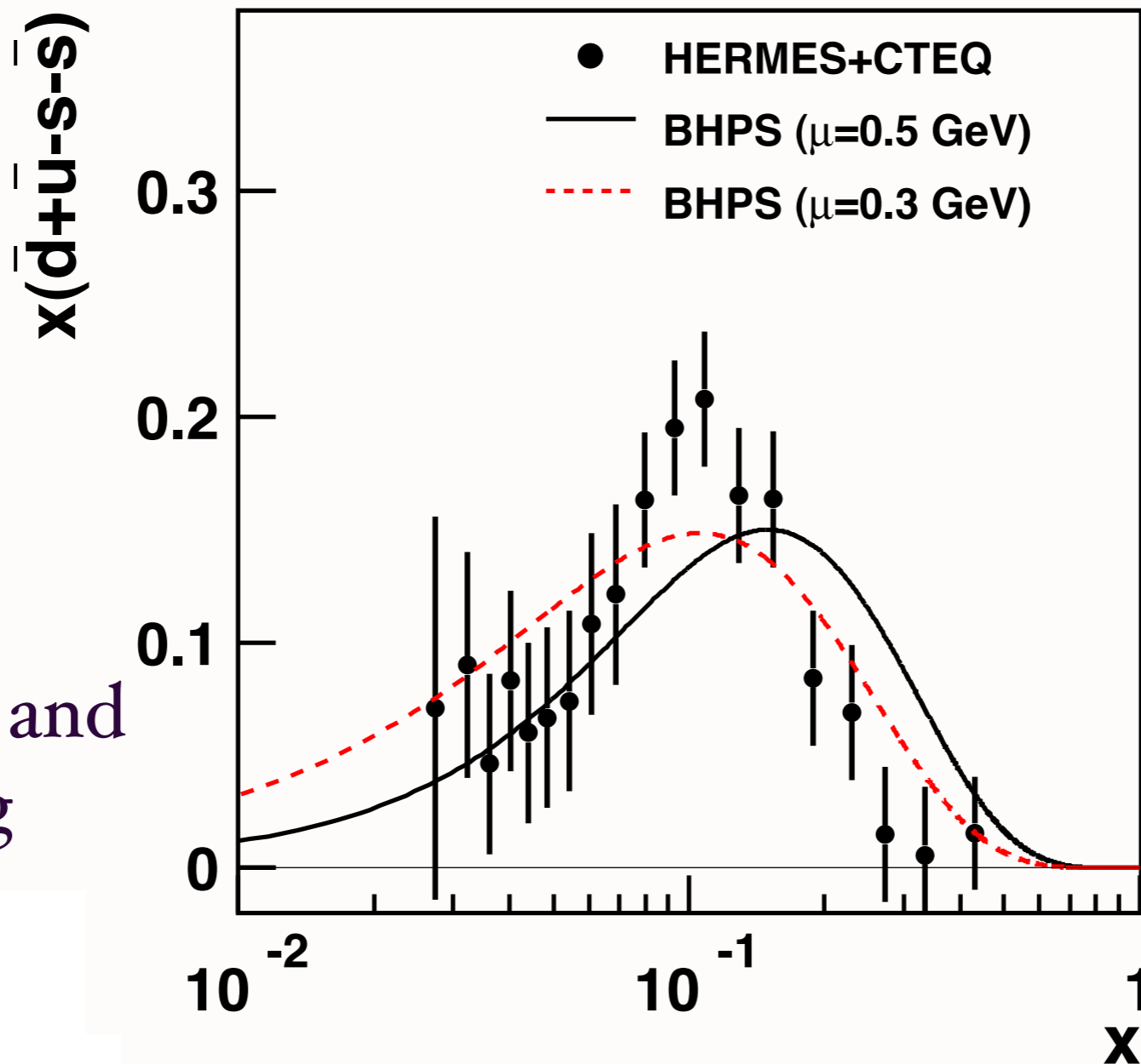
$\bar{d}-\bar{u}$ 

Figure 1: Comparison of the  $\bar{d}(x) - \bar{u}(x)$  data from Fermilab E866 and HERMES with the calculations based on the BHPS model. Eq. 1 and Eq. 3 were used to calculate the  $\bar{d}(x) - \bar{u}(x)$  distribution at the initial scale. The distribution was then evolved to the  $Q^2$  of the experiments and shown as various curves. Two different initial scales,  $\mu = 0.5$  and  $0.3$  GeV, were used for the E866 calculations in order to illustrate the dependence on the choice of the initial scale.

**X**

W. C. Chang and  
J.-C. Peng  
arXiv:1105.2381

$$x[\bar{u}(x) + \bar{d}(x) - s(x) - \bar{s}(x)]$$



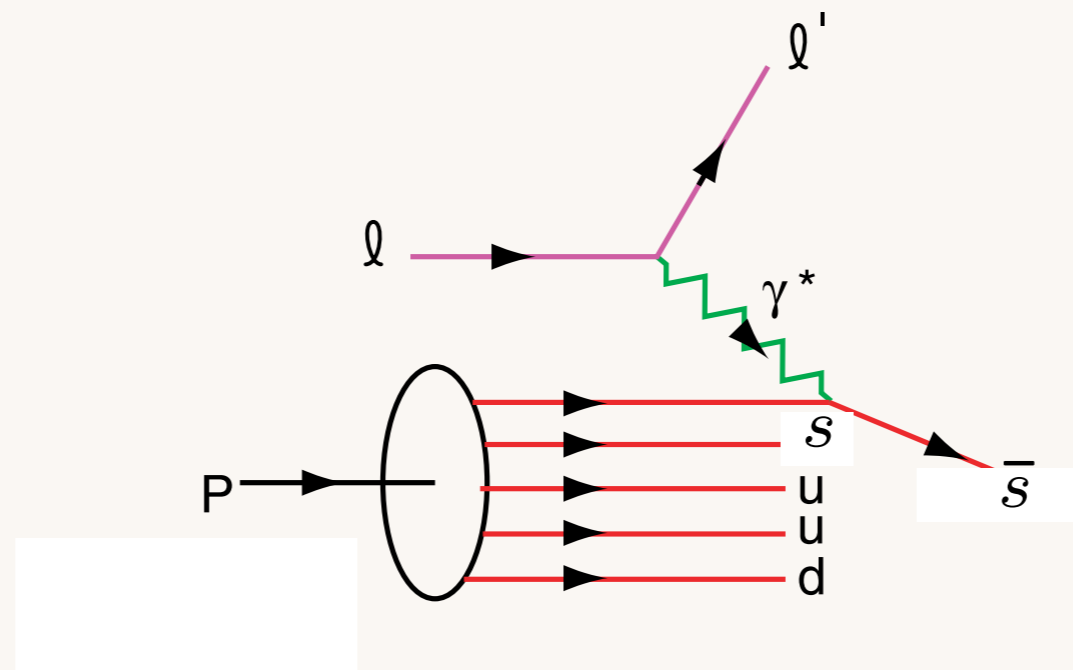
W. C. Chang and  
J.-C. Peng

Comparison of the  $x(\bar{d}(x) + \bar{u}(x) - s(x) - \bar{s}(x))$  data with the calculations based on the BHPS model. The values of  $x(s(x) + \bar{s}(x))$  are from the HERMES experiment [6], and those of  $x(\bar{d}(x) + \bar{u}(x))$  are obtained from the PDF set CTEQ6.6 [11]. The solid and dashed curves are obtained by evolving the BHPS result to  $Q^2 = 2.5 \text{ GeV}^2$  using  $\mu = 0.5 \text{ GeV}$  and  $\mu = 0.3 \text{ GeV}$ , respectively. The normalization of the calculations are adjusted to fit the data.

# Measure strangeness distribution in Semi-Inclusive DIS at JLab

$$\text{Is } s(x) = \bar{s}(x)?$$

- **Non-symmetric strange and antistrange sea?**
- **Non-perturbative physics; e.g**  $|uuds\bar{s}\rangle \simeq |\Lambda(uds)K^+(\bar{s}u)\rangle$
- **Crucial for interpreting NuTeV anomaly**



**Tag quark flavor in semi-inclusive DIS**

$$ep \rightarrow e' K^+ X$$

- EMC data:  $c(x, Q^2) > 30 \times \text{DGLAP}$   
 $Q^2 = 75 \text{ GeV}^2, x = 0.42$

- High  $x_F$   $pp \rightarrow J/\psi X$

**CERN NA<sub>3</sub>**

- High  $x_F$   $pp \rightarrow J/\psi J/\psi X$

- High  $x_F$   $pp \rightarrow \Lambda_c X$

**ISR**

- High  $x_F$   $pp \rightarrow \Lambda_b X$

**Intrinsic Bottom!**  
**Zichichi, Cifarelli, et al.**

- High  $x_F$   $pp \rightarrow \Xi(ccd)X$  (SELEX)

**FermiLab**

**IC Structure Function: Critical Measurement for EIC**

**Many interesting spin, charge asymmetry, spectator effects**

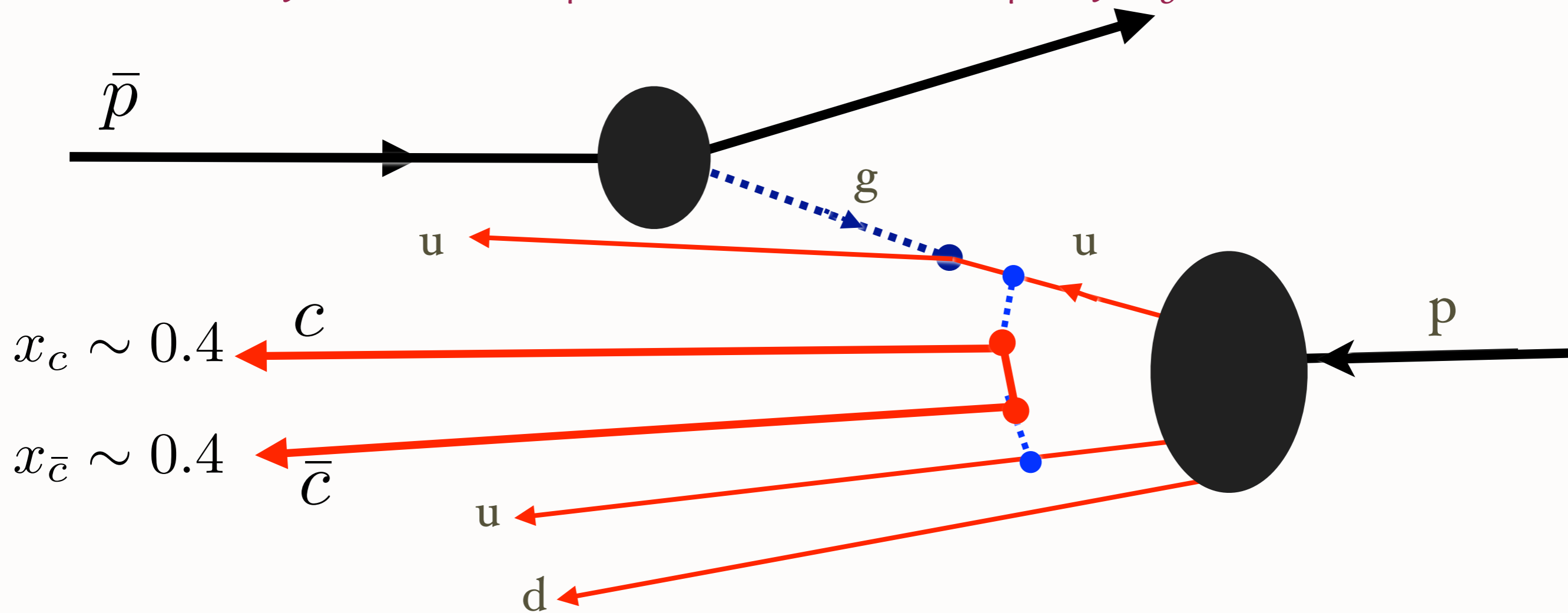
# Excitation of Intrinsic Heavy Quarks in Proton

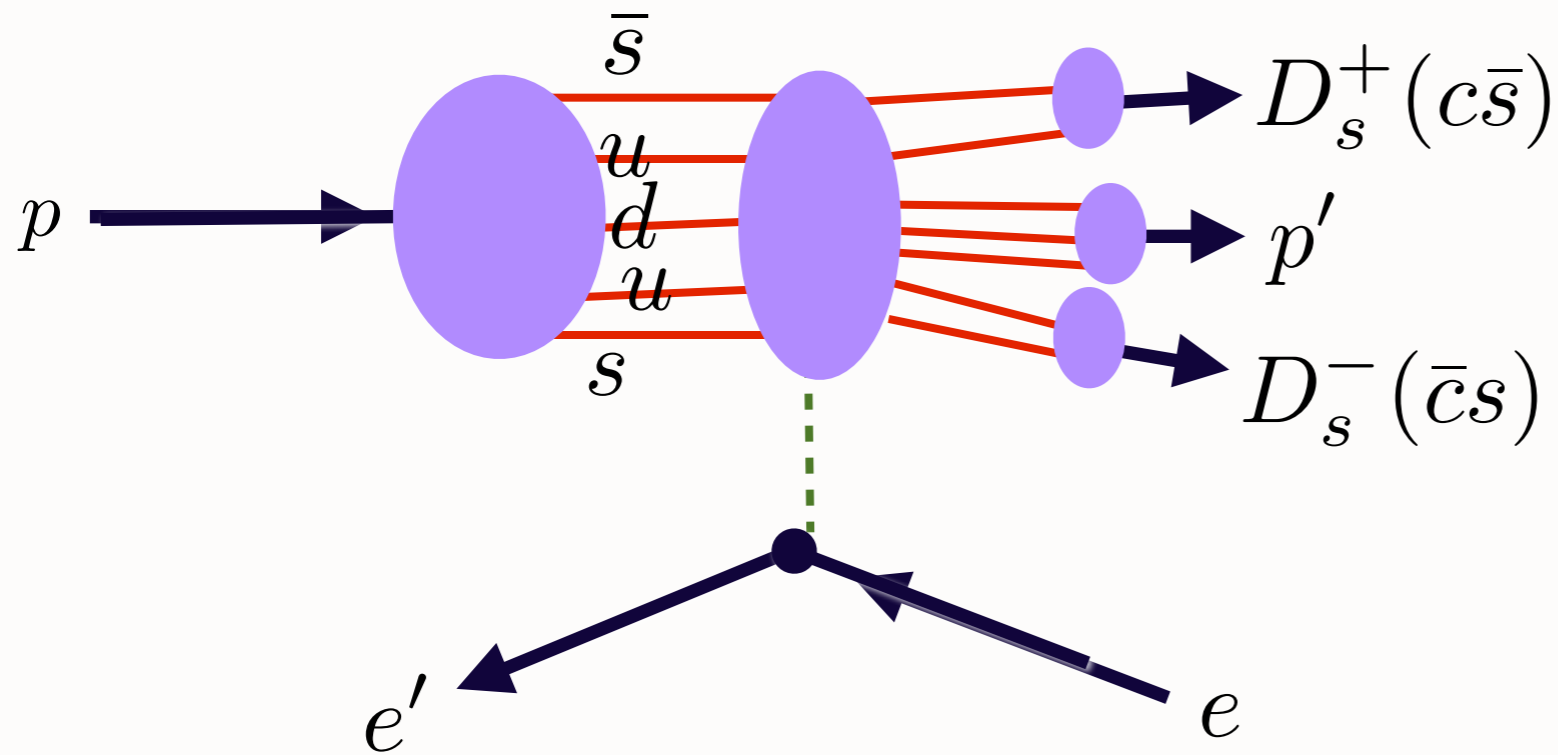
**Amplitude maximal at small invariant mass, equal rapidity**

$$x_i \sim \frac{m_{\perp i}}{\sum_j^n m_{\perp j}} \quad \frac{d\sigma}{dy_{J/\psi}} (\bar{p}p \rightarrow J/\psi X)$$

J-P Lansberg, sjb

Heavy Quarkonium produced in **TARGET** rapidity region





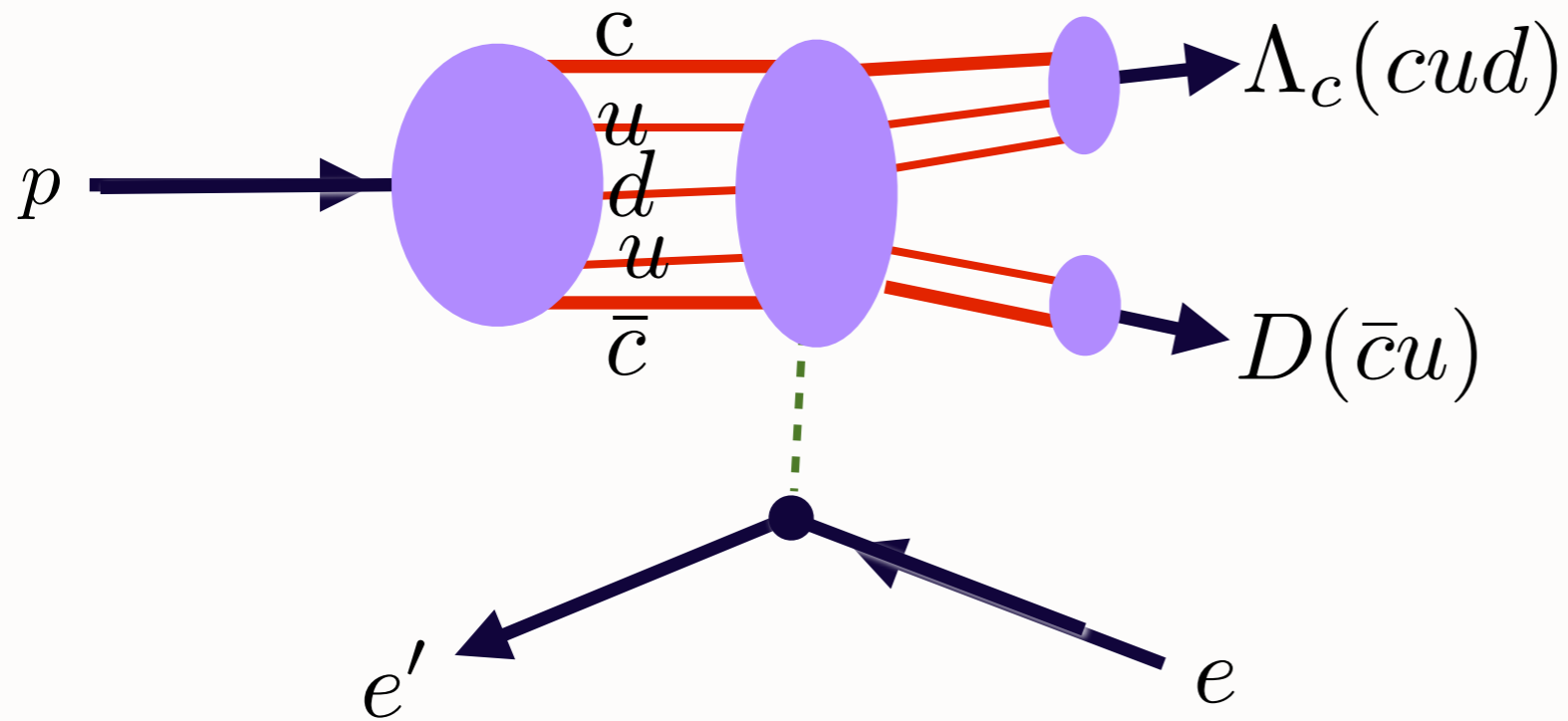
Look for  $D_s^- (\bar{c}s)$  vs.  $D_s^+ (c\bar{s})$  asymmetry

Reflects  $s$  vs.  $\bar{s}$  asymmetry in proton  $|uuds\bar{s}\rangle$  Fock LF state.

Asymmetry natural from  $|K^+\Lambda\rangle$  excitation

**Ma, sjb**

Assumes symmetric charm and anti-charm distributions



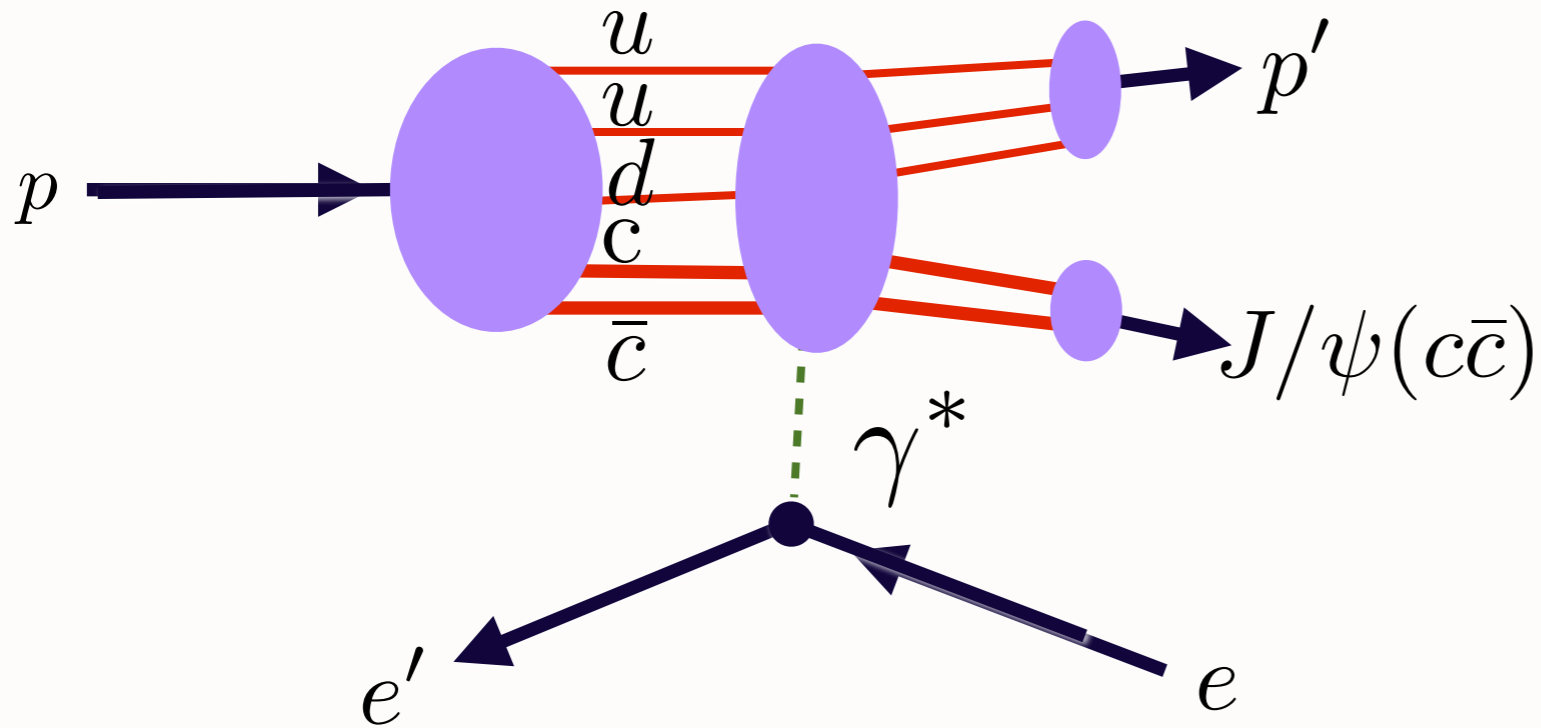
*EIC  
Experiment*

Dissociate proton to high  $x_F$  heavy-quark pair

$$\gamma^* p \rightarrow \Lambda_c(cdd) + D(\bar{c}u), \gamma^* p \rightarrow \Lambda_b(bud)B^+(\bar{b}u)$$

*Test intrinsic charm, bottom*

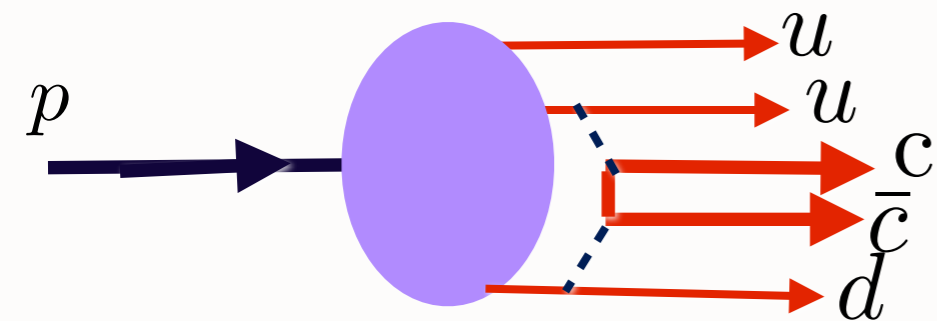




Dissociate proton to high  $x_F$  Quarkonium:

$$\gamma^* p \rightarrow J/\psi + p'$$

$$\gamma^* p \rightarrow \Upsilon + p'$$



*But possibly disfavored since*

$$|p\rangle \simeq |(uud)_{8C} (c\bar{c})_{8C}\rangle$$

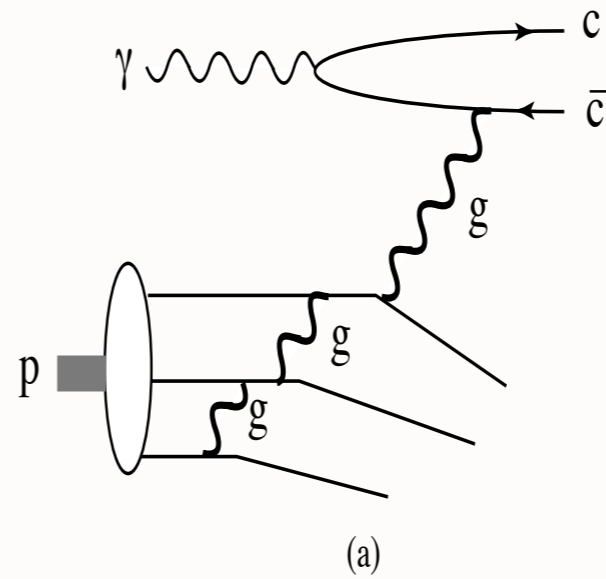
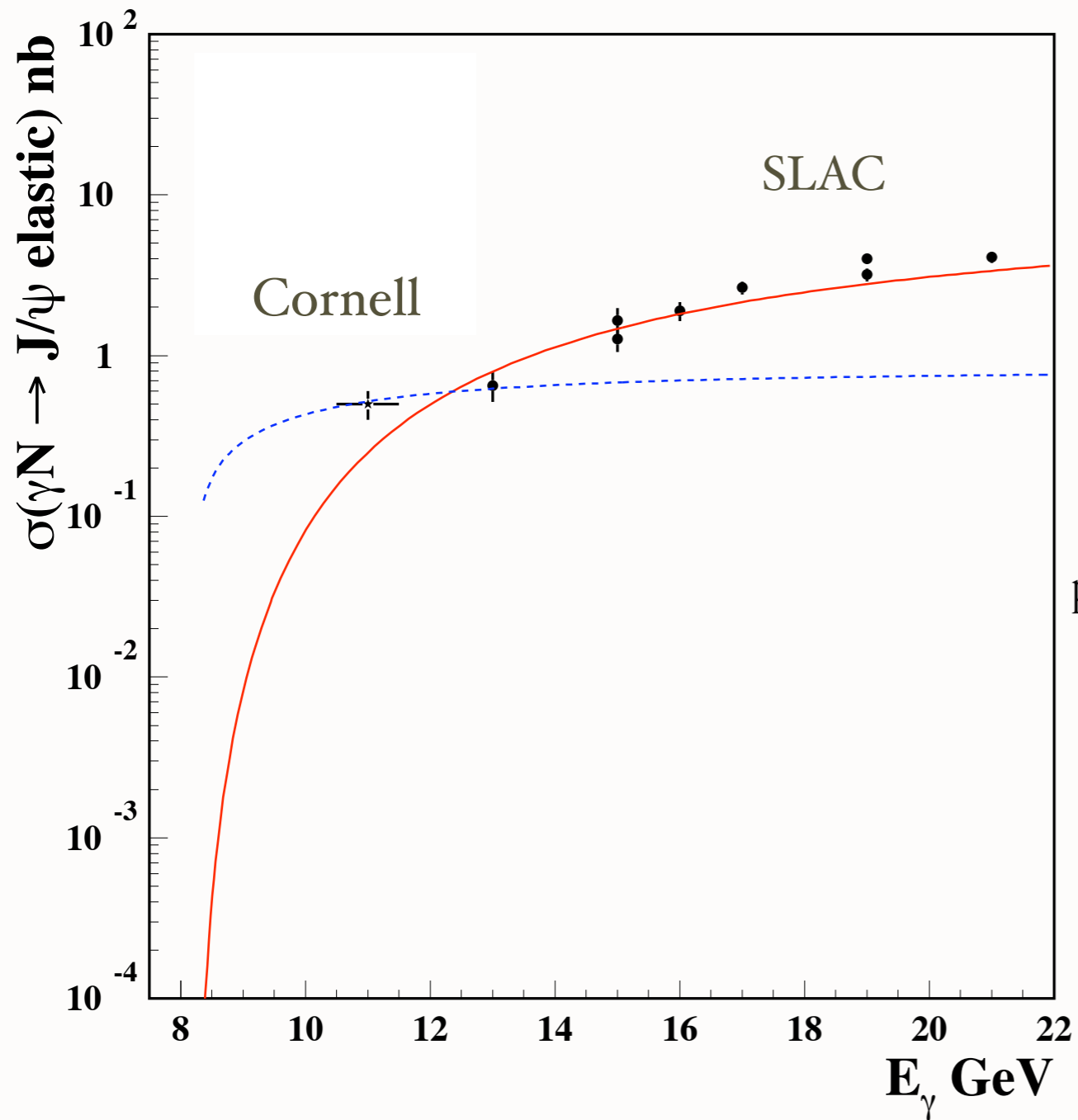
*Test intrinsic charm, bottom*

**Collins, Ellis,  
Gunion, Mueller, sjb**

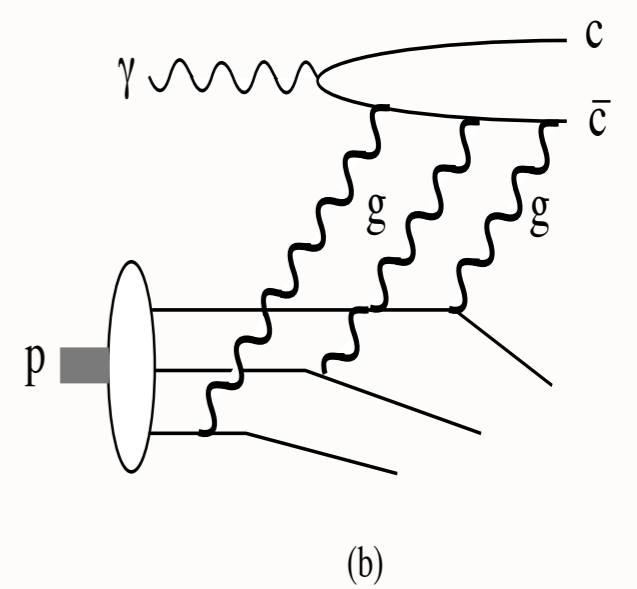
**M. Polyakov et al.**

$$\gamma p \rightarrow J/\psi p$$

Chudakov, Hoyer, Laget, sjb



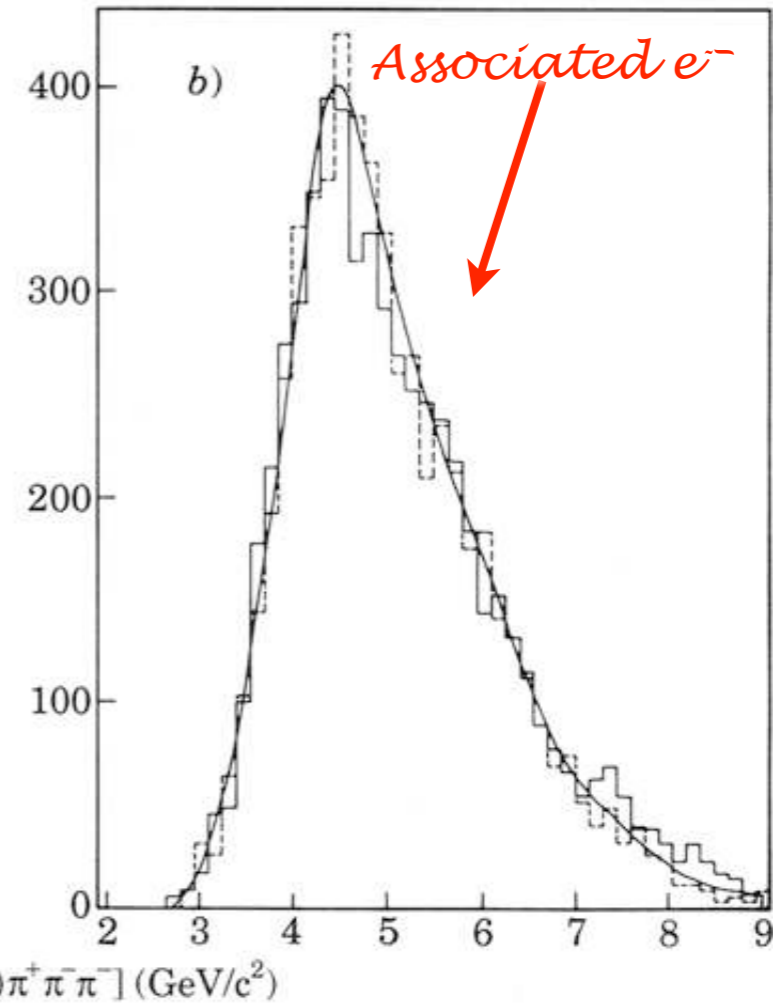
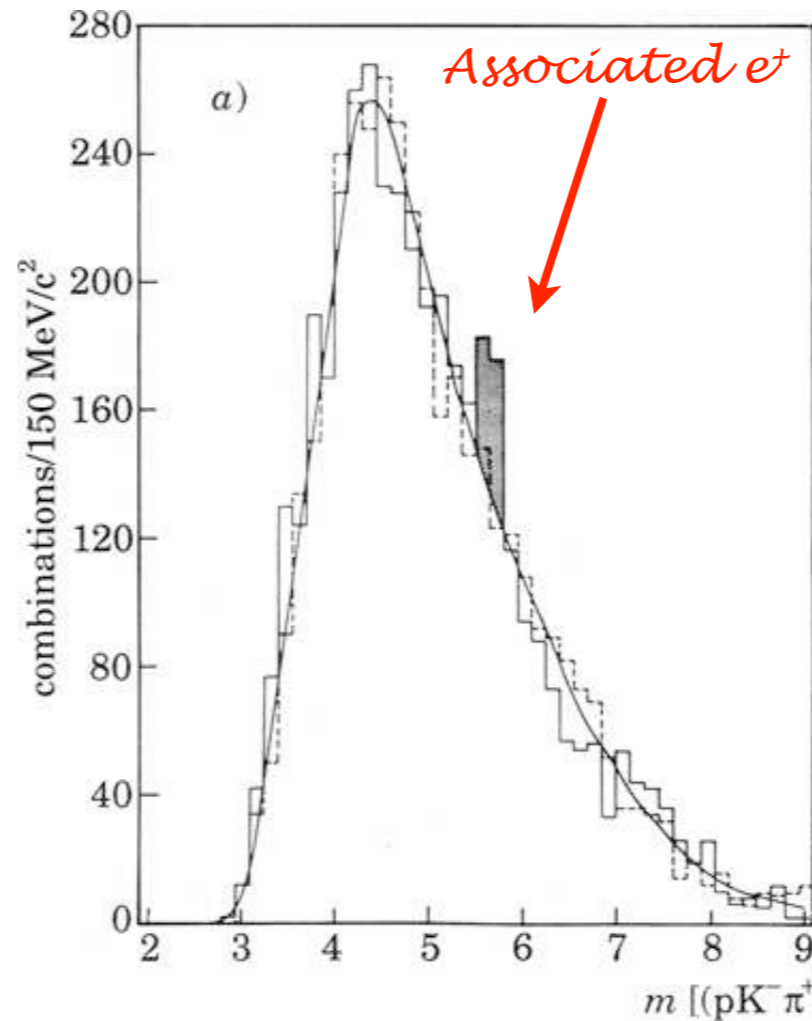
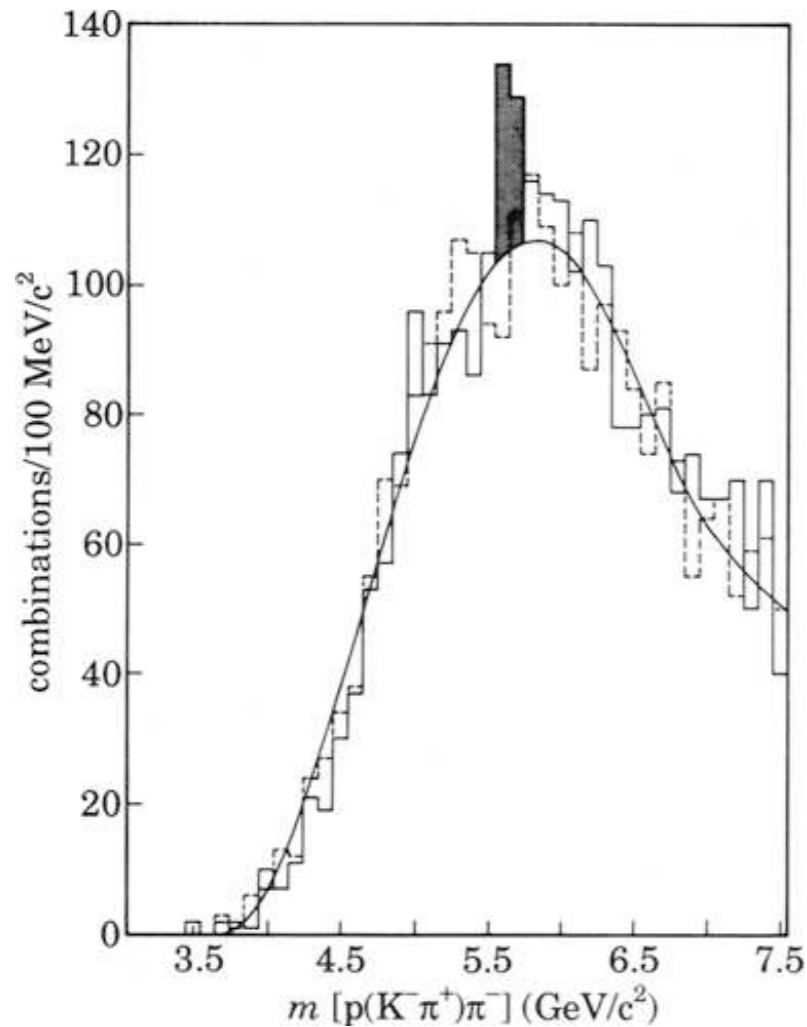
*Leading twist contribution*



*Dominant near threshold*

$$pp \rightarrow \Lambda_b(bud)B(\bar{b}q)X \text{ at large } x_F$$

## CERN-ISR R422 (Split Field Magnet), 1988/1991



$$\Lambda_b^0 \rightarrow pD^0\pi^-$$

$$\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^+ \pi^- \pi^-$$

Il Nuovo Cimento 104, 1787

*First Evidence for Intrinsic Bottom!*

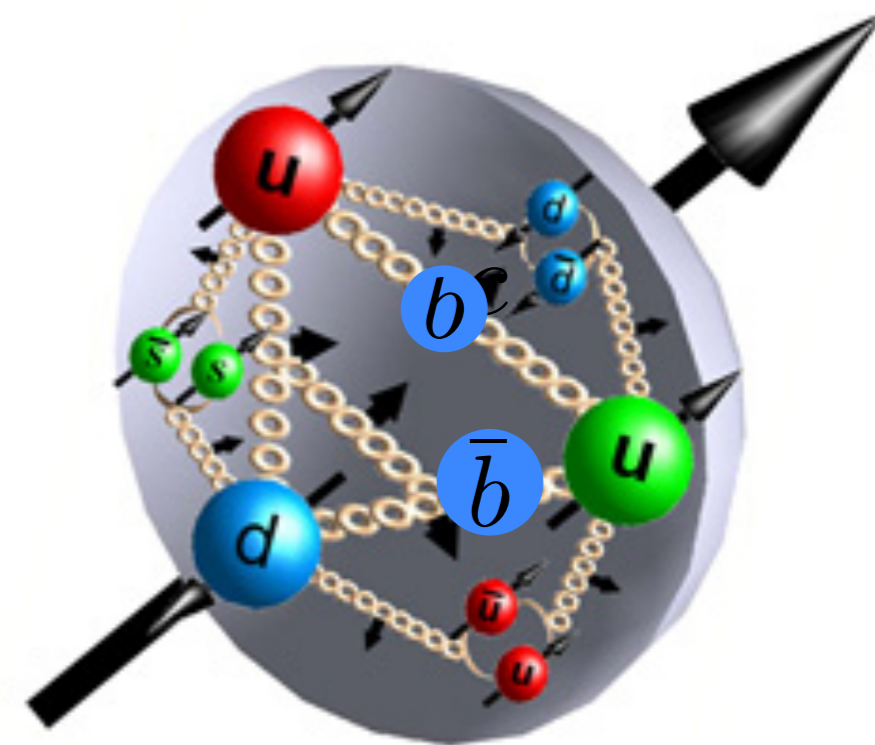


CM-P00063074

# THE $\Lambda_b^0$ BEAUTY BARYON PRODUCTION IN PROTON-PROTON INTERACTIONS AT $\sqrt{s}=62$ GeV: A SECOND OBSERVATION

G. Bari, M. Basile, G. Bruni, G. Cara Romeo, R. Casaccia, L. Cifarelli, F. Cindolo, A. Contin, G. D'Alì, C. Del Papa, S. De Pasquale, P. Giusti, G. Iacobucci, G. Maccarrone, T. Massam, R. Nania, F. Palmonari, G. Sartorelli, G. Susinno, L. Votano and A. Zichichi

CERN, Geneva, Switzerland  
 Dipartimento di Fisica dell'Università, Bologna, Italy  
 Dipartimento di Fisica dell'Università, Cosenza, Italy  
 Istituto di Fisica dell'Università, Palermo, Italy  
 Istituto Nazionale di Fisica Nucleare, Bologna, Italy  
 Istituto Nazionale di Fisica Nucleare, LNF, Frascati, Italy



## Abstract

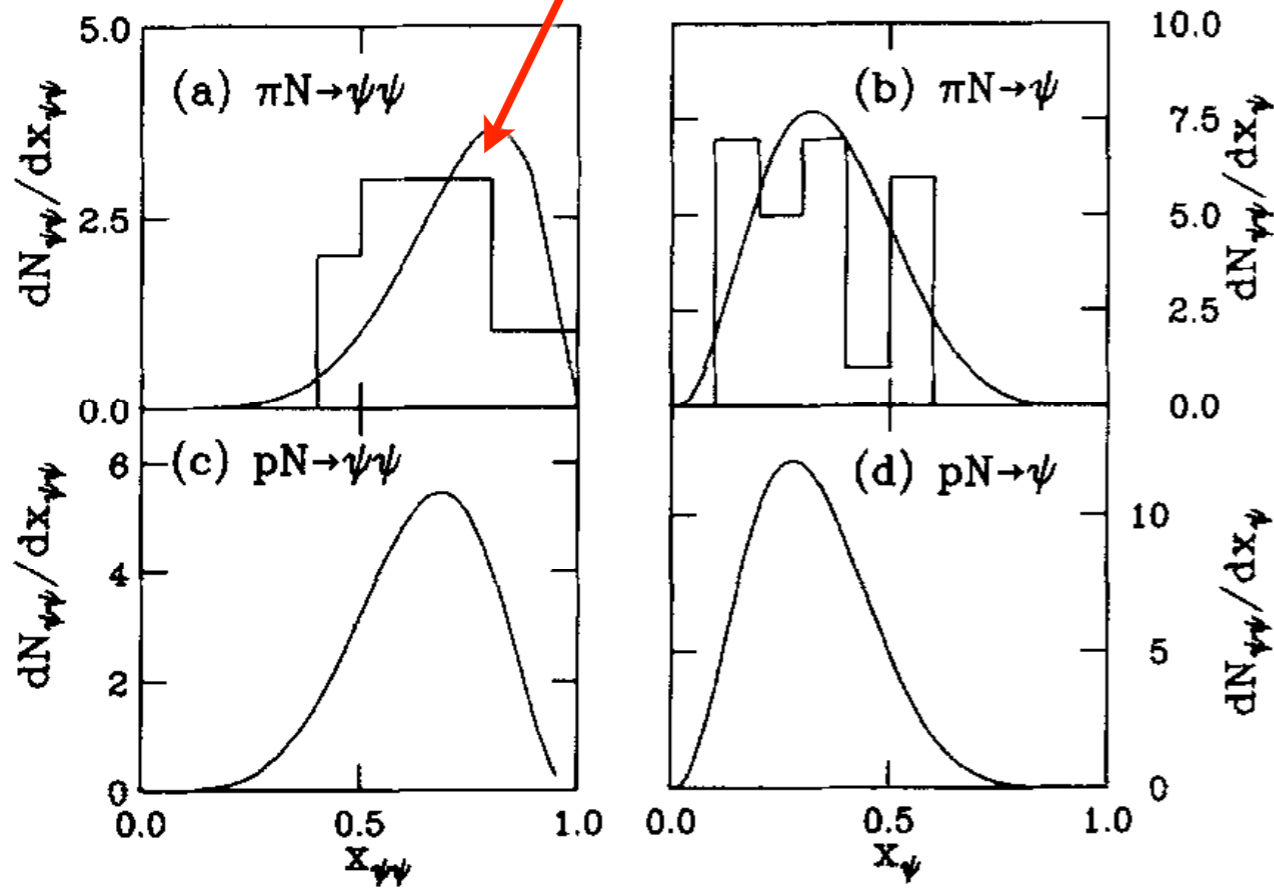
Another decay mode of the  $\Lambda_b^0$  (open-beauty baryon) state has been observed:  $\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^+ \pi^- \pi^-$ . In addition, new results on the previously observed decay channel,  $\Lambda_b^0 \rightarrow p D^0 \pi^-$ , are reported. These results confirm our previous findings on  $\Lambda_b^0$  production at the ISR. The mass value ( $5.6 \text{ GeV}/c^2$ ) is found to be in good agreement with theoretical predictions. The production mechanism is found to be “leading”.

*First Evidence for Intrinsic Bottom!*



# Excludes PYTHIA 'color drag' model

All events have  $x_{\psi\psi}^F > 0.4$  !



$$\pi A \rightarrow J/\psi J/\psi X$$

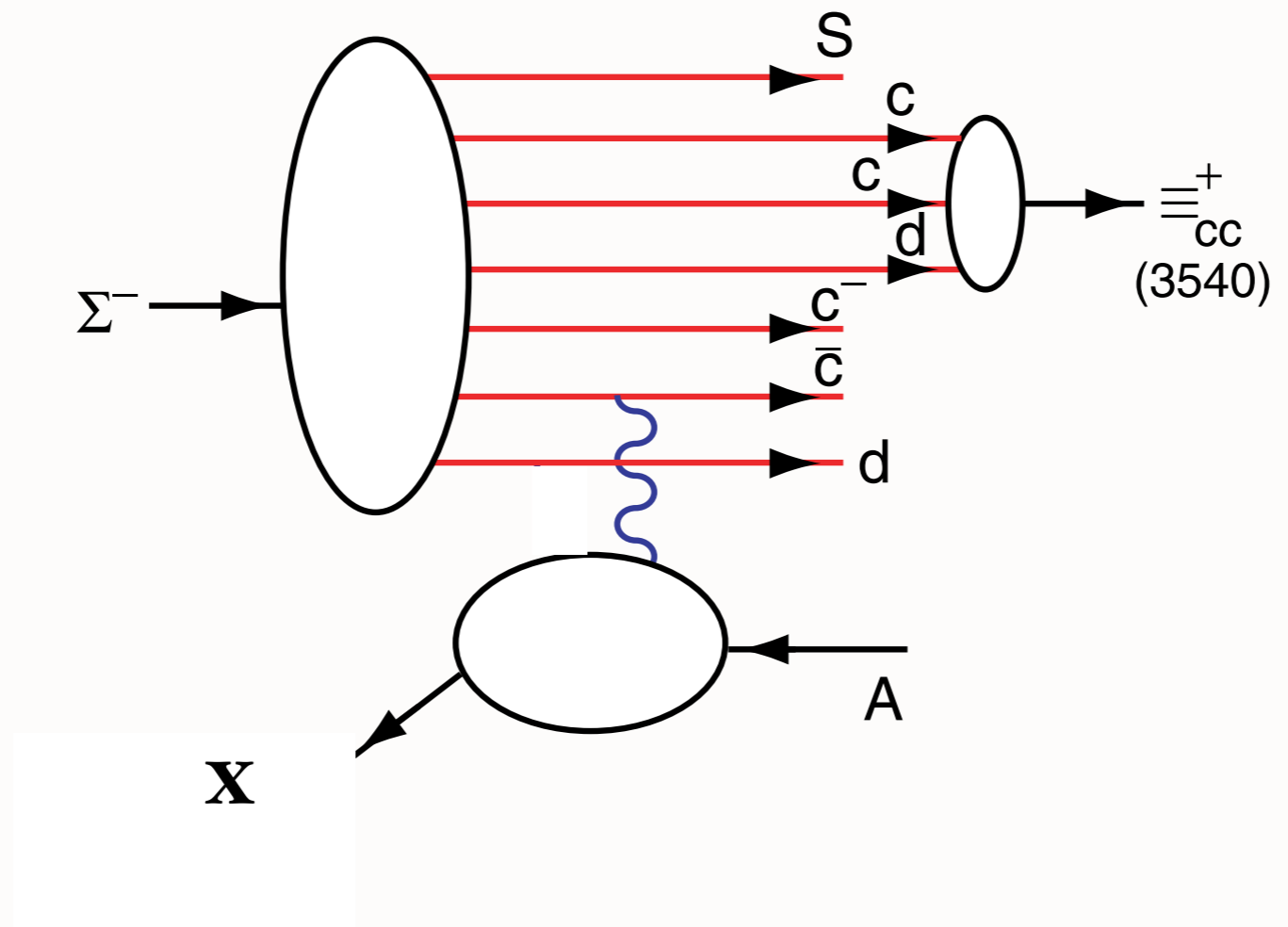
R, Vogt, sjb

The probability distribution for a general  $n$ -particle intrinsic  $c\bar{c}$  Fock state as a function of  $x$  and  $k_T$  is written as

$$\frac{dP_{ic}}{\prod_{i=1}^n dx_i d^2 k_{T,i}} = N_n \alpha_s^4 (M_{c\bar{c}}) \frac{\delta(\sum_{i=1}^n k_{T,i}) \delta(1 - \sum_{i=1}^n x_i)}{(m_h^2 - \sum_{i=1}^n (m_{T,i}^2/x_i))^2},$$

Fig. 3. The  $\psi\psi$  pair distributions are shown in (a) and (c) for the pion and proton projectiles. Similarly, the distributions of  $J/\psi$ 's from the pairs are shown in (b) and (d). Our calculations are compared with the  $\pi^- N$  data at 150 and 280 GeV/c [1]. The  $x_{\psi\psi}$  distributions are normalized to the number of pairs from both pion beams (a) and the number of pairs from the 400 GeV proton measurement (c). The number of single  $J/\psi$ 's is twice the number of pairs.

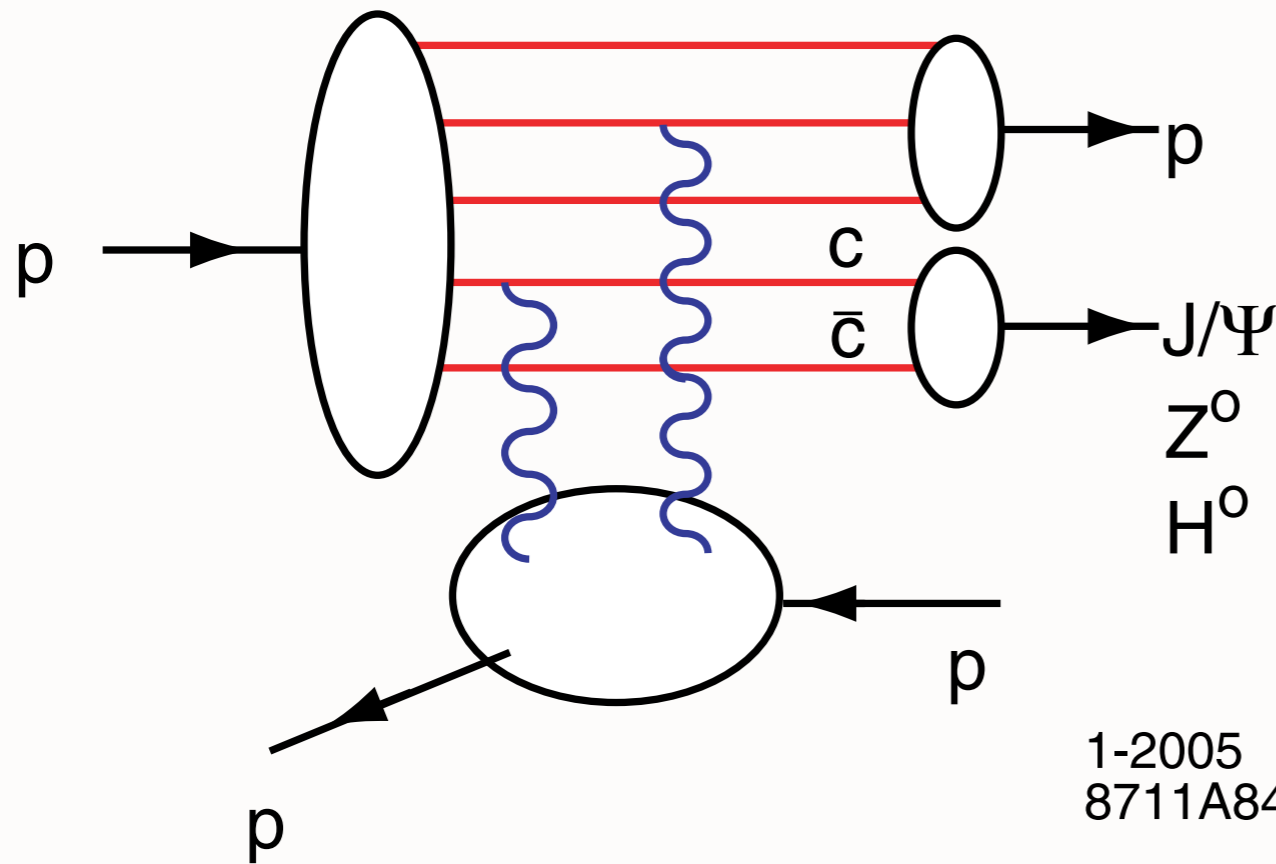
NA3 Data



*Production of a Double-Charm Baryon*

**SELEX high  $x_F$**        $\langle x_F \rangle = 0.33$

# Intrinsic Charm Mechanism for Exclusive Diffraction Production



1-2005  
8711A84

$$p p \rightarrow J/\psi p p$$

$$x_{J/\psi} = x_c + x_c$$

**Exclusive Diffractive  
High- $X_F$  Higgs Production**

**Kopeliovitch,  
Schmidt, Soffer, sjb**

Intrinsic  $cc$  pair formed in color octet  $8_C$  in proton wavefunction Large Color Dipole

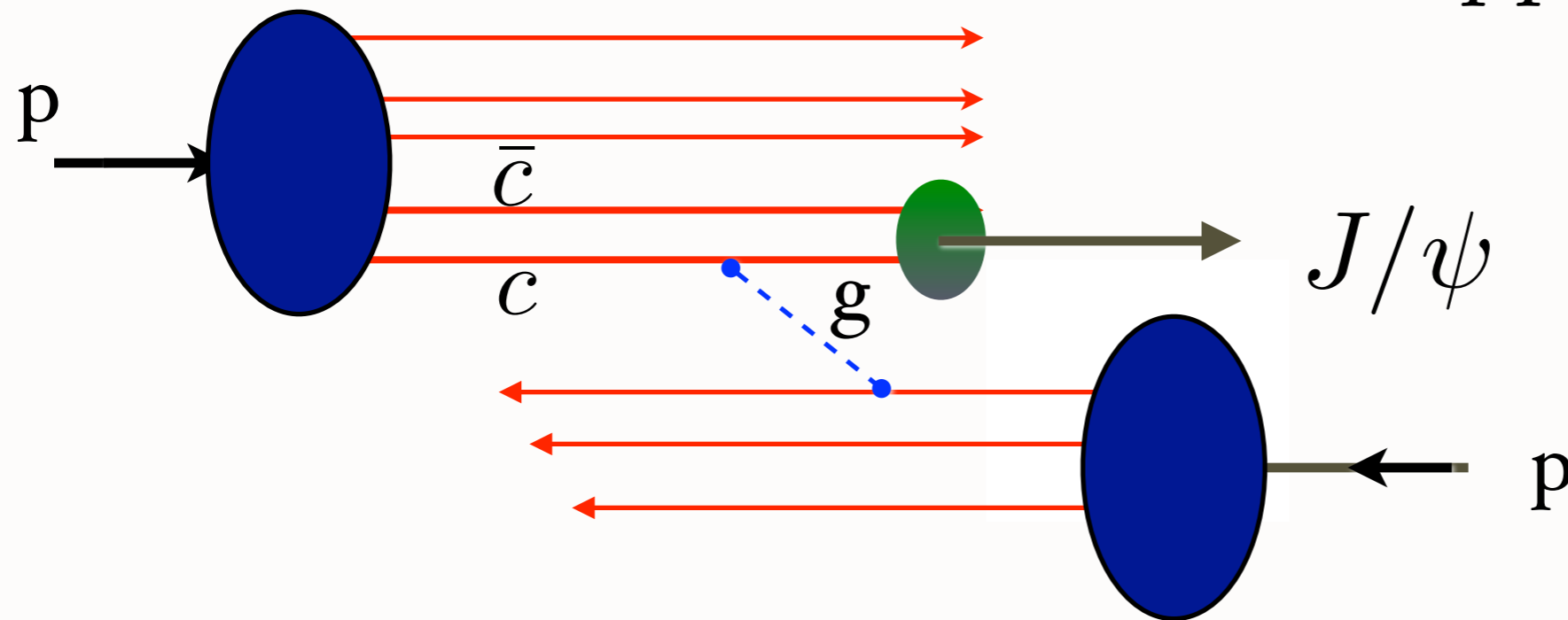
Collision produces color-singlet  $J/\psi$  through color exchange

RHIC Experiment



# *Intrinsic Charm Mechanism for Inclusive High- $x_F$ Quarkonium Production*

$$pp \rightarrow J/\psi X$$



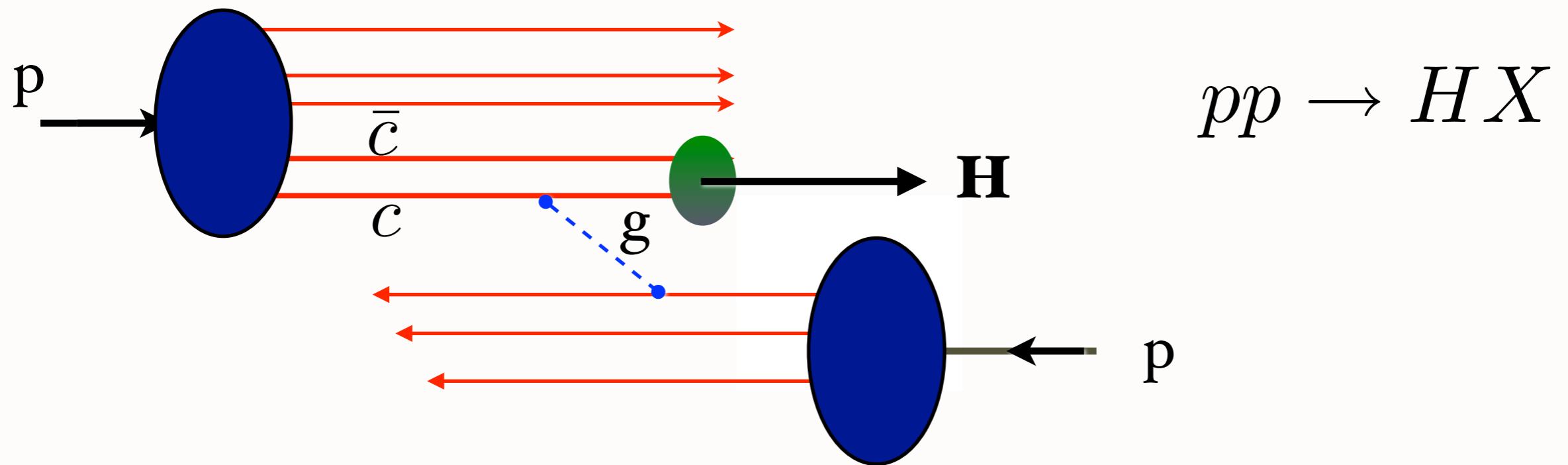
**Goldhaber, Kopeliovich, Soffer,  
Schmidt, sjb**

**Quarkonia can have 80% of Proton Momentum!**

*Color-octet IC interacts at front surface of nucleus*

**IC can explain large excess of quarkonia at large  $x_F$ , A-dependence**

# Intrinsic Charm Mechanism for Inclusive High- $x_F$ Higgs Production



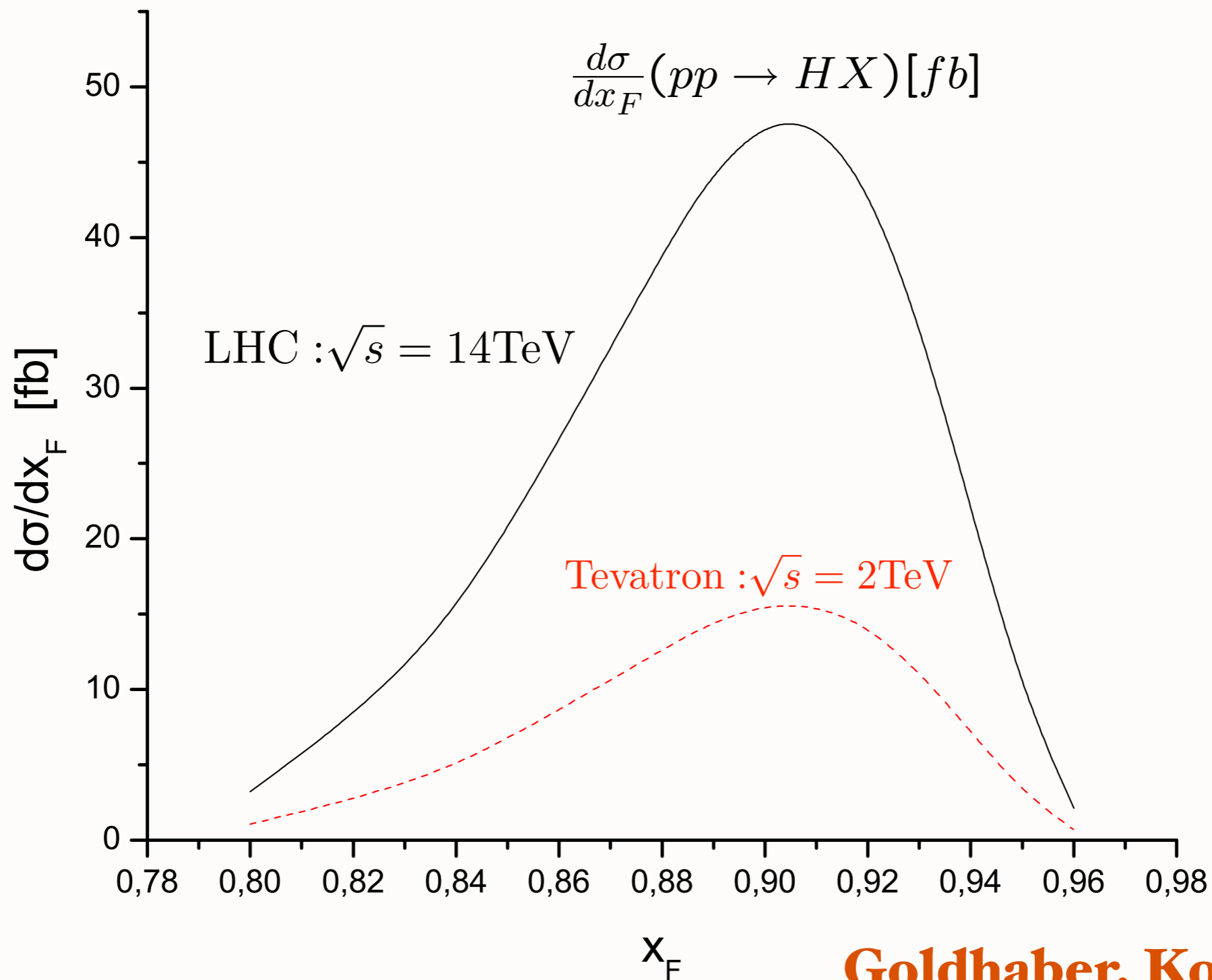
**Also: intrinsic bottom, top**

**Goldhaber, Kopeliovich,  
Schmidt, sjb**

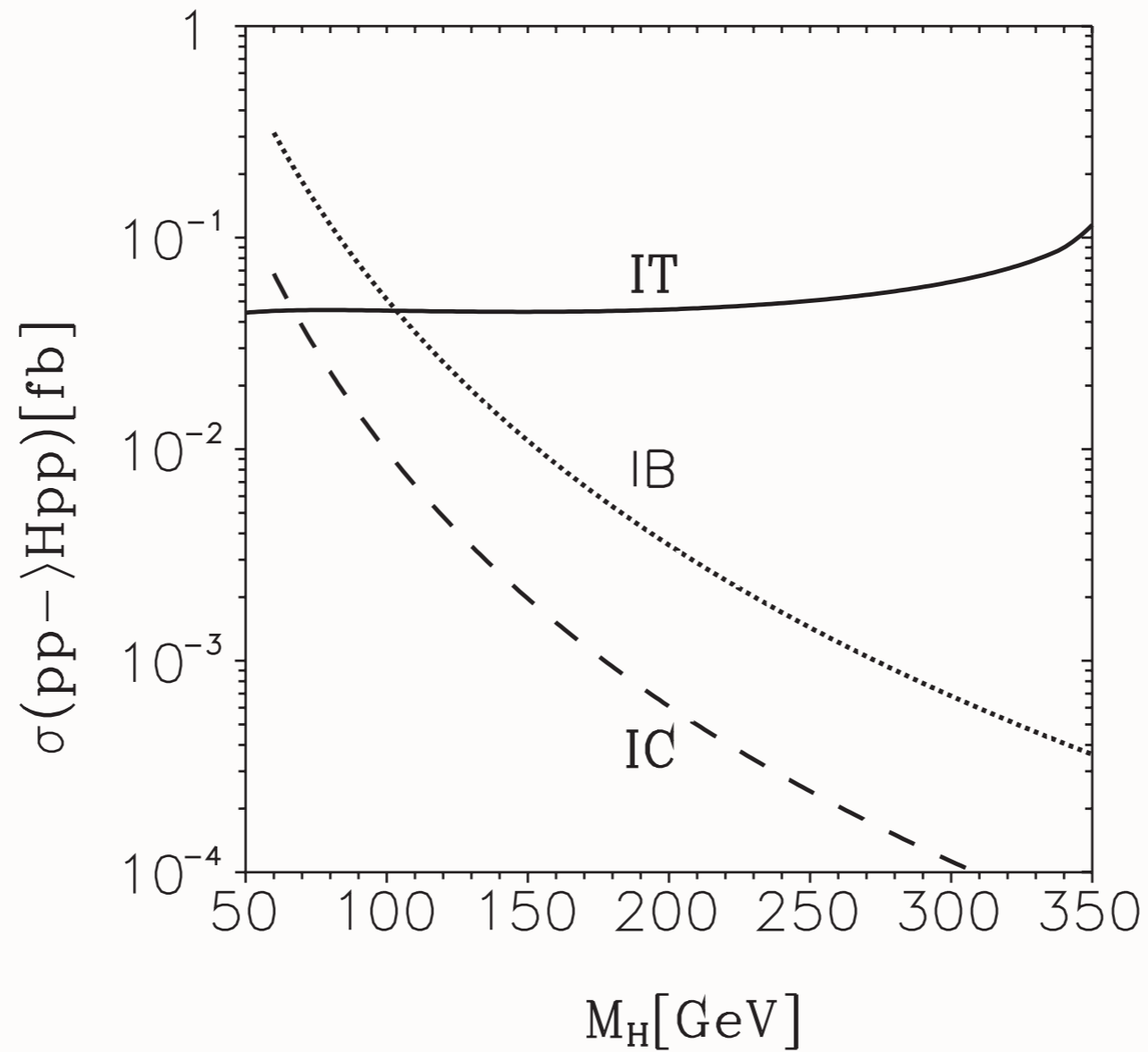
**Higgs can have 80% of Proton Momentum!**

*New search strategy for Higgs*

# Intrinsic Bottom Contribution to Inclusive Higgs Production

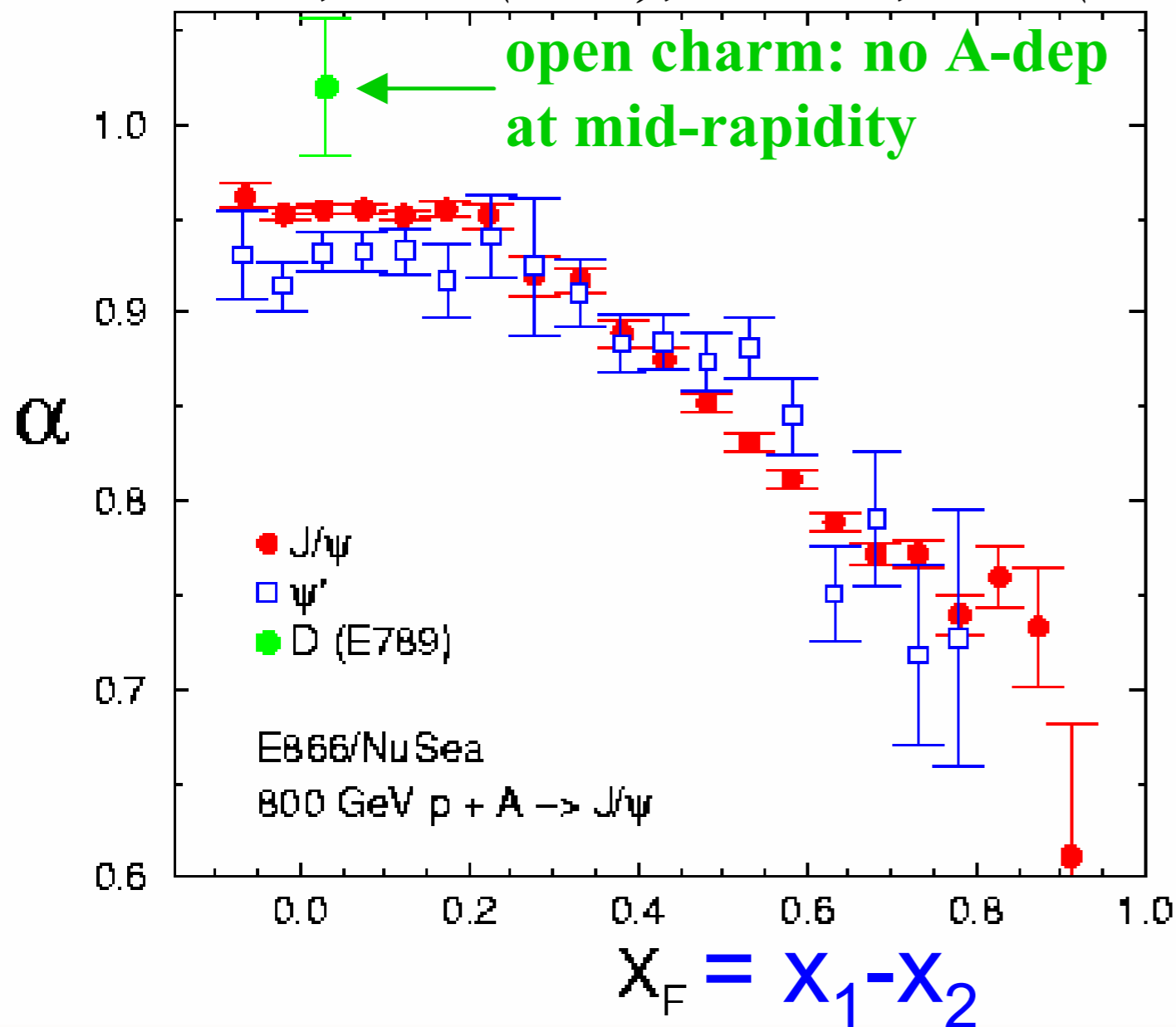


**Goldhaber, Kopeliovich,  
Schmidt, sjb**



The cross section of the reaction  $pp \rightarrow Hp + p$  as a function of the Higgs mass. Contributions of IC (dashed line), IB (dotted line), and IT (solid line).

800 GeV p-A (FNAL)  $\sigma_A = \sigma_p * A^\alpha$   
*PRL 84, 3256 (2000); PRL 72, 2542 (1994)*



$$\frac{d\sigma}{dx_F} (pA \rightarrow J/\psi X)$$

*Remarkably Strong Nuclear Dependence for Fast Charmonium*

*Violation of PQCD Factorization*

Violation of factorization in charm hadroproduction.

[P. Hoyer](#), [M. Vanttinen](#) (Helsinki U.), [U. Sukhatme](#) (Illinois U., Chicago) . HU-TFT-90-14, May 1990. 7pp.

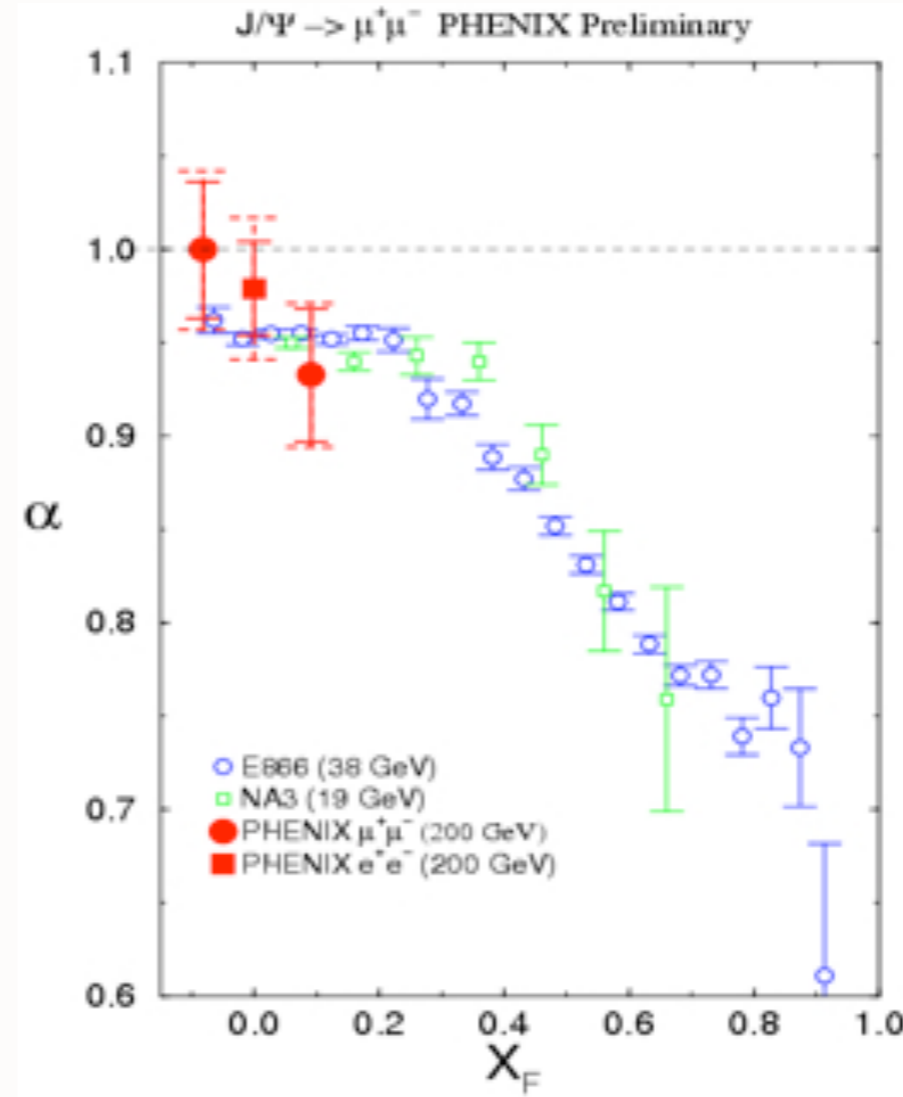
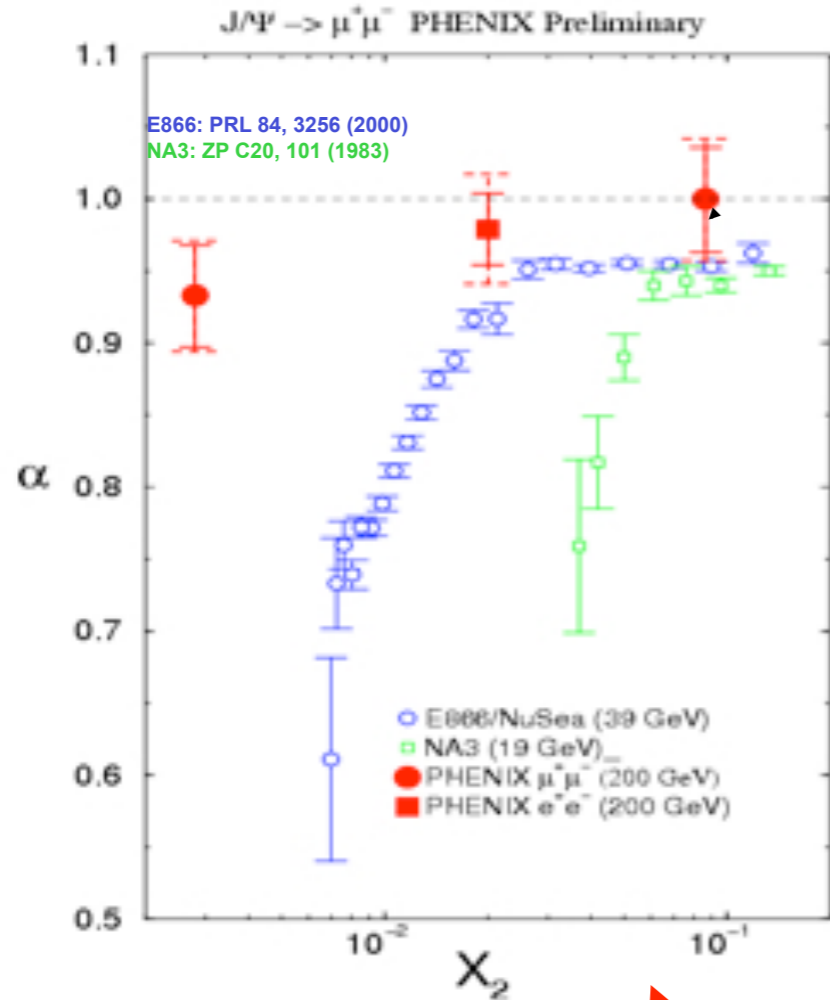
Published in Phys.Lett.B246:217-220,1990

**IC Explains large excess of quarkonia at large  $x_F$ , A-dependence**

# J/ψ nuclear dependence vrs rapidity, $x_{Au}$ , $x_F$

M.Leitch

## PHENIX compared to lower energy measurements



*Huge "absorption" effect*



Klein, Vogt, PRL 91:142301, 2003  
Kopeliovich, NP A696:669, 2001

*Violates PQCD factorization!*

$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X)$$

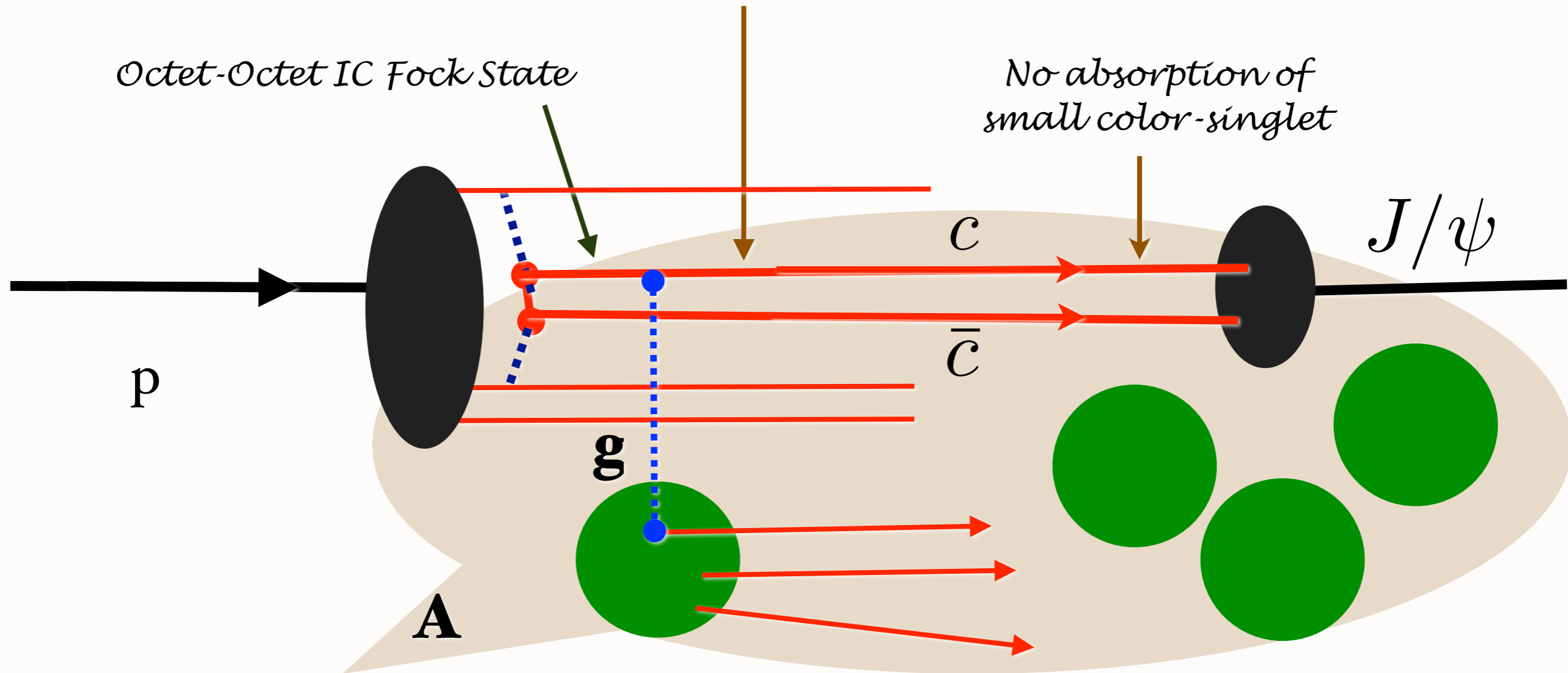
Hoyer, Sukhatme, Vanttinen

Violates PQCD Factorization:  $A^\alpha(x_F)$  not  $A^\alpha(x_2)$

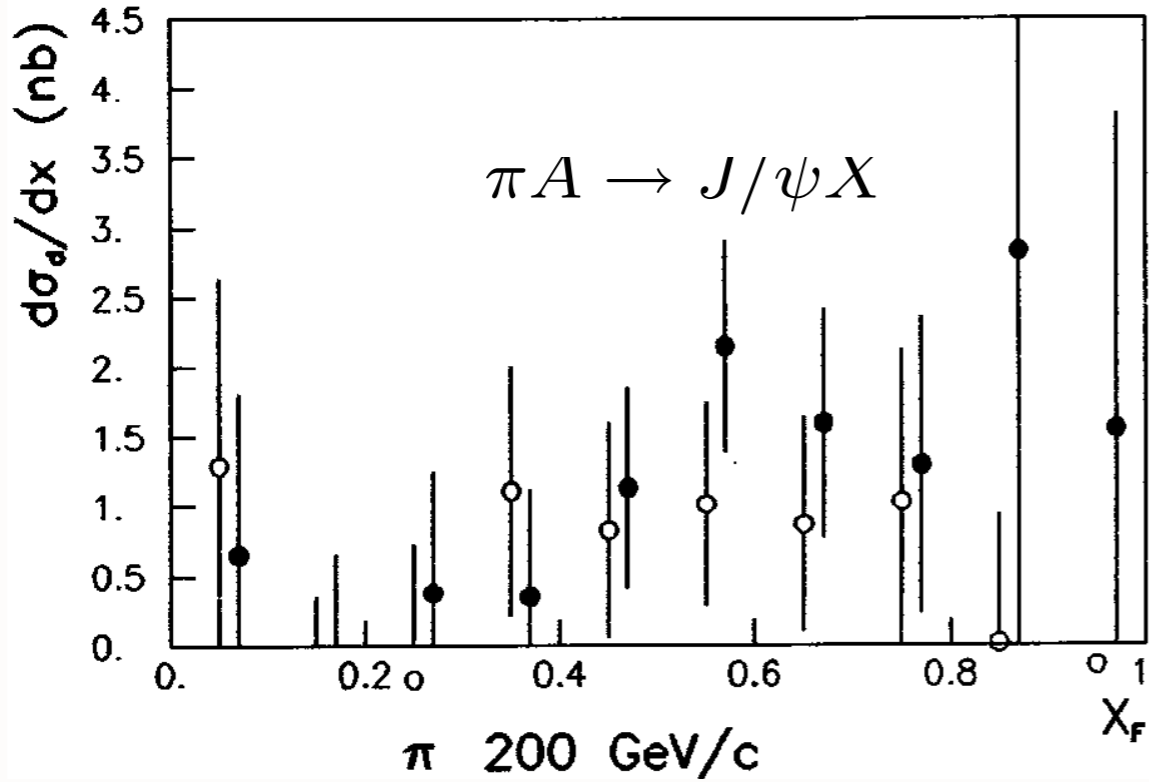
*Color-Opaque IC Fock state  
interacts on nuclear front surface*

**Kopeliovich,  
Schmidt, Goldhaber,  
Soffer, sjb**

*Scattering on front-face nucleon produces color-singlet  $c\bar{c}$  pair*

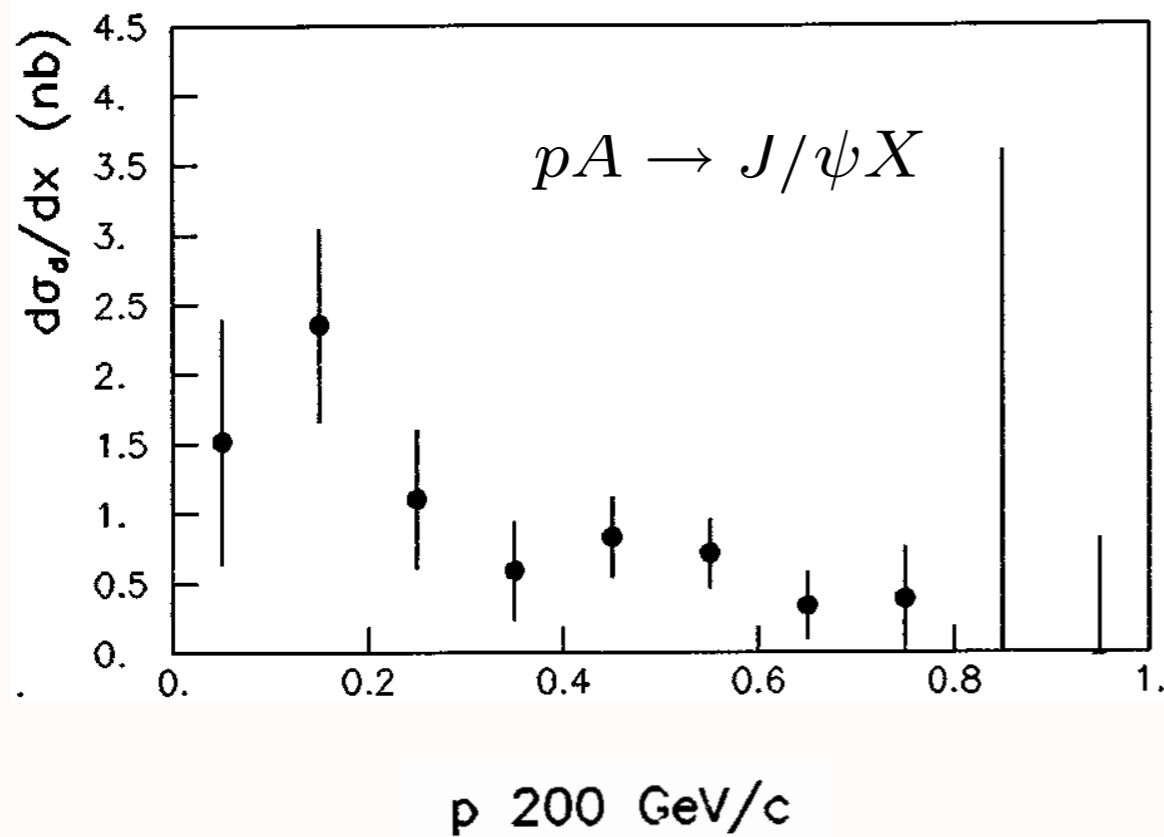


$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) = A^{2/3} \times \frac{d\sigma}{dx_F}(pN \rightarrow J/\psi X)$$



$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) = A^1 \frac{d\sigma_1}{dx_F} + A^{2/3} \frac{d\sigma_2}{dx_F}$$

$A^{2/3}$  component



*High  $x_F$ :*

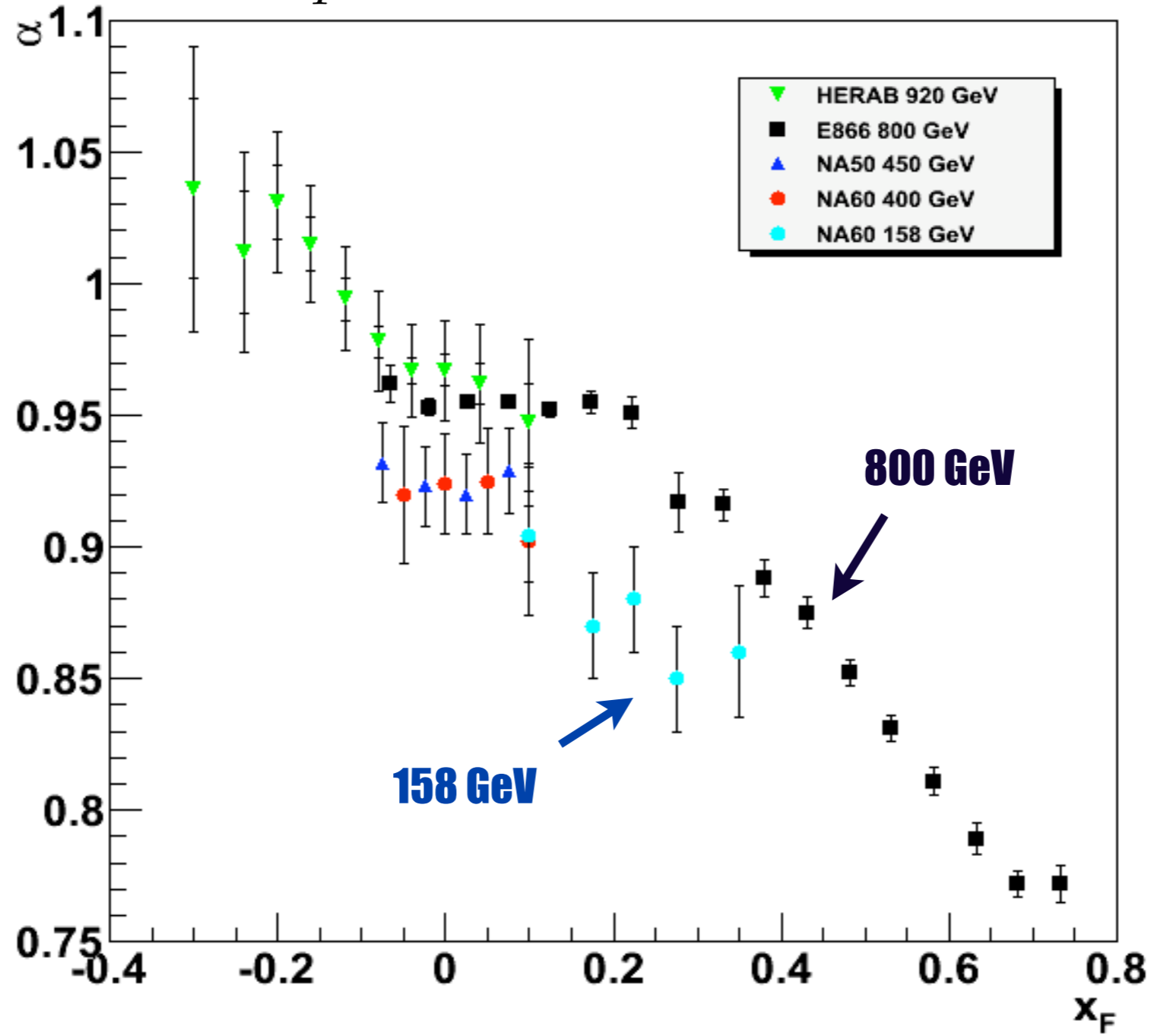
*Consistent with  
color-octet intrinsic  
charm*

**Excess beyond conventional gluon-splitting PQCD  
subprocesses**

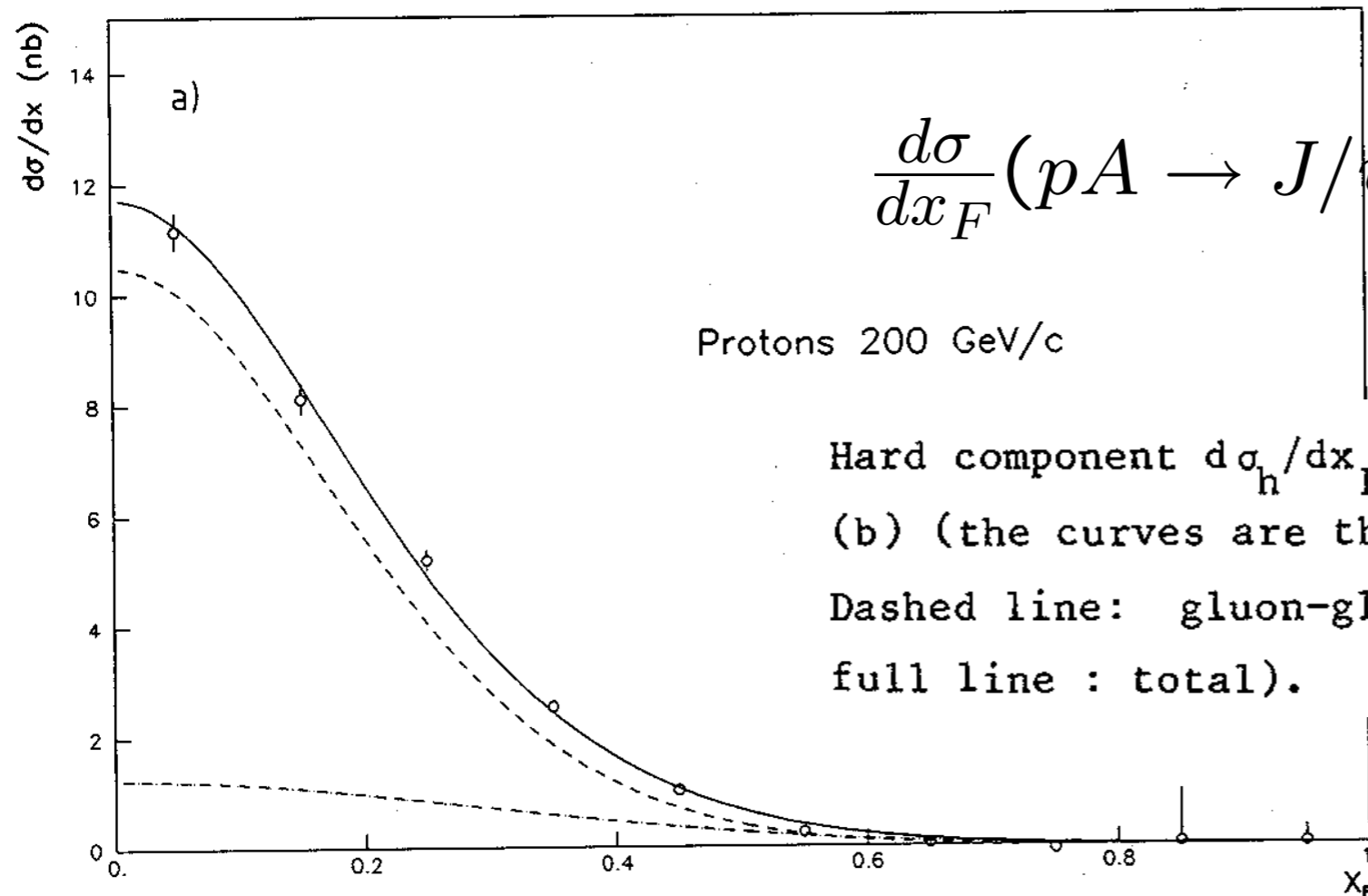


# NA60 pA data @ 158GeV

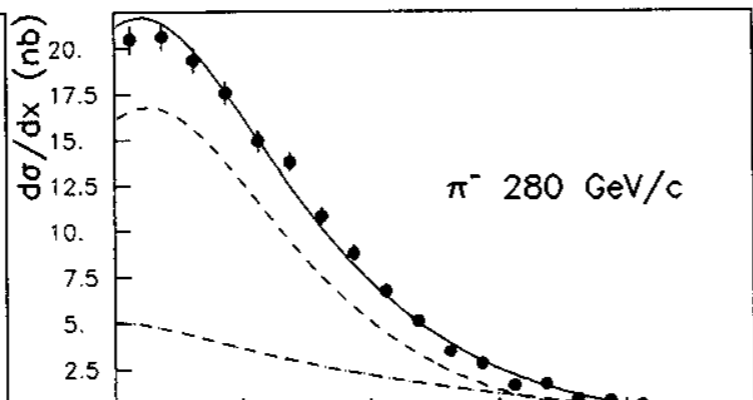
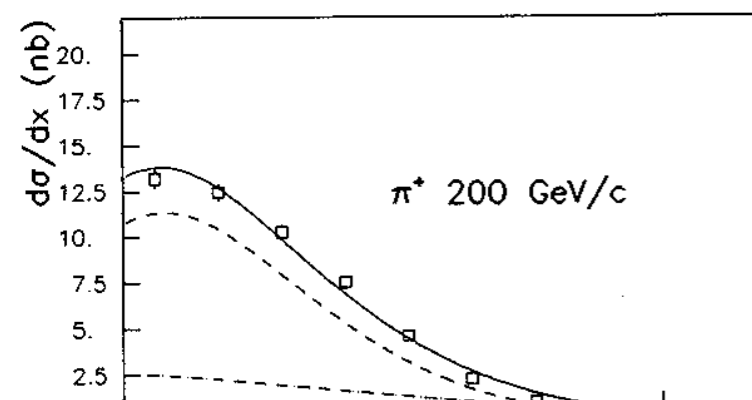
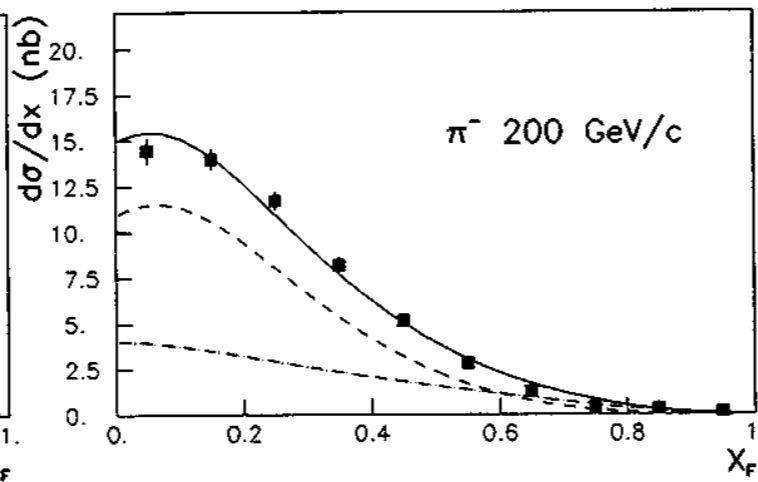
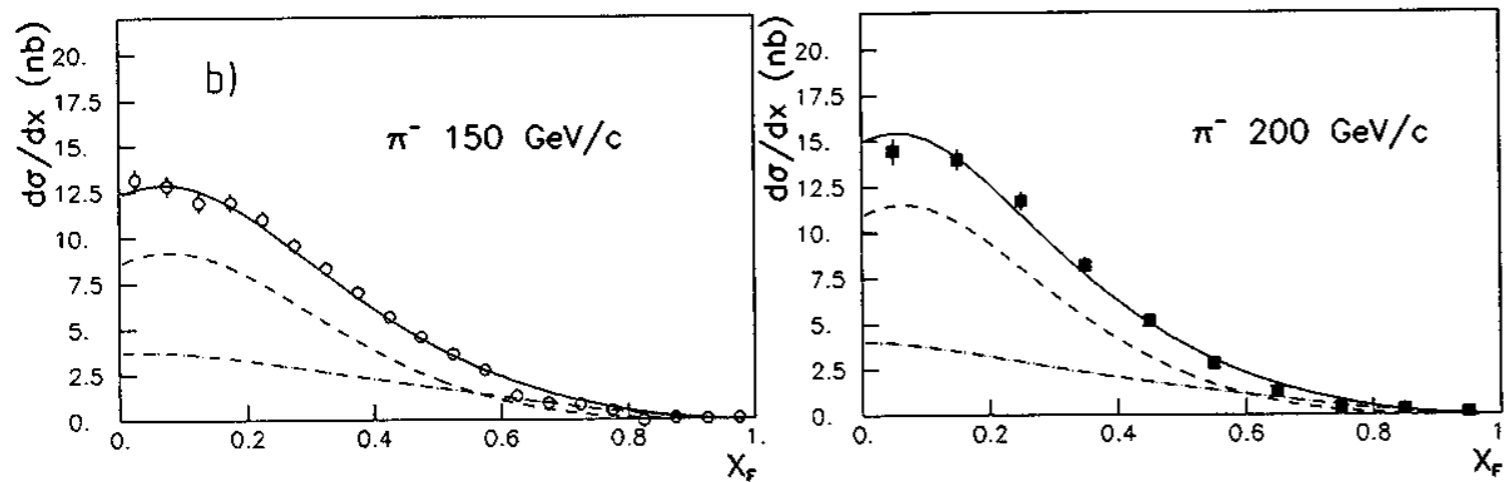
$$\frac{d\sigma}{dx_F}(pA \rightarrow J/\psi X) \propto A^\alpha$$



*Clear dependence  
on  $x_F$  and  
beam energy*



Hard component  $d\sigma_h/dx_F$  for incident protons (a) and pions (b) (the curves are the result of the fit described in the text. Dashed line: gluon-gluon fusion; dash-dotted line :  $q\bar{q}$  fusion; full line : total).



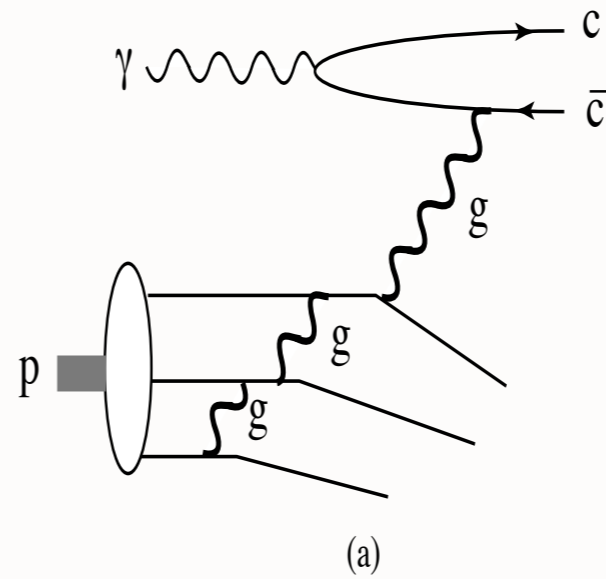
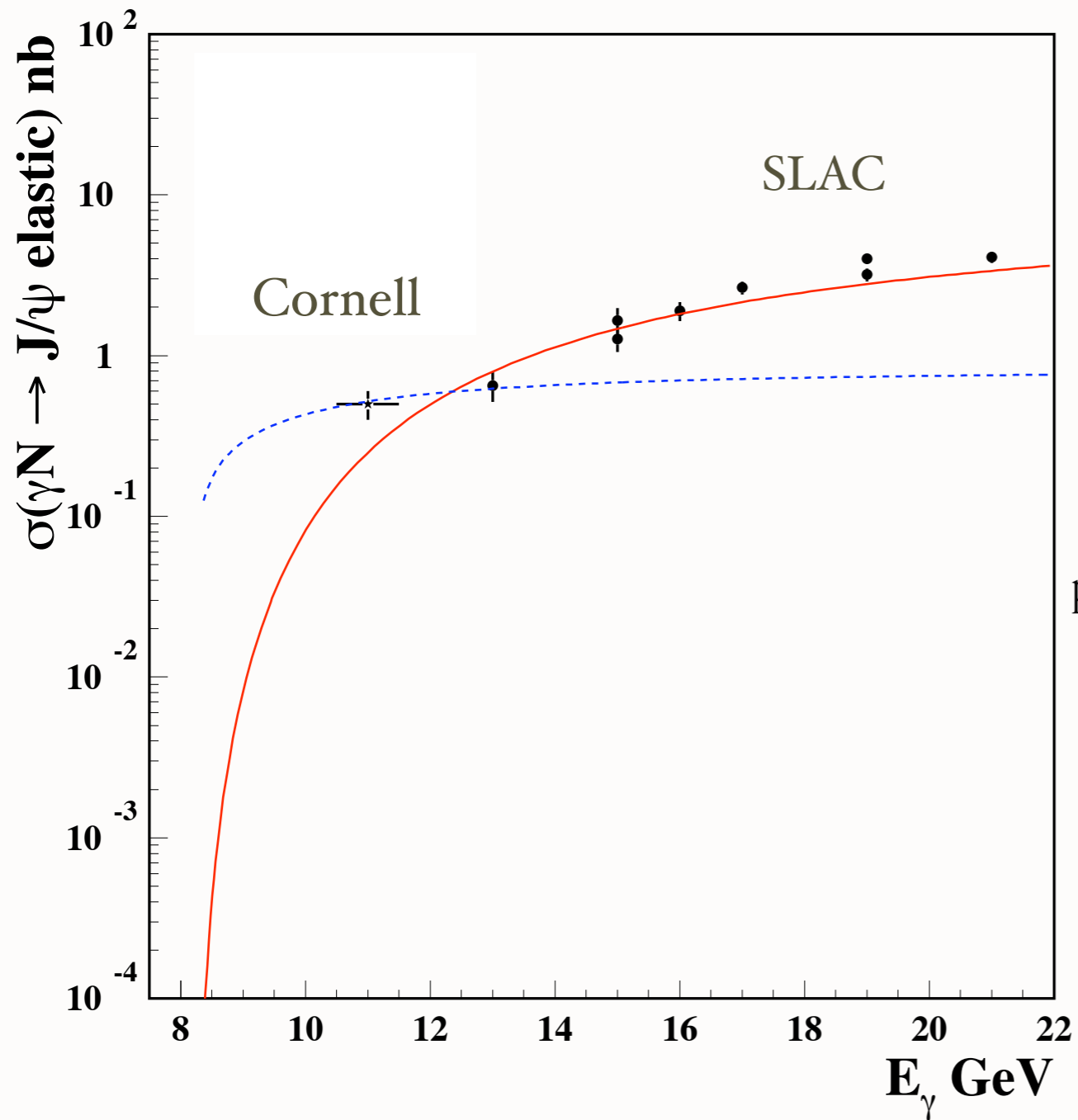
$A^1$  component consistent with sum of  $gg$  and  $q\bar{q}$  fusion

- IC Explains Anomalous  $\alpha(x_F)$  not  $\alpha(x_2)$  dependence of  $pA \rightarrow J/\psi X$   
(Mueller, Gunion, Tang, SJB)
- Color Octet IC Explains  $A^{2/3}$  behavior at high  $x_F$  (NA3, Fermilab) *Color Opacity*  
(Kopeliovitch, Schmidt, Soffer, SJB)
- IC Explains  $J/\psi \rightarrow \rho\pi$  puzzle  
(Karliner, SJB)
- IC leads to new effects in  $B$  decay  
(Gardner, SJB)

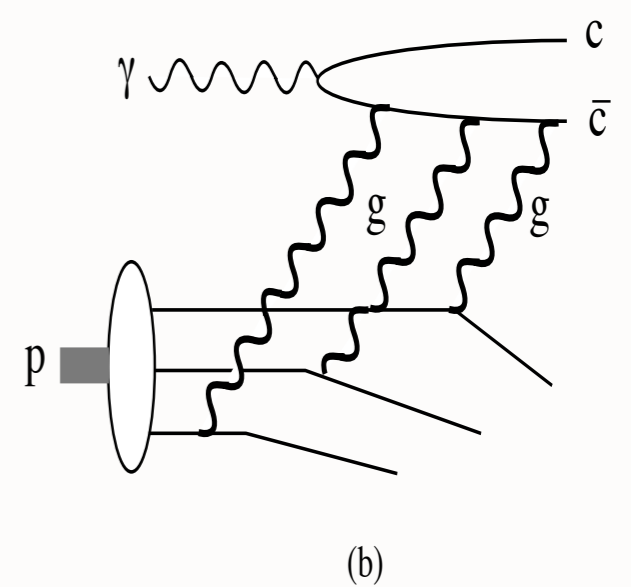
**Higgs production at  $x_F = 0.8$**

$$\gamma p \rightarrow J/\psi p$$

Chudakov, Hoyer, Laget, sjb



*Leading twist contribution*



*Dominant near threshold*

# Why is IQ Important for Flavor Physics?

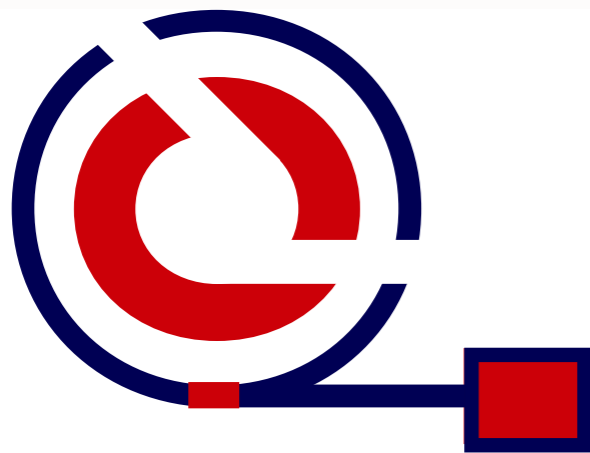
- **New perspective on fundamental nonperturbative hadron structure**
- **Charm structure function at high  $x$**
- **Dominates high  $x_F$  charm and charmonium production**
- **Hadroproduction of new heavy quark states such as ccu, ccd, bcc, bbb, at high  $x_F$**
- **Intrinsic charm -- long distance contribution to penguin mechanisms for weak decay** *Gardner, sjb*
- **$J/\psi \rightarrow \rho\pi$  puzzle explained** *Karliner, sjb*
- **Novel Nuclear Effects from color structure of IC, Heavy Ion Collisions**
- **New mechanisms for high  $x_F$  Higgs hadroproduction**
- **Dynamics of b production: LHCb** *New Multi-lepton Signals*
- **Fixed target program at LHC: produce bbb states**

- *7 TeV proton beam collisions on a proton or nuclear target -- Extract beam with Crystals -*
- *Minimal effects on the collider*
- *Equivalent to  $E_{cm} = 115$  GeV*
- *Nuclear and Polarized Targets*
- *Nuclear Beams: Produce QGP in Rest Frame of Target Nucleus*
- *Study Dynamics at extreme rapidities:  $X_F = -1$*
- *Secondary Beams -- Even B and D*
- *Diffraction on Nucleons and Nucleus*
- *Cosmic Ray Simulations*



## A Compelling Idea for QCD:

*Utilize the High-Energy LHC proton and nuclear beams in a fixed-target mode*



***AFTER @ LHC***

**A Fixed-Target Experiment**

*A new hadron physics laboratory for studying and testing QCD*

- Both  $p$  and  $Pb$  LHC beams can be extracted without disturbing the other experiments
- Extracting a few per cent of the beam  $\rightarrow 5 \times 10^8$  protons per sec
- This allows for high luminosity  $pp$ ,  $pA$  and  $PbA$  collisions at  $\sqrt{s} = 115$  GeV and  $\sqrt{s_{NN}} = 72$  GeV
- **Example: precision quarkonium studies** taking advantage of
  - high luminosity (reach in  $y$ ,  $P_T$ , small BR channels)
  - target versatility (CNM effects, strongly limited at colliders)
  - modern detection techniques (e.g.  $\gamma$  detection with high multiplicity)
- This would likely prepare the ground for  $g(x, Q^2)$  extraction
- A wealth of possible measurements: DY, Open  $b/c$ , jet correlation, UPC... (not mentioning secondary beams)
- Planned LHC long shutdown (< 2020 ?) could be used to install the extraction system
- Very good complementarity with electron-ion programs



# *Fixed Target Physics with the LHC Beams*

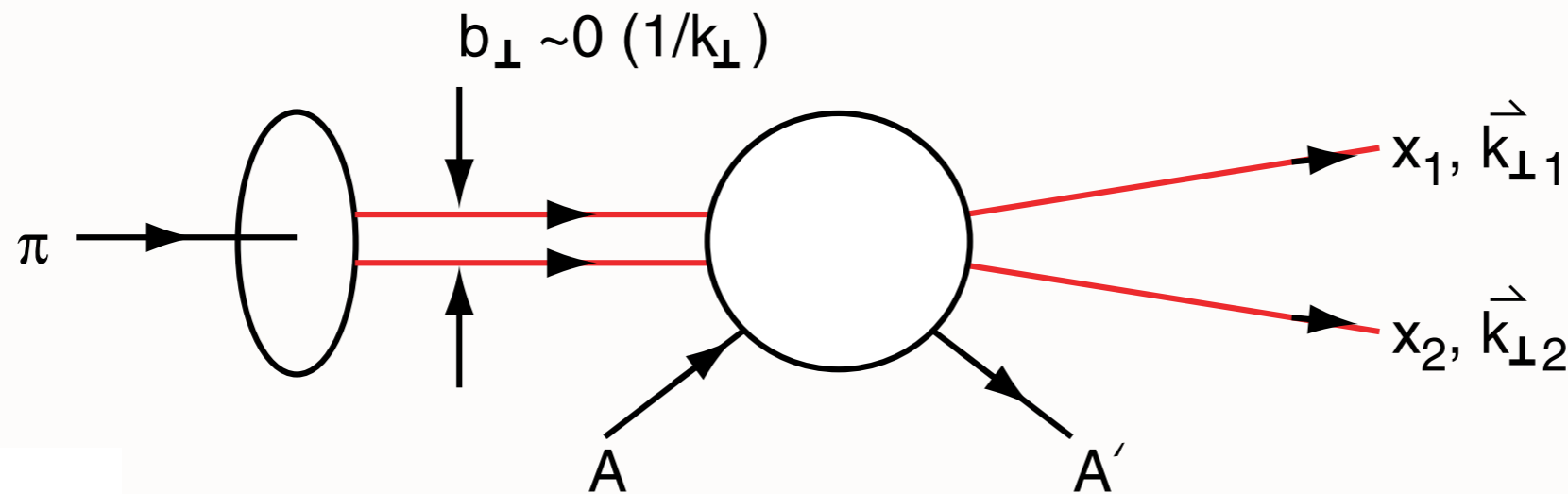
- **7 TeV proton beam, nuclear beams**
- **Full Range of Nuclear and Polarized Targets**
- **Cosmic Ray simulations!**
- **Single-Spin Asymmetries, Transversity Studies,  $A_N$**
- **High- $x_F$  Dynamics**
- **High- $x_F$  Heavy Quark Phenomena**
- **Production of  $ccq$  to  $ccc$  to  $bbb$  baryons**
- **Quark-Gluon Plasma in Nuclear Rest System**
- **Anti-Shadowing: Flavor Specific?**

# *Nuclear Collisions with AFTER*

- **Nucleus-Nucleus and Proton-Nucleus Scattering in Lab Frame Look at Target Fragmentation Region  $x_F = -1$**
- **What happens to Target Nucleus when QGP is formed?**
- **Ridge at extreme rapidity**
- **What are the critical parameters for the onset of QGP**
- **Light-Front Description: Frame-Independent**
- **Use Fool's ISR Frame -- No Lorentz Contraction of LFWF**
- **Energy Loss Studies, LPM, Non-Abelian**
- **Quarkonium Production, Polarization**
- **Open charm, bottom**

# Diffractive Dissociation of Pion into Quark Jets

E791 Ashery et al.



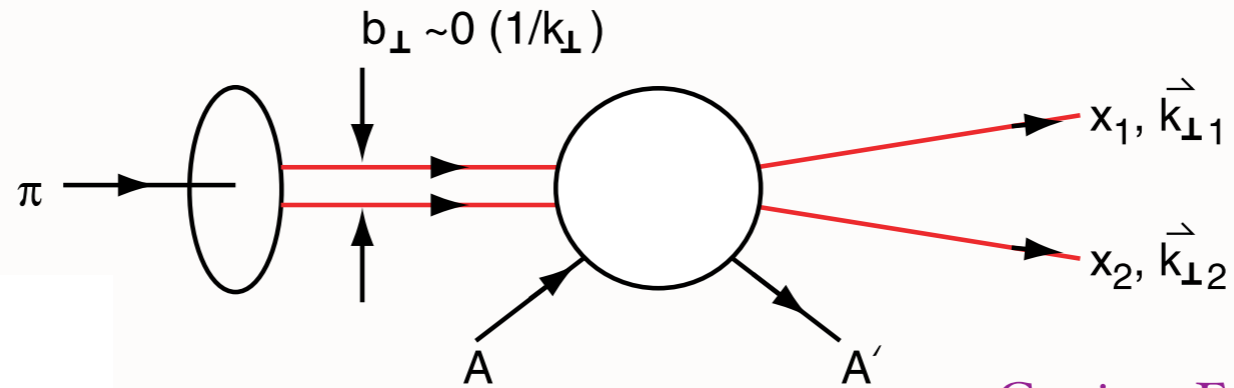
$$M \propto \frac{\partial^2}{\partial^2 k_{\perp}} \psi_{\pi}(x, k_{\perp})$$

Measure Light-Front Wavefunction of Pion

Minimal momentum transfer to nucleus

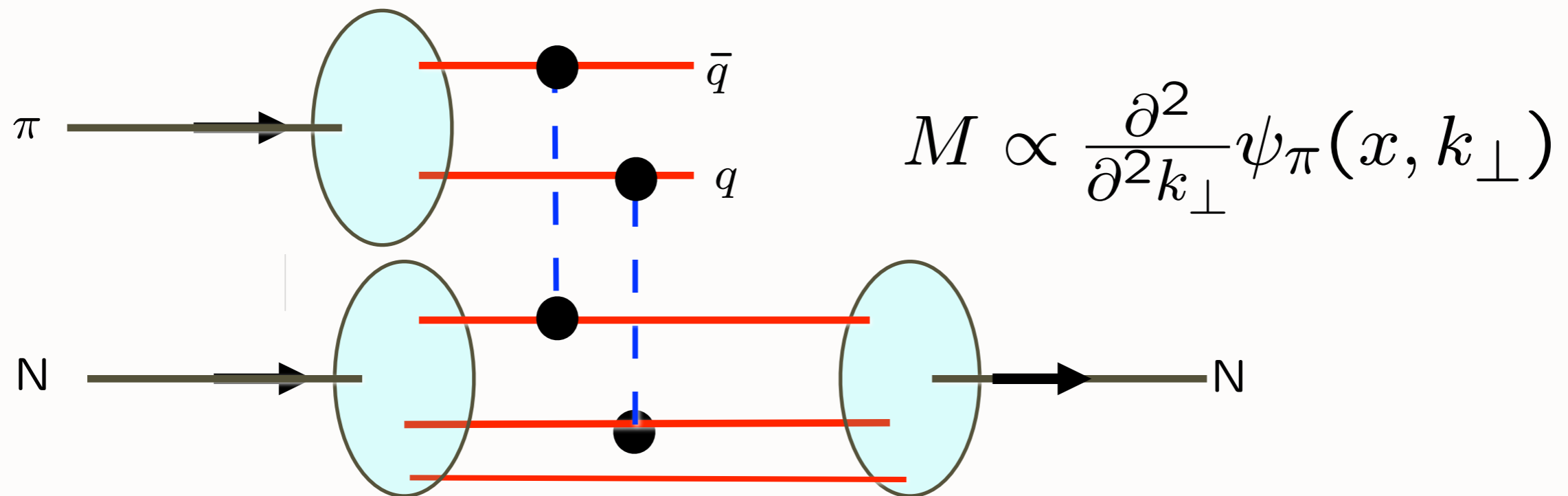
Nucleus left Intact!

# E791 FNAL Diffractive DiJet

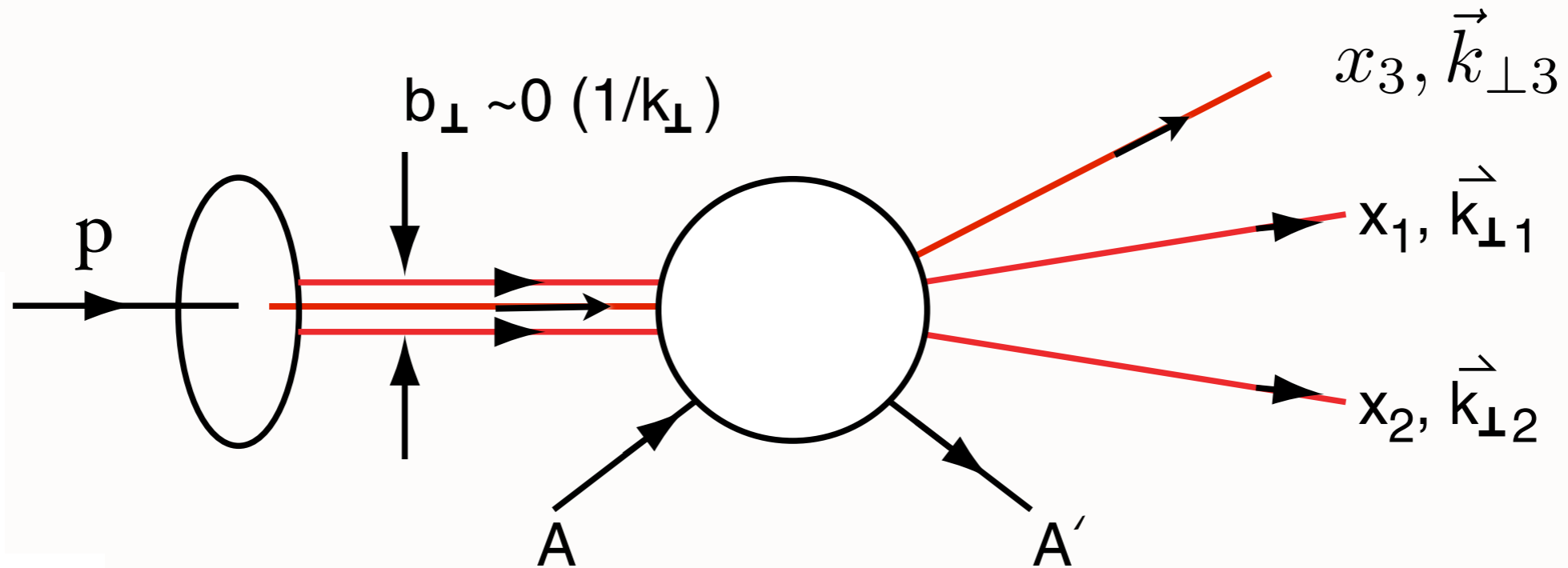


Gunion, Frankfurt, Mueller, Strikman, sjb  
Frankfurt, Miller, Strikman

*Two-gluon exchange measures the second derivative of the pion light-front wavefunction*



# Diffractive Dissociation of Proton into Three Quark Jets

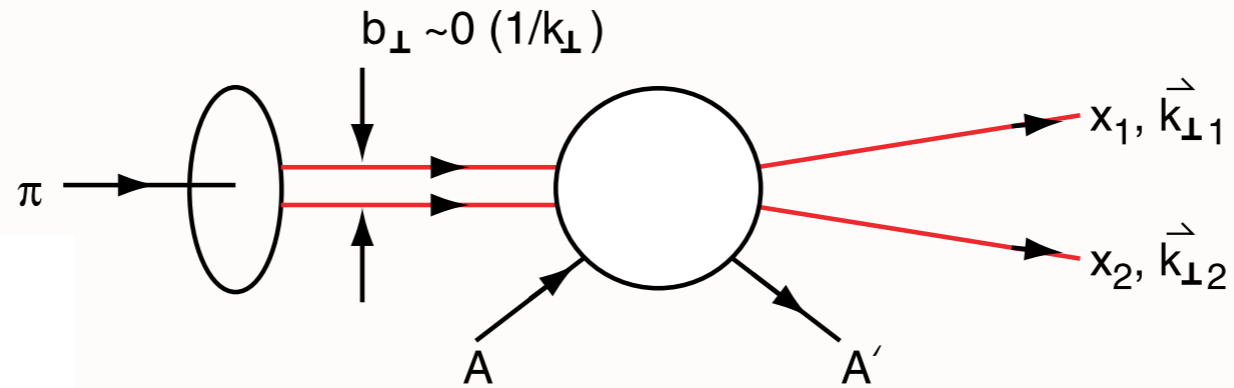


Measure Light-Front Wavefunction of Proton

*Minimal momentum transfer to nucleus*

*Nucleus left Intact!*

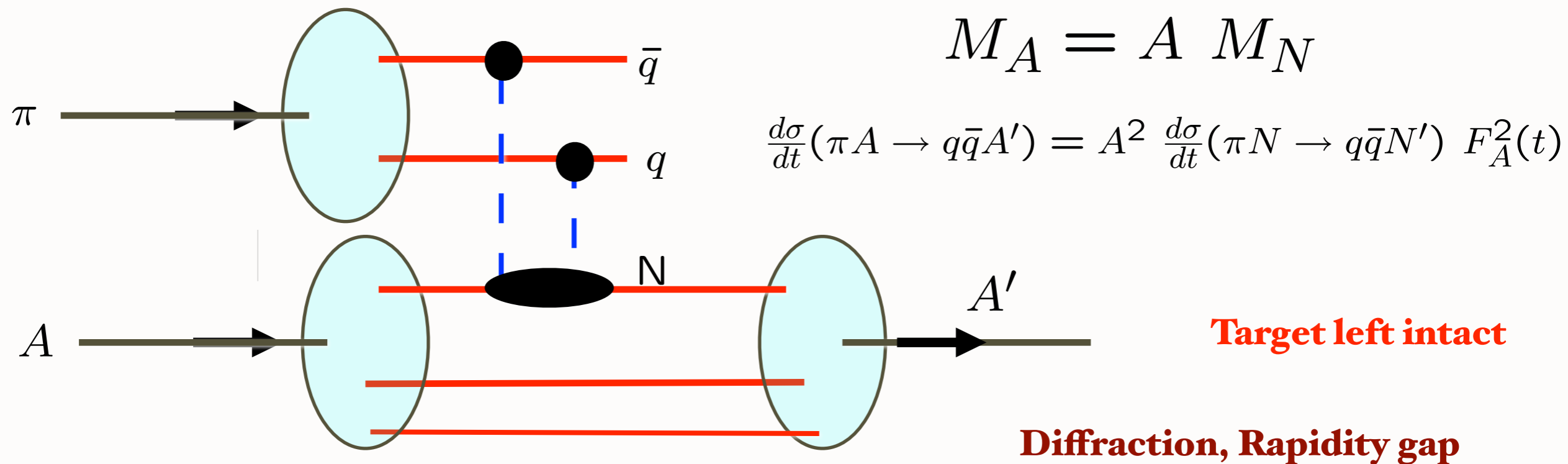
# Key Ingredients in E791 Experiment



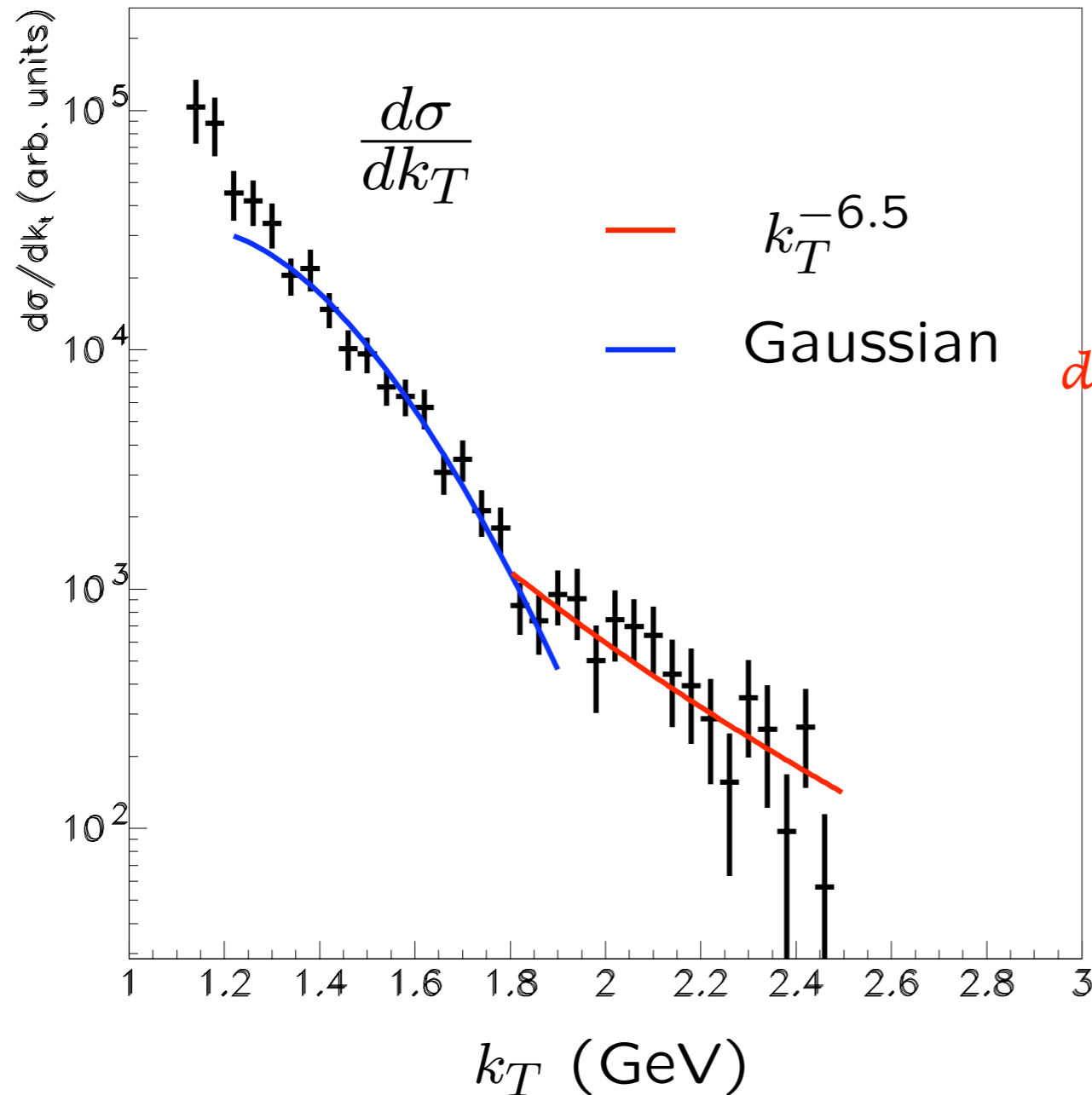
Brodsky Mueller  
Frankfurt Miller Strikman

*Small color-dipole moment pion not absorbed;  
interacts with each nucleon coherently*

QCD COLOR Transparency



# E791 Diffractive Di-Jet transverse momentum distribution

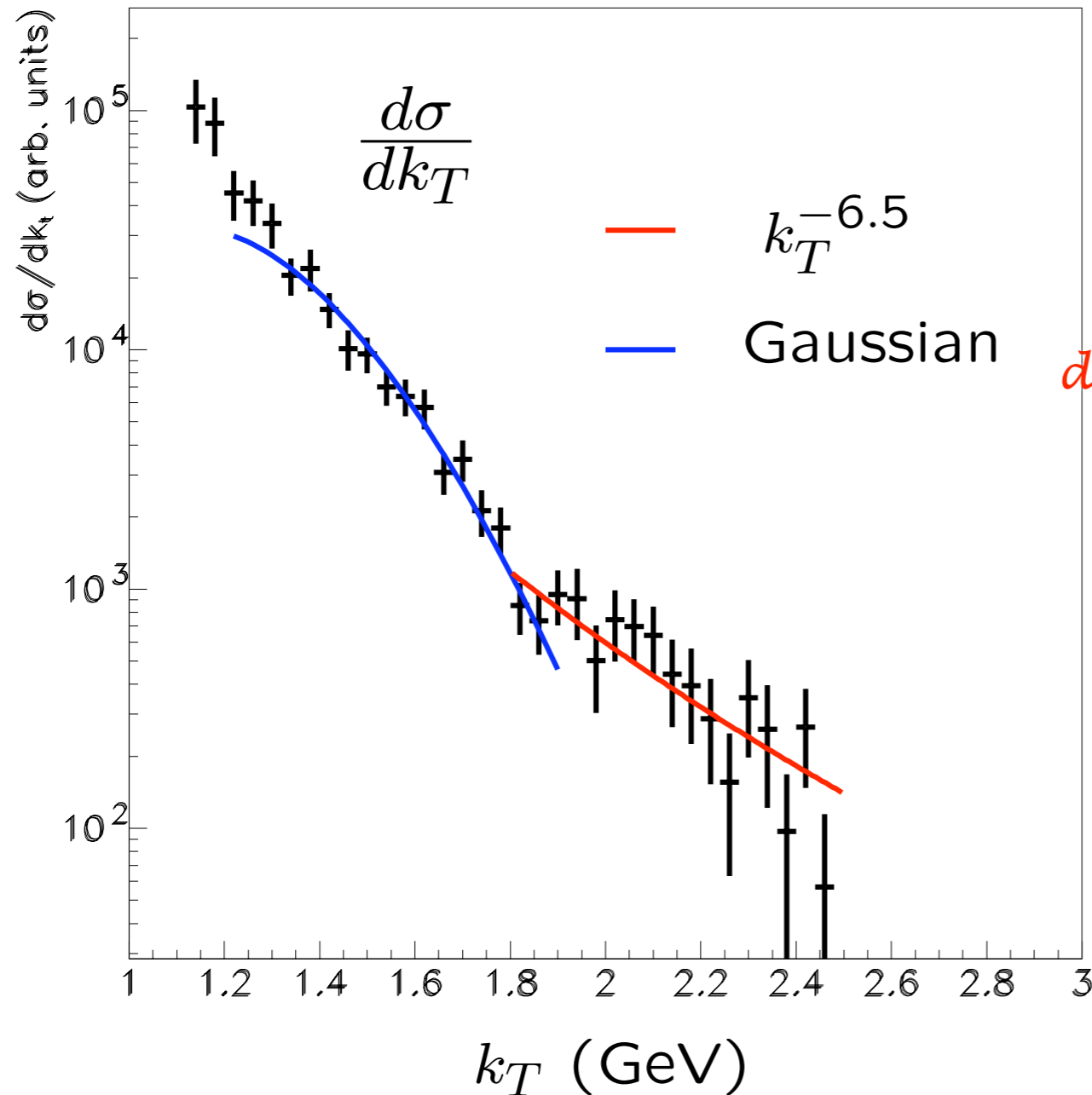


## Two Components

*High Transverse momentum dependence consistent with PQCD, ERBL Evolution,  $k_T^{-6.5}$*

*Gaussian component similar to AdS/CFT H0 LFWF*

# E791 Diffractive Di-Jet transverse momentum distribution



## Two Components

*High Transverse momentum dependence consistent with PQCD, ERBL Evolution,  $k_T^{-6.5}$*

*Gaussian component similar to AdS/CFT H0 LFWF*

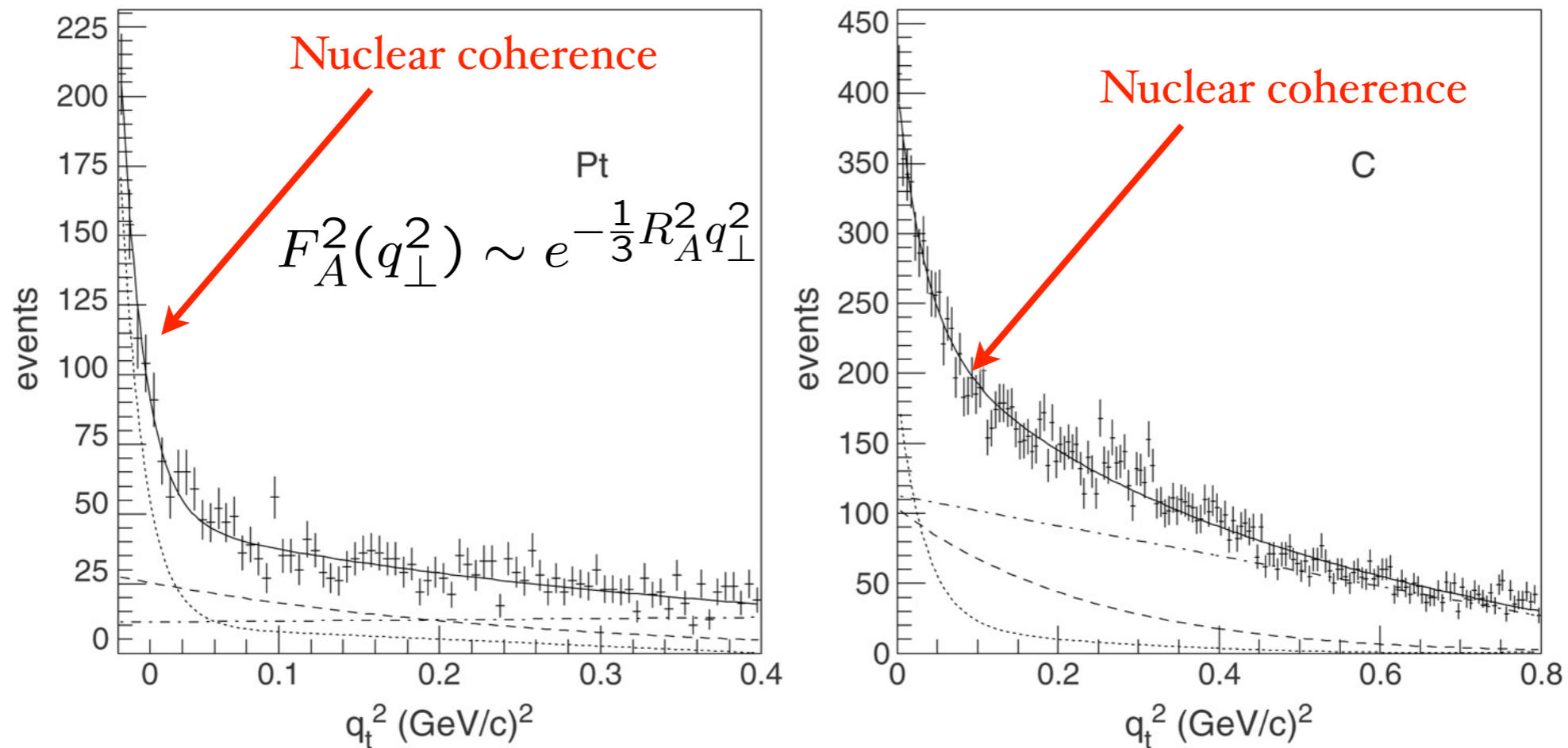


- Fully coherent interactions between pion and nucleons.
- Emerging Di-Jets do not interact with nucleus.

$$\mathcal{M}(A) = A \cdot \mathcal{M}(N)$$

$$\frac{d\sigma}{dq_t^2} \propto A^2 \quad q_t^2 \sim 0$$

$$\sigma \propto A^{4/3}$$



# Measure pion LFWF in diffractive dijet production

## Confirmation of color transparency

A-Dependence results:  $\sigma \propto A^\alpha$

<u><math>k_t</math> range (GeV/c)</u>	<u><math>\alpha</math></u>	<u><math>\alpha</math> (CT)</u>
$1.25 < k_t < 1.5$	$1.64 +0.06 -0.12$	1.25
$1.5 < k_t < 2.0$	$1.52 \pm 0.12$	1.45
$2.0 < k_t < 2.5$	$1.55 \pm 0.16$	1.60

Ashery E791

$\alpha$  (Incoh.) =  $0.70 \pm 0.1$

*Conventional Glauber Theory Ruled Out !*

**Factor of 7**

# Color Transparency

**Bertsch, Gunion,  
Goldhaber, sjb  
A. H. Mueller, sjb**

- Fundamental test of gauge theory in hadron physics
- Small color dipole moments interact weakly in nuclei
- Complete coherence at high energies
- Clear Demonstration of CT from Diffractive Di-Jets

$$\pi^- N \rightarrow \mu^+ \mu^- X \text{ at } 80 \text{ GeV}/c$$

$$\frac{d\sigma}{d\Omega} \propto 1 + \lambda \cos^2\theta + \rho \sin 2\theta \cos\phi + \omega \sin^2\theta \cos 2\phi.$$

$$\frac{d^2\sigma}{dx_\pi d\cos\theta} \propto x_\pi \left[ (1-x_\pi)^2 (1 + \cos^2\theta) + \frac{4}{9} \frac{\langle k_T^2 \rangle}{M^2} \sin^2\theta \right]$$

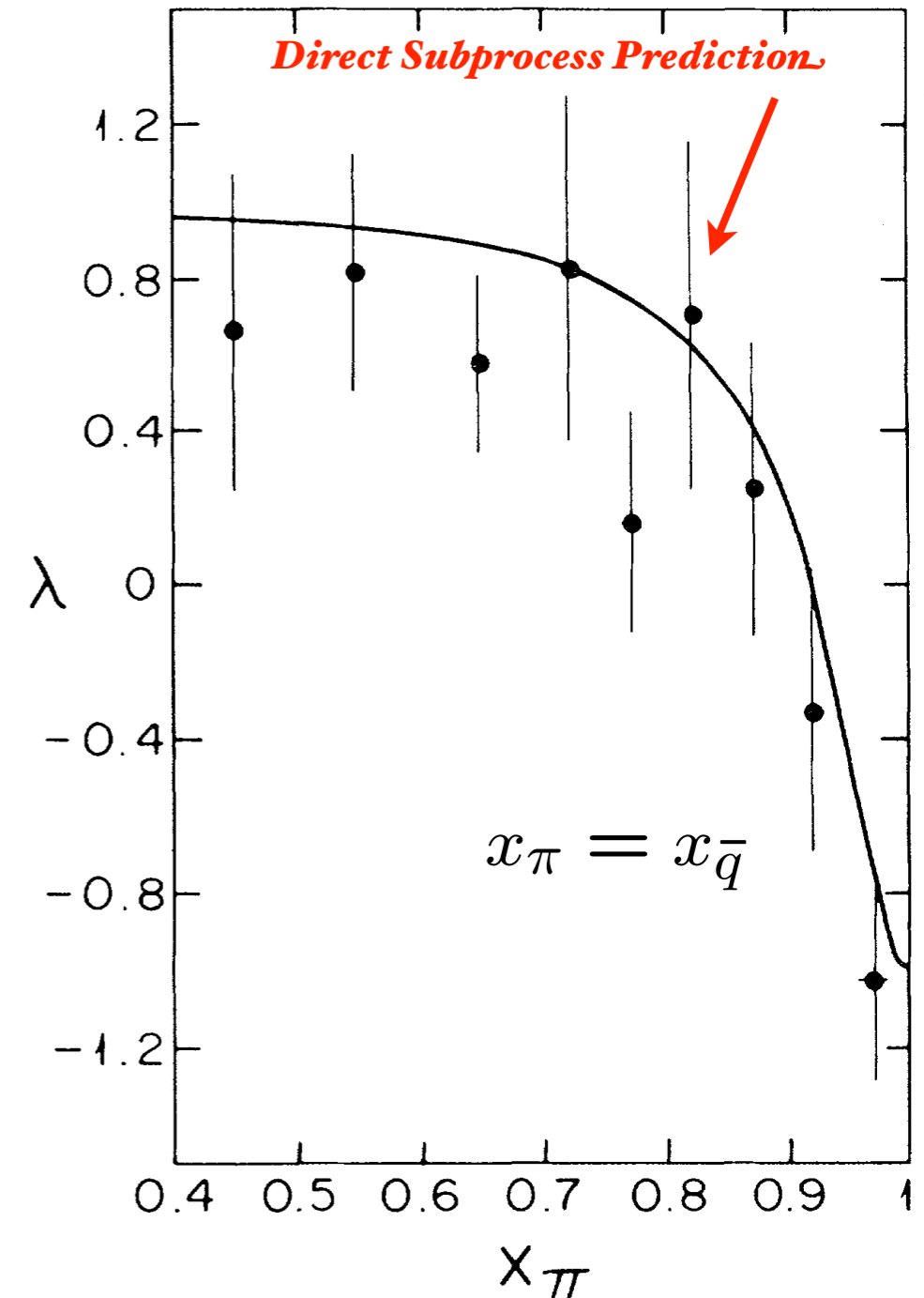
$$\langle k_T^2 \rangle = 0.62 \pm 0.16 \text{ GeV}^2/c^2$$

$$Q^2 = M^2$$

*Dramatic change in angular distribution at large  $x_F$*

**Example of a higher-twist direct subprocess**

*Many Tests at AFTER*



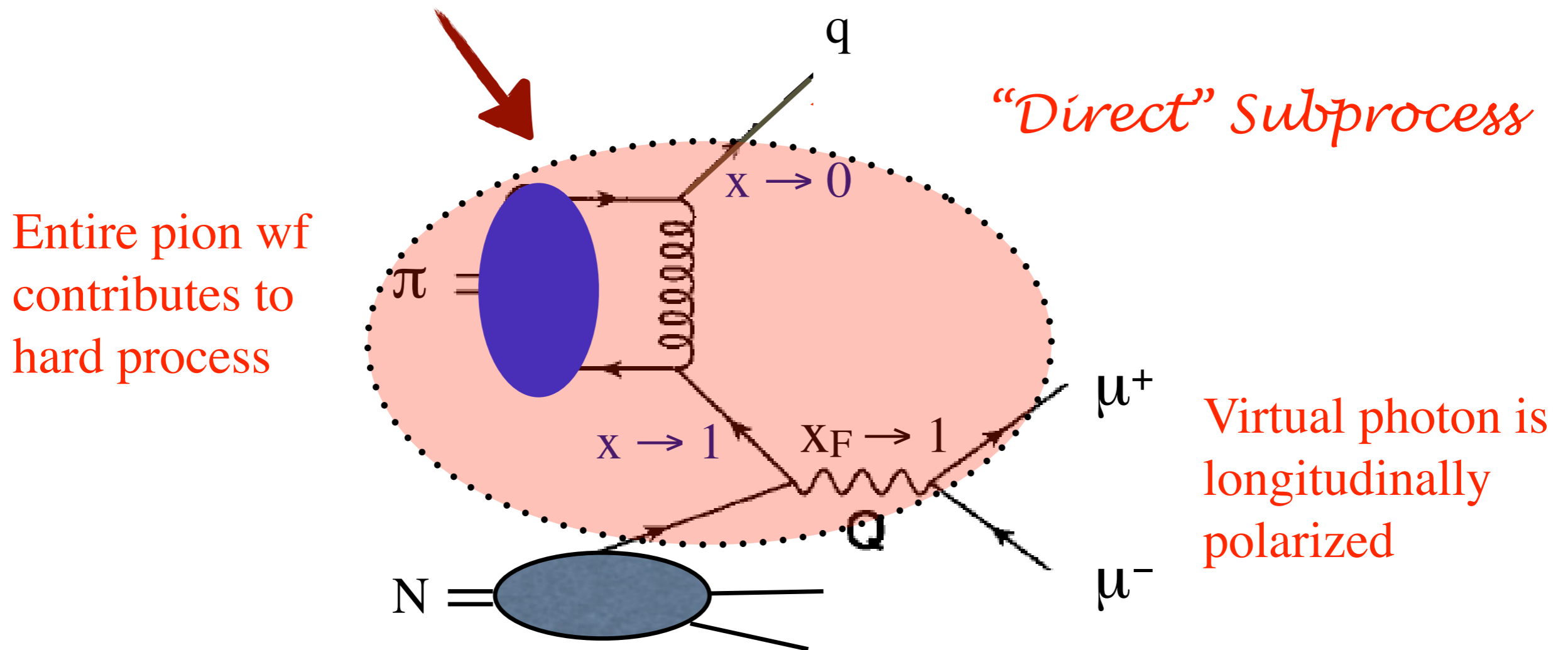
Chicago-Princeton  
Collaboration

Phys.Rev.Lett.55:2649,1985

$$\pi N \rightarrow \mu^+ \mu^- X \text{ at high } x_F$$

In the limit where  $(1-x_F)Q^2$  is fixed as  $Q^2 \rightarrow \infty$

*Distribution amplitude from AdS/CFT*



***Similar higher twist terms in jet hadronization at large  $z$***

**Berger, sjb  
Khoze, Brandenburg, Muller, sjb**

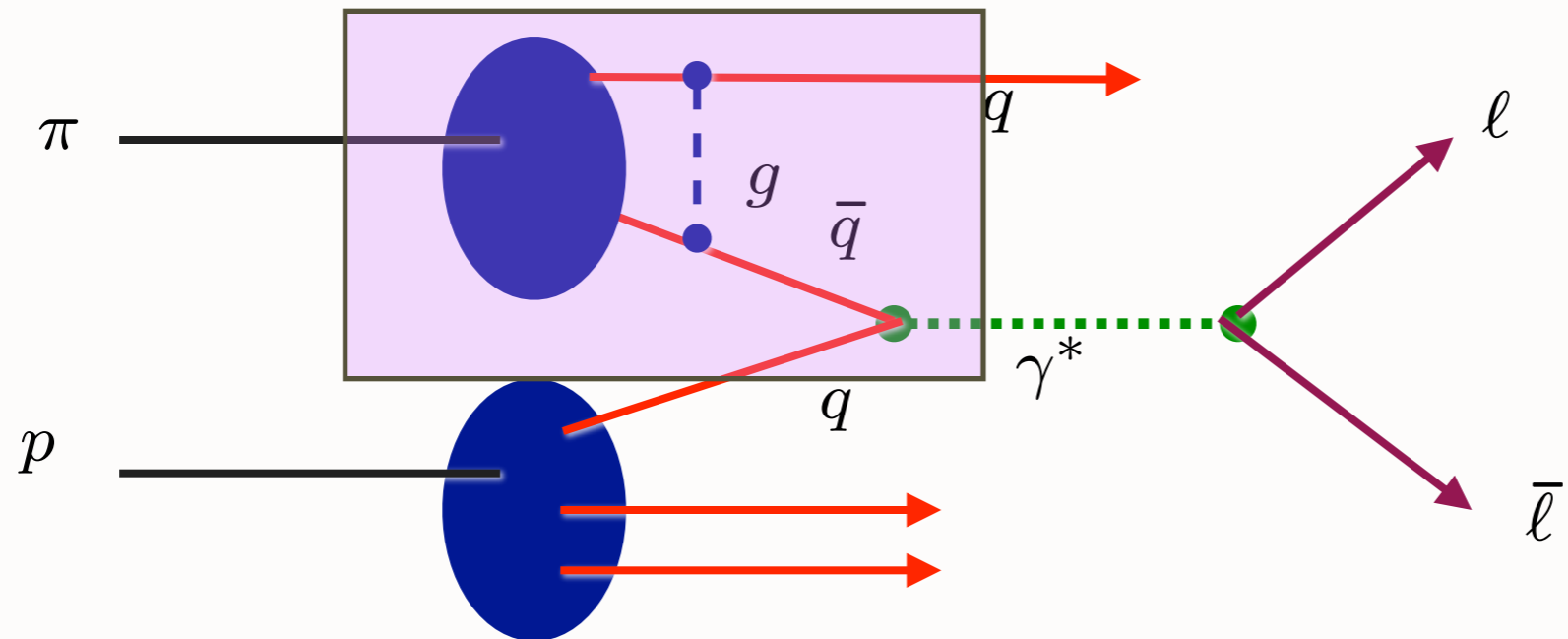
**Hoyer Vanttinen**

**Warsaw  
July 6, 2012**

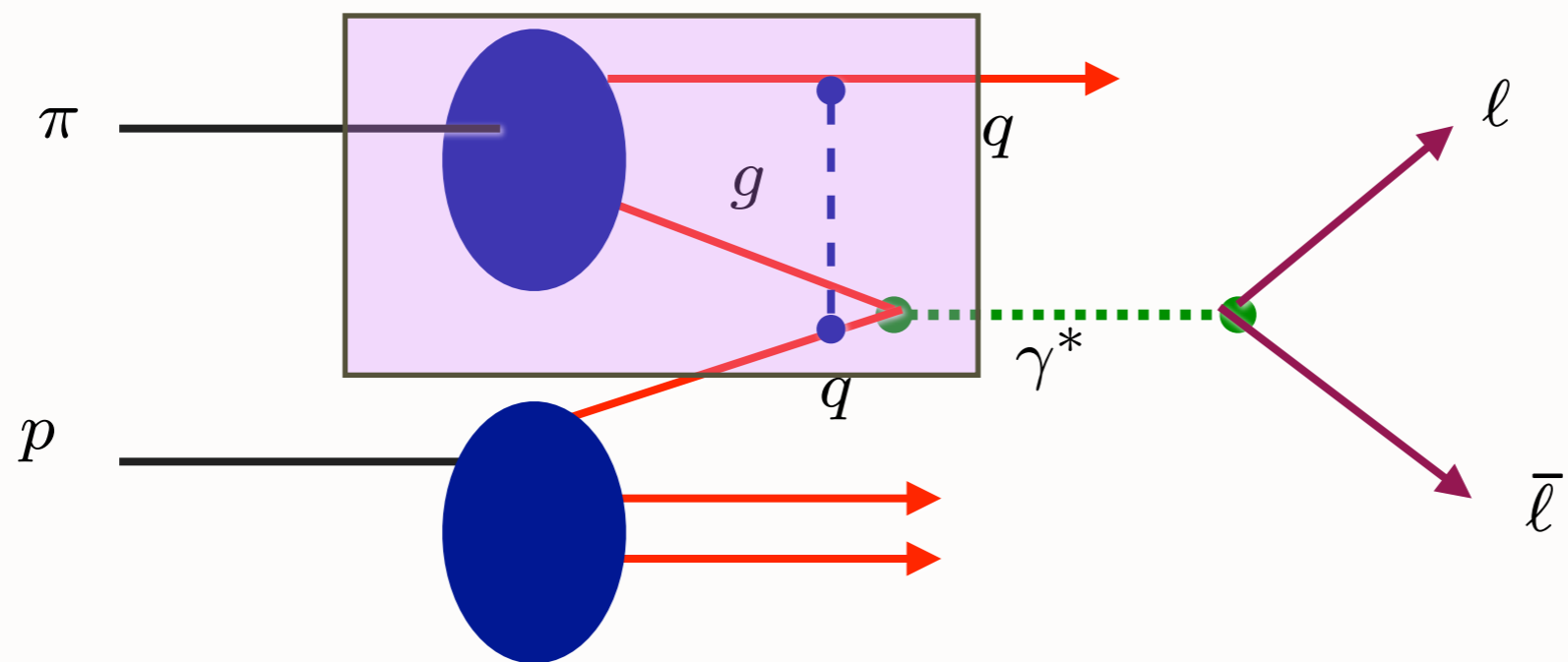
**Hot Topics in QCD Phenomenology  
101**

**Stan Brodsky**





$$\pi q \rightarrow \gamma^* q$$



**Initial State Interaction**

***Pion appears directly in subprocess at large  $x_F$***   
*All of the pion's momentum is transferred to the lepton pair*  
*Lepton Pair is produced longitudinally polarized*

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

*sum over states with  $n=3, 4, \dots$  constituents*

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

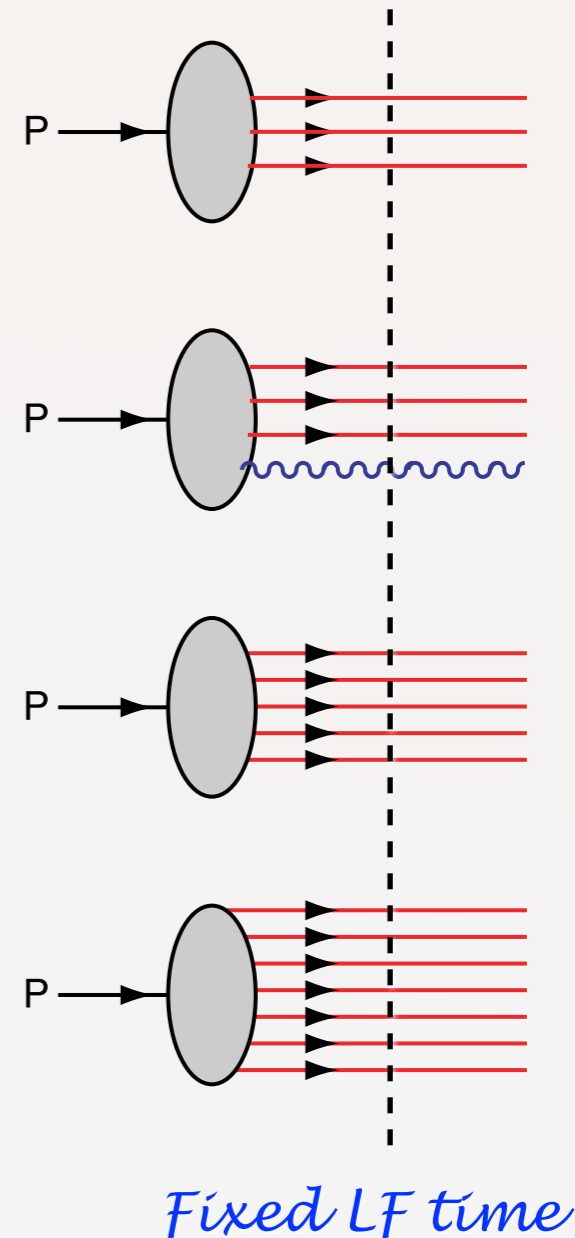
are boost invariant; they are independent of the hadron's energy and momentum  $P^\mu$ .

The light-cone momentum fraction

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_i^\perp = \vec{0}^\perp.$$



*Intrinsic heavy quarks*  
 **$c(x), b(x)$  at high  $x$ !**

$$\bar{s}(x) \neq s(x)$$

$$\bar{u}(x) \neq \bar{d}(x)$$

**Mueller: gluon Fock states**      **BFKL Pomeron**

*Crucial Test of Leading -Twist QCD:  
Scaling at fixed  $x_T$*

$$E \frac{d\sigma}{d^3p} (pp \rightarrow H X) = \frac{F(x_T, \theta_{cm})}{p_T^{n_{\text{eff}}}} \quad x_T = \frac{2p_T}{\sqrt{s}}$$

**Parton model:  $n_{\text{eff}} = 4$**

**As fundamental as Bjorken scaling in DIS**

**scaling law:  $n_{\text{eff}} = 2 n_{\text{active}} - 4$**



# Dimensional analysis

Scattering amplitude  $1\ 2\ \dots \rightarrow \dots\ n$  has dimension

$$\mathcal{M} \sim [\text{length}]^{n-4}$$

## Consequence

In a **conformal** theory (no intrinsic scale), scaling of inclusive particle production

$$E \frac{d\sigma}{d^3p}(A\ B \rightarrow C\ X) \sim \frac{|\mathcal{M}|^2}{s^2} = \frac{F(x_{\perp}, \vartheta^{\text{cm}})}{p_{\perp}^{2n_{\text{active}}-4}}$$

where  $n_{\text{active}}$  is the number of fields participating to the hard process

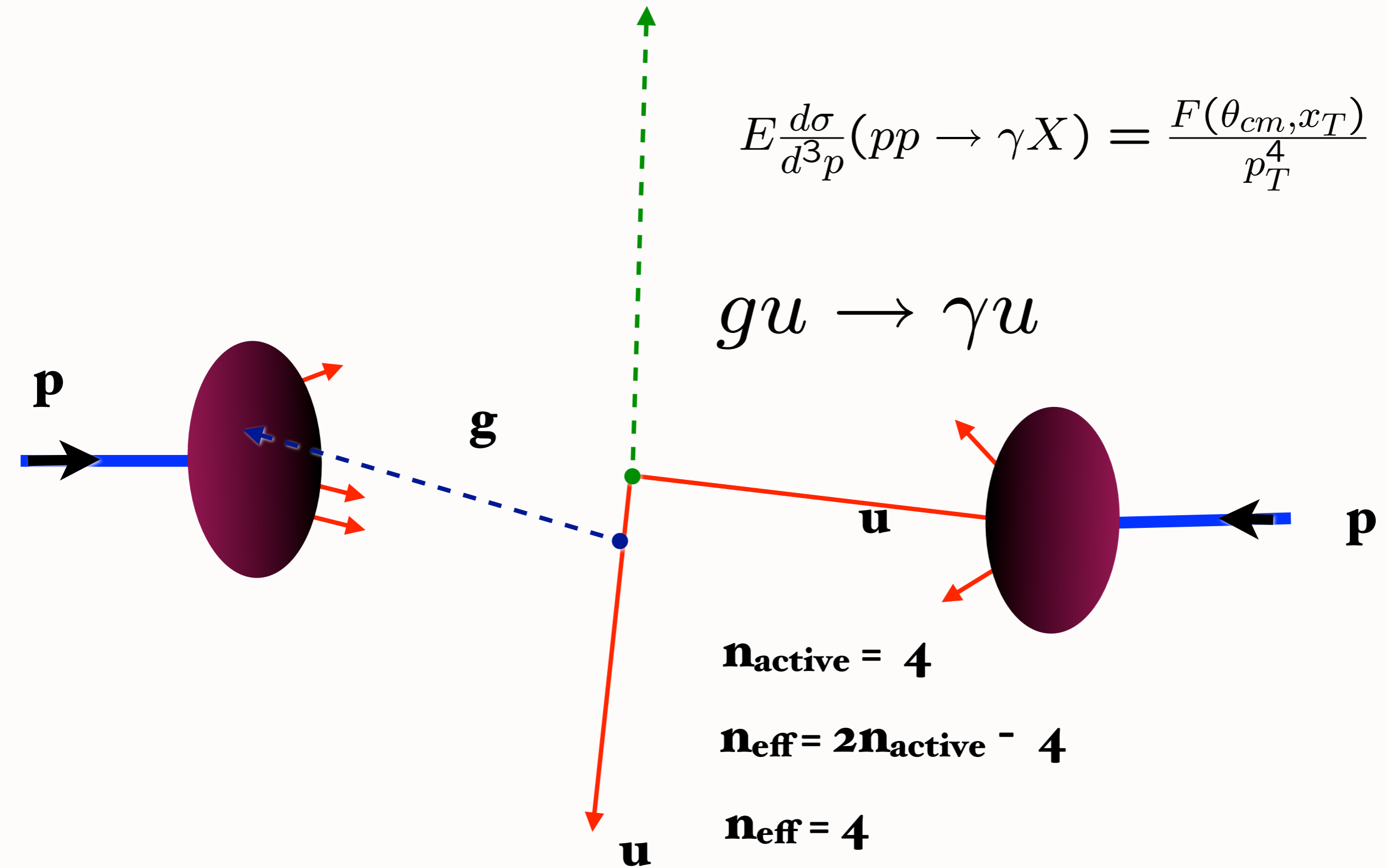
$x_{\perp} = 2p_{\perp}/\sqrt{s}$  and  $\vartheta^{\text{cm}}$ : ratios of invariants

$$n_{\text{active}} = 4 \rightarrow n_{\text{eff}} = 4$$

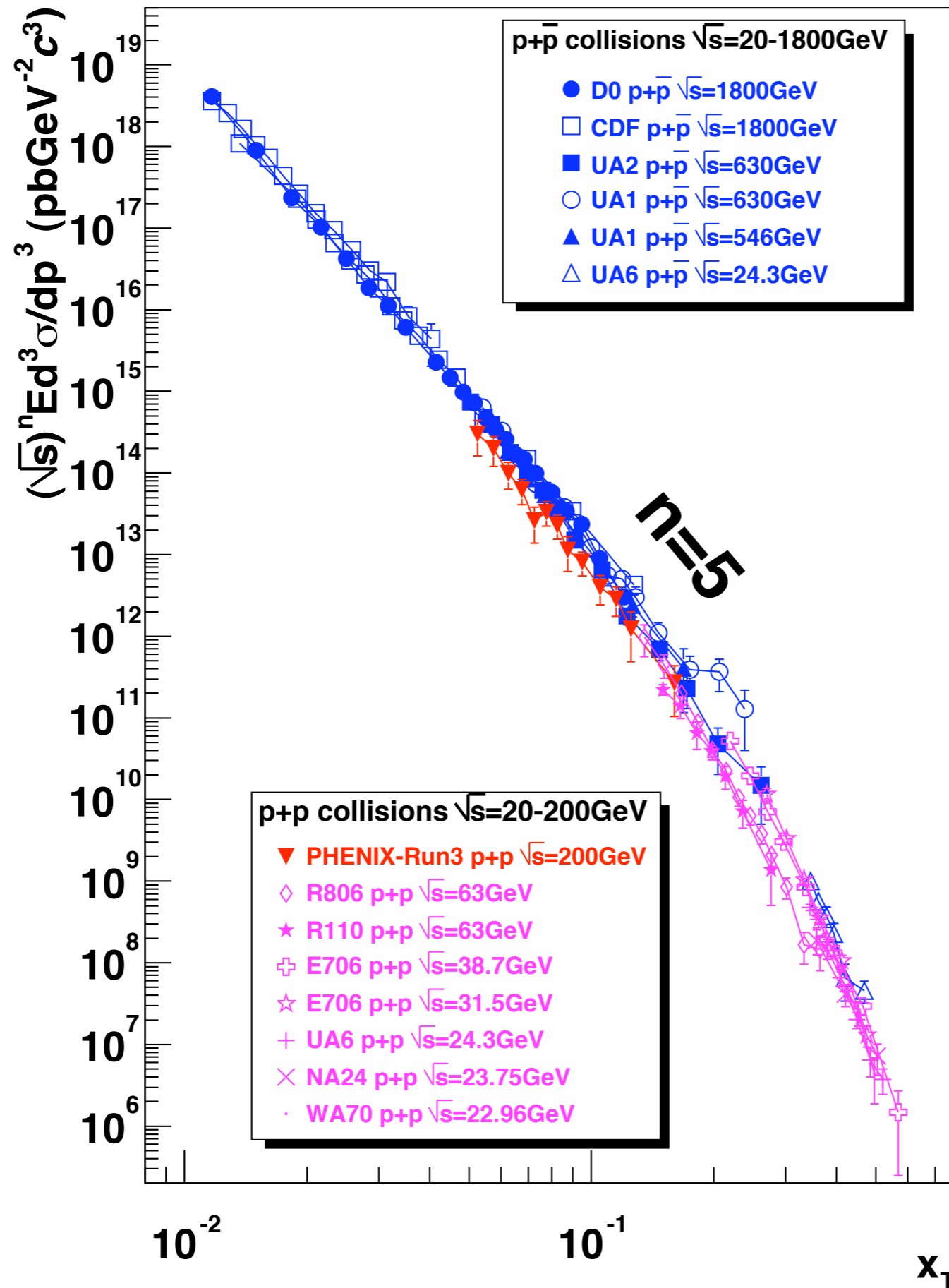
$$pp \rightarrow \gamma X$$

$$E \frac{d\sigma}{d^3p}(pp \rightarrow \gamma X) = \frac{F(\theta_{cm}, x_T)}{p_T^4}$$

$$gu \rightarrow \gamma u$$



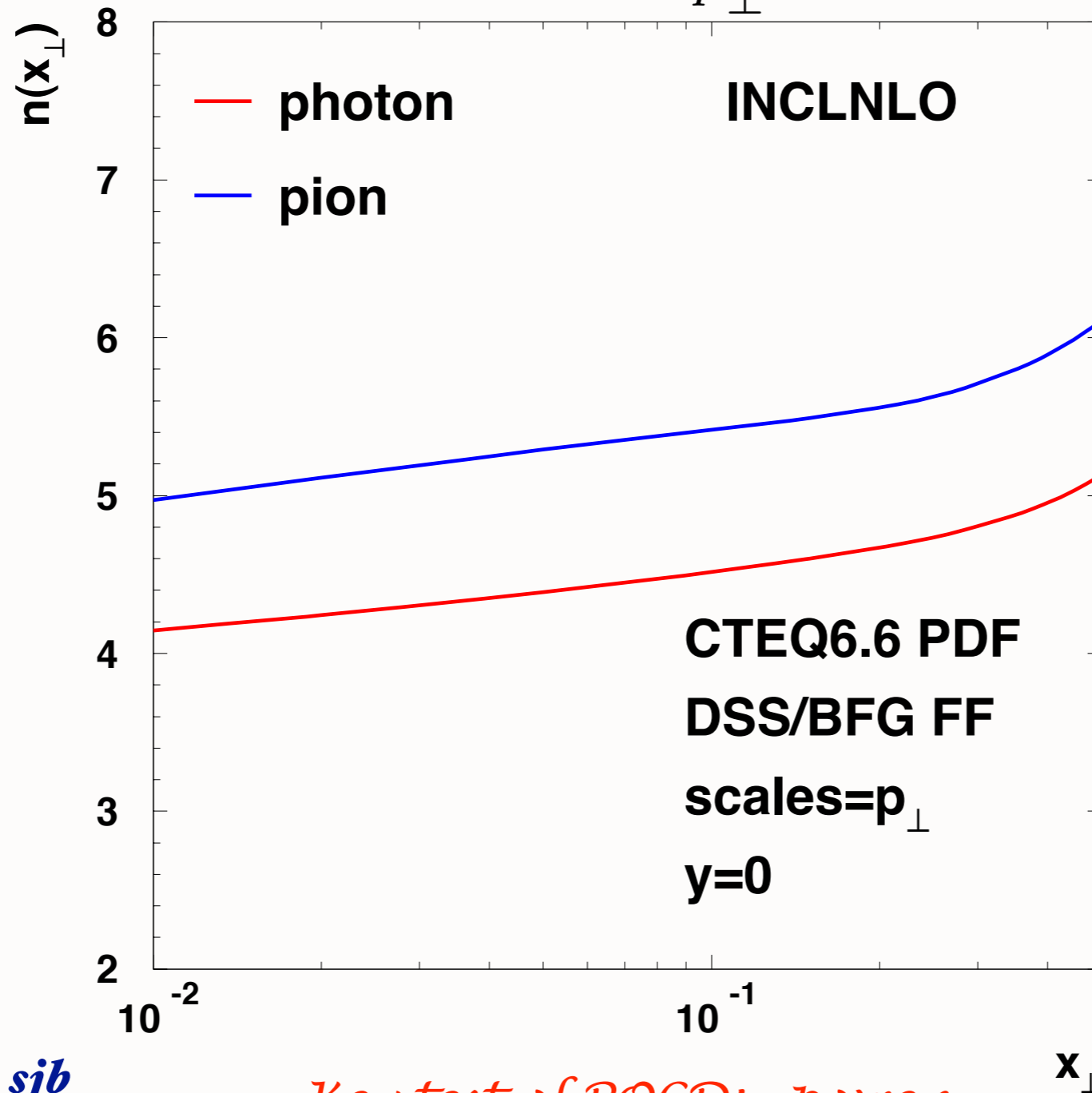
$$\sqrt{s}^n E \frac{d\sigma}{d^3p} (pp \rightarrow \gamma X) \text{ at fixed } x_T$$



**$x_T$ -scaling of direct  
photon production:  
consistent with  
PQCD**

*QCD prediction: Modification of power fall-off due to DGLAP evolution and the Running Coupling*

$$\frac{d\sigma}{d^3p/E} = \frac{F(x_{\perp}, y)}{p_{\perp}^{n(x_{\perp})}}$$



$$pp \rightarrow \pi X$$

$$pp \rightarrow \gamma X$$

$$5 < p_{\perp} < 20 \text{ GeV}$$

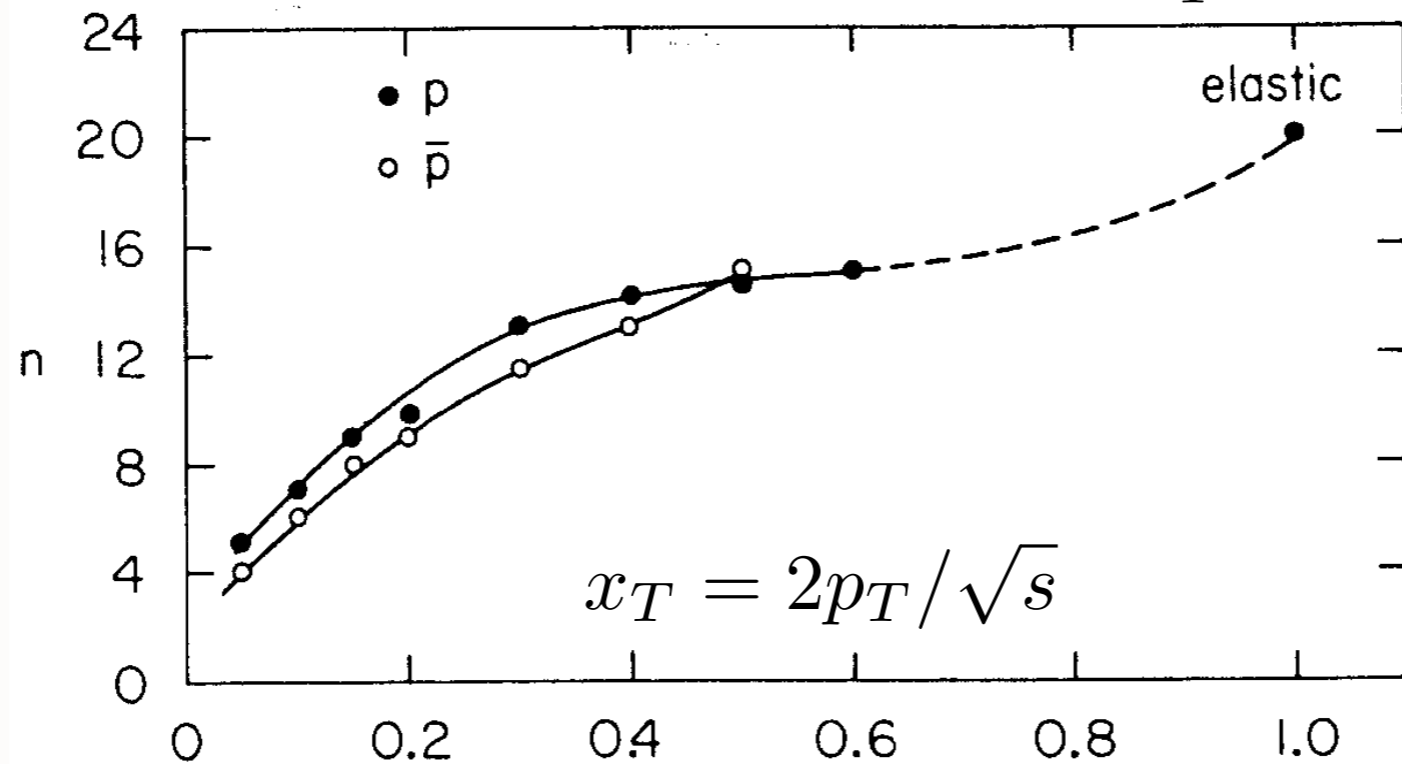
$$70 \text{ GeV} < \sqrt{s} < 4 \text{ TeV}$$

*Arleo,  
Hwang, Sickles, sjb*

*Pirner, Raufeisen, sjb*

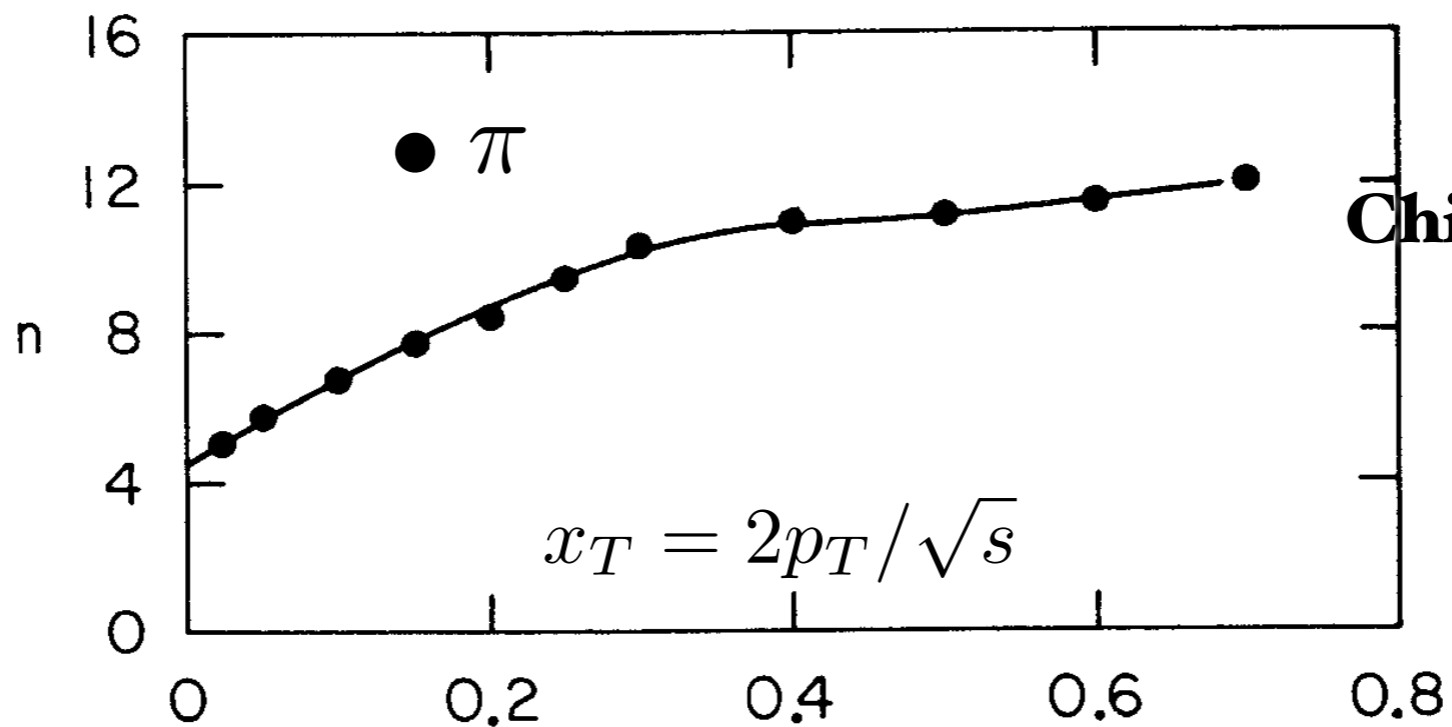
*Key test of PQCD: power-law fall-off at fixed  $x_{\perp}$*

$$E \frac{d\sigma}{d^3p}(pp \rightarrow HX) = \frac{F(x_T, \theta_{cm} = \pi/2)}{p_T^n}$$



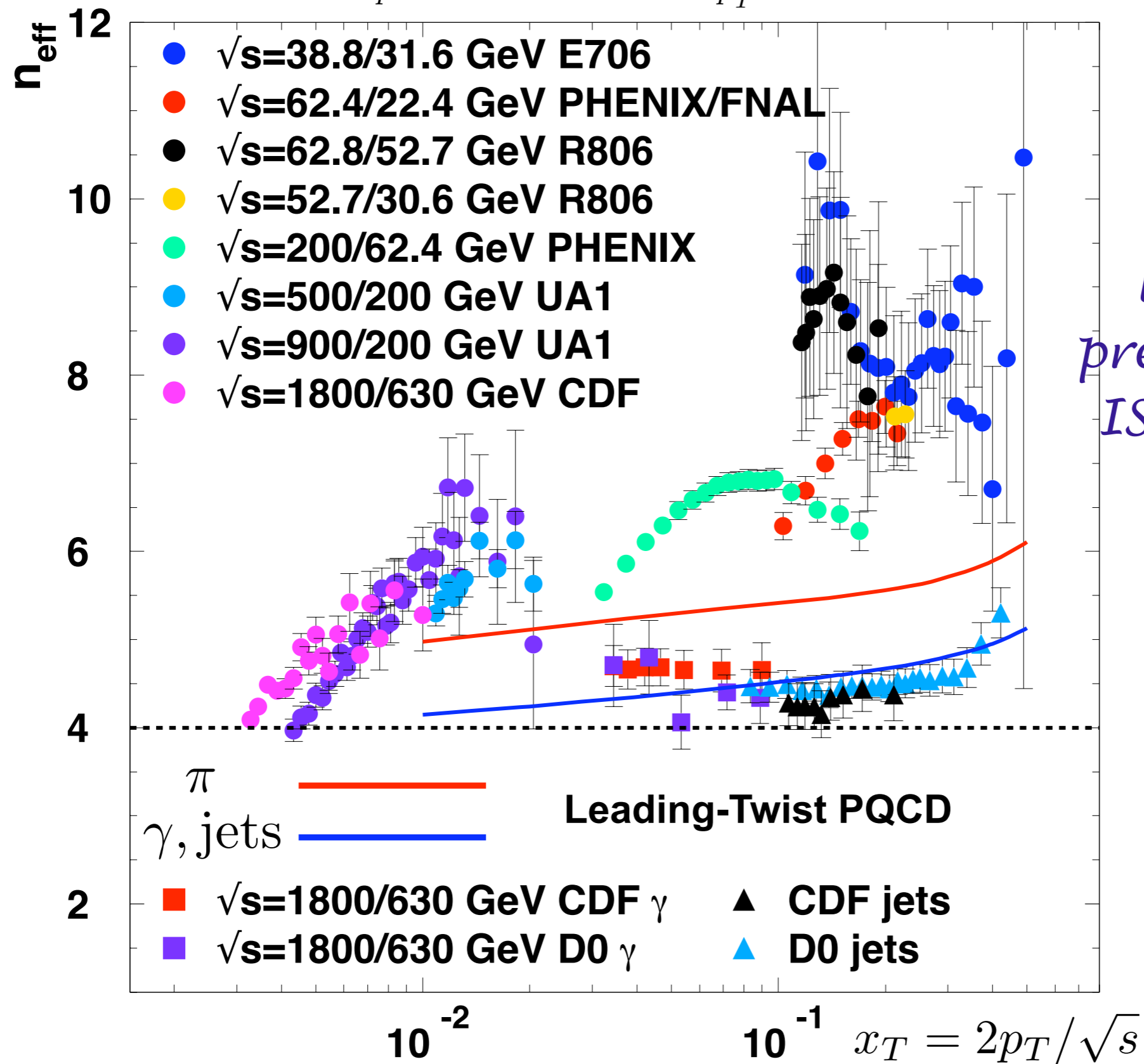
*Clear evidence for  
higher-twist  
contributions*

**J. W. Cronin, SSI 1974**



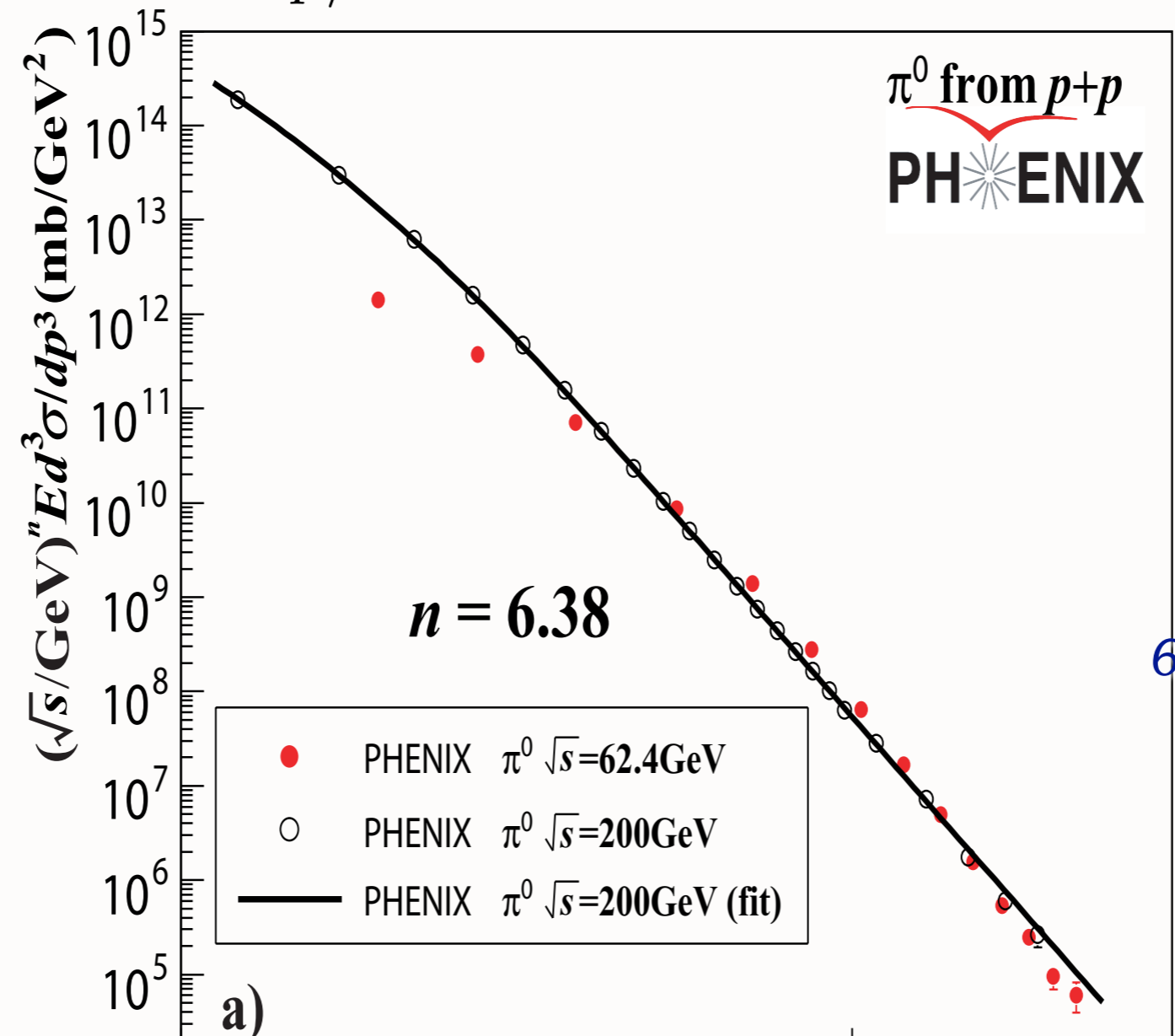
**Chicago-Princeton FNA**

$$E \frac{d\sigma}{d^3p}(pp \rightarrow HX) = \frac{F(x_T, \theta_{CM} = \pi/2)}{p_T^{n_{\text{eff}}}}$$



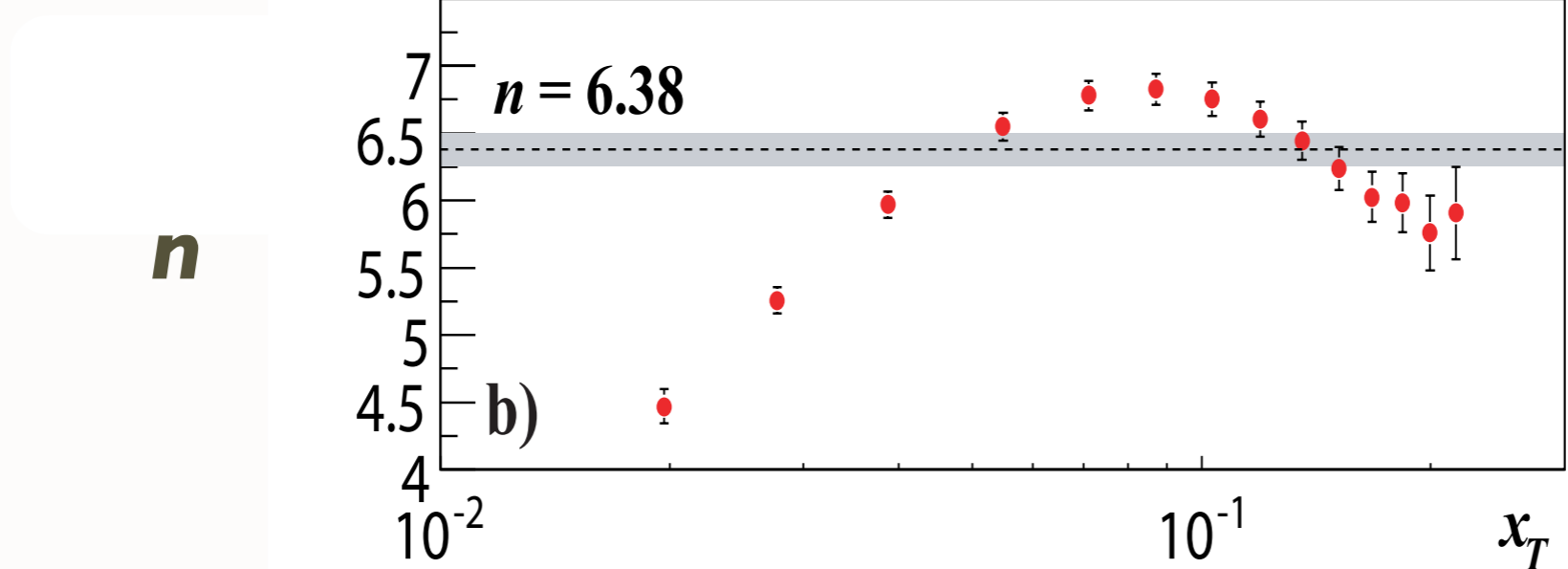
*Leading-twist prediction fails at ISR, FNAL, RHIC, CDF!*

$$[\sqrt{s}]^n \frac{d\sigma}{d^3p/E} (pp \rightarrow \pi^0 X) \text{ at fixed } x_T = \frac{2p_T}{\sqrt{s}}$$



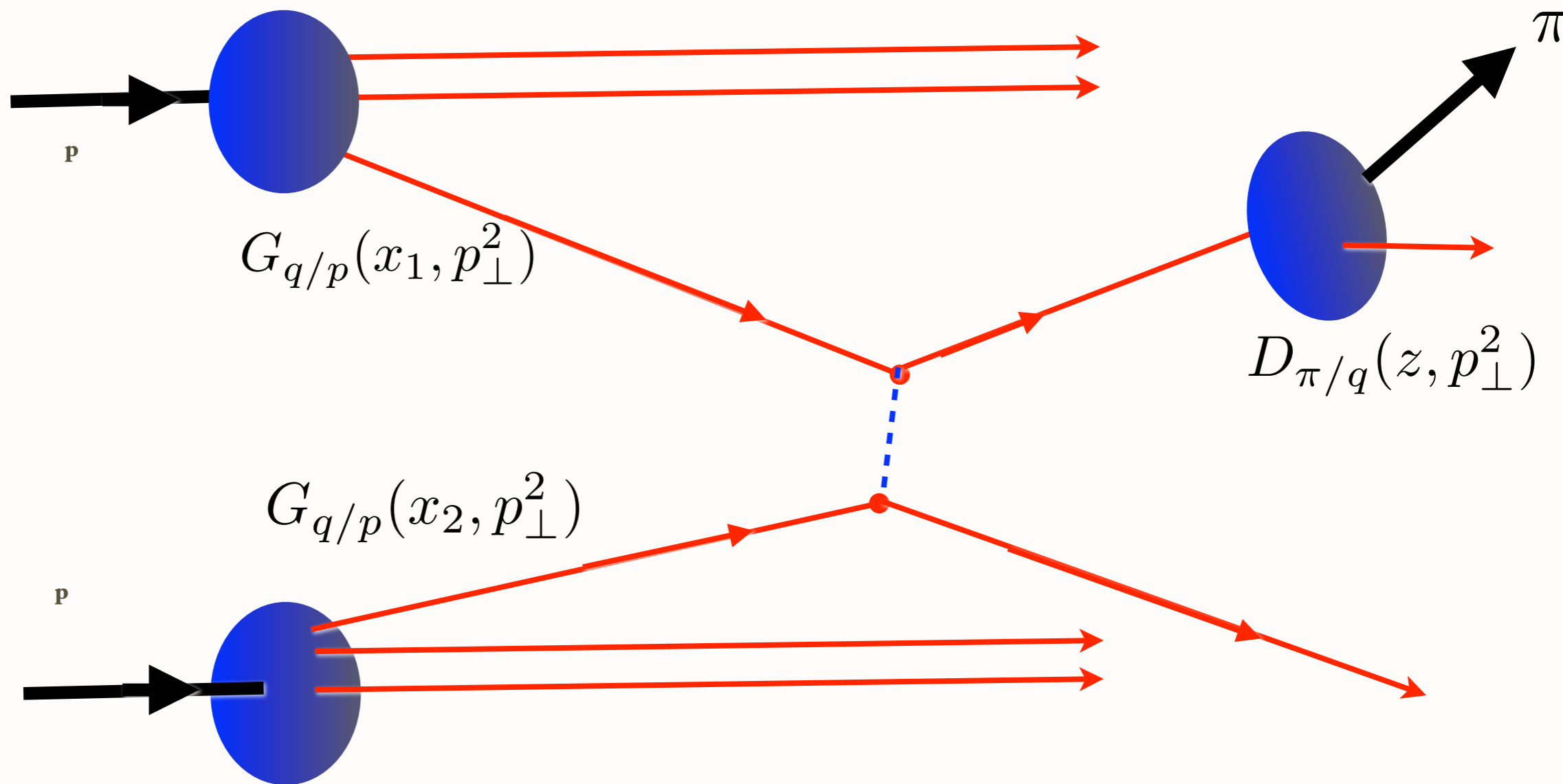
M. J.  
Tannenbaum

PHENIX  
62.4 and 200 GeV data



**n**

# Leading-Twist Contribution to Hadron Production

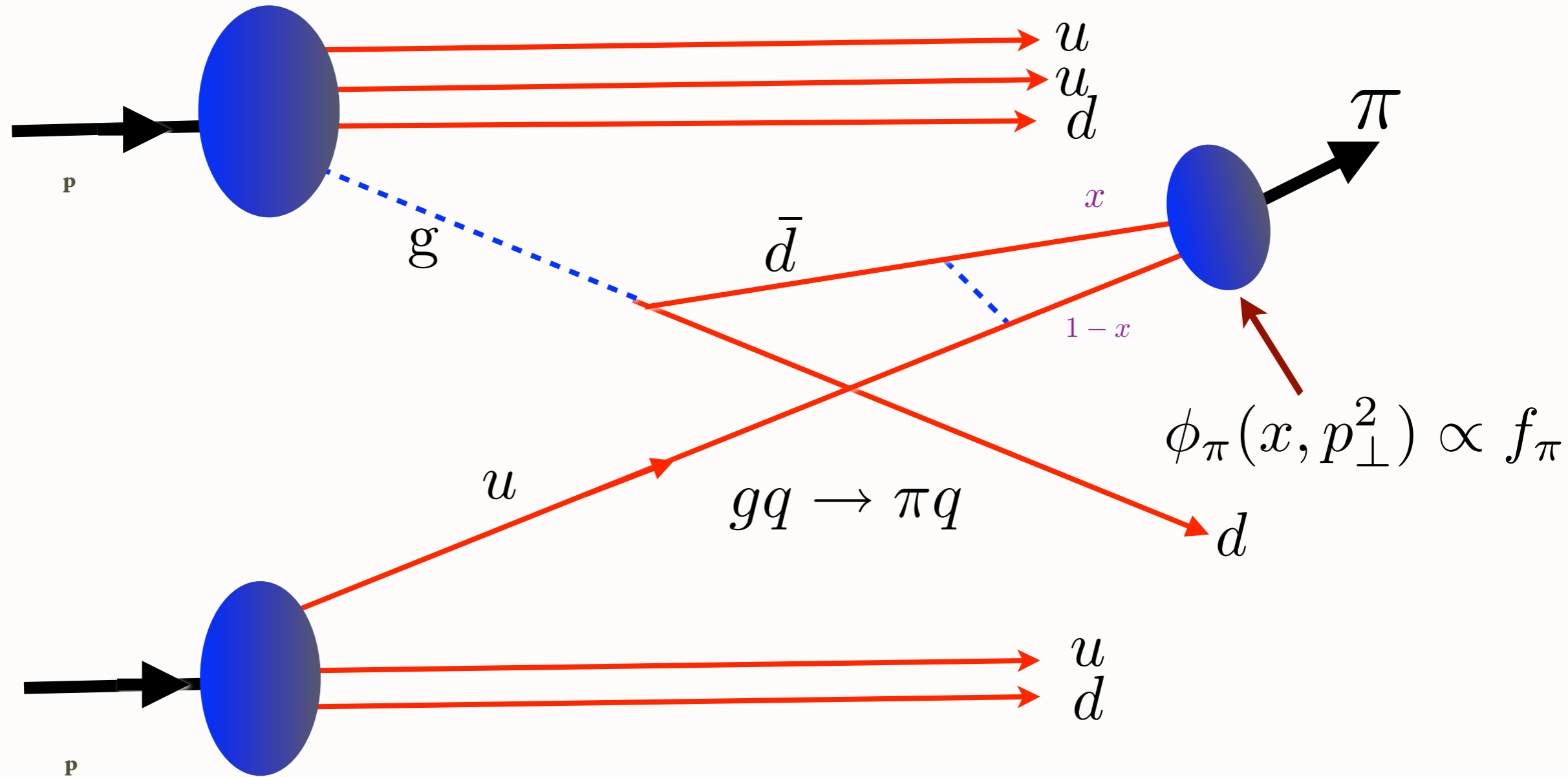


*Parton model and  
Conformal Scaling:*

$$\frac{d\sigma}{d^3 p / E} = \alpha_s^2 \frac{F(x_{\perp}, y)}{p_{\perp}^4}$$



# Direct Higher-Twist Contribution to Hadron Production



$$\frac{d\sigma}{d^3 p / E} = \alpha_s^3 f_\pi^2 \frac{F(x_\perp, y)}{p_\perp^6}$$

No Fragmentation Function

# Scale dependence

Pion scaling exponent extracted vs.  $p_{\perp}$  at fixed  $x_{\perp}$   
2-component toy-model

$$\sigma^{\text{model}}(pp \rightarrow \pi X) \propto \frac{A(x_{\perp})}{p_{\perp}^4} + \frac{B(x_{\perp})}{p_{\perp}^6}$$

Define effective exponent

$$\begin{aligned} n_{\text{eff}}(x_{\perp}, p_{\perp}, B/A) &\equiv -\frac{\partial \ln \sigma^{\text{model}}}{\partial \ln p_{\perp}} + n^{\text{NLO}}(x_{\perp}, p_{\perp}) - 4 \\ &= \frac{2B/A}{p_{\perp}^2 + B/A} + n^{\text{NLO}}(x_{\perp}, p_{\perp}) \end{aligned}$$

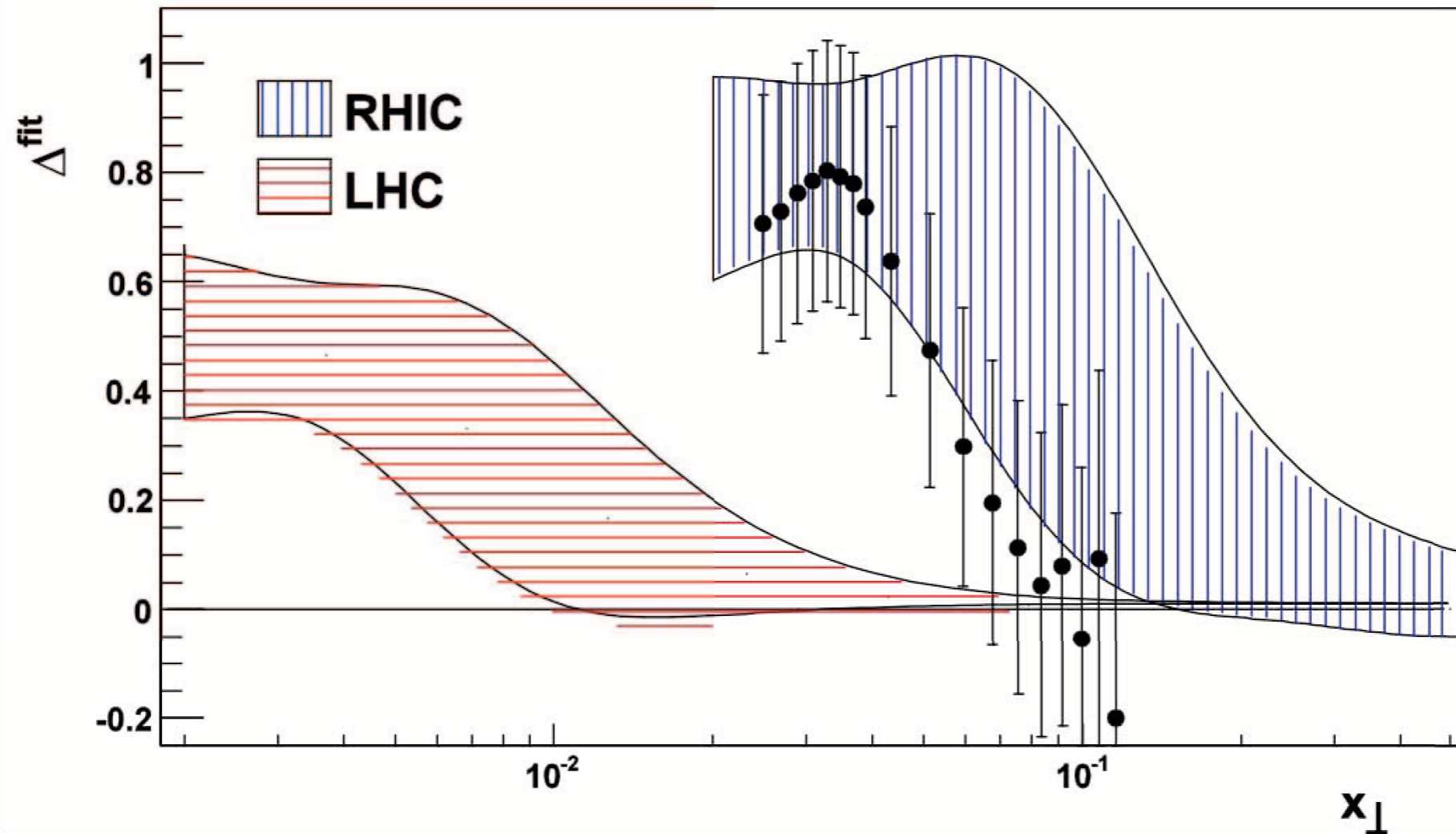
*Arleo, Hwang, Sickles,  
sjb*

# RHIC/LHC predictions

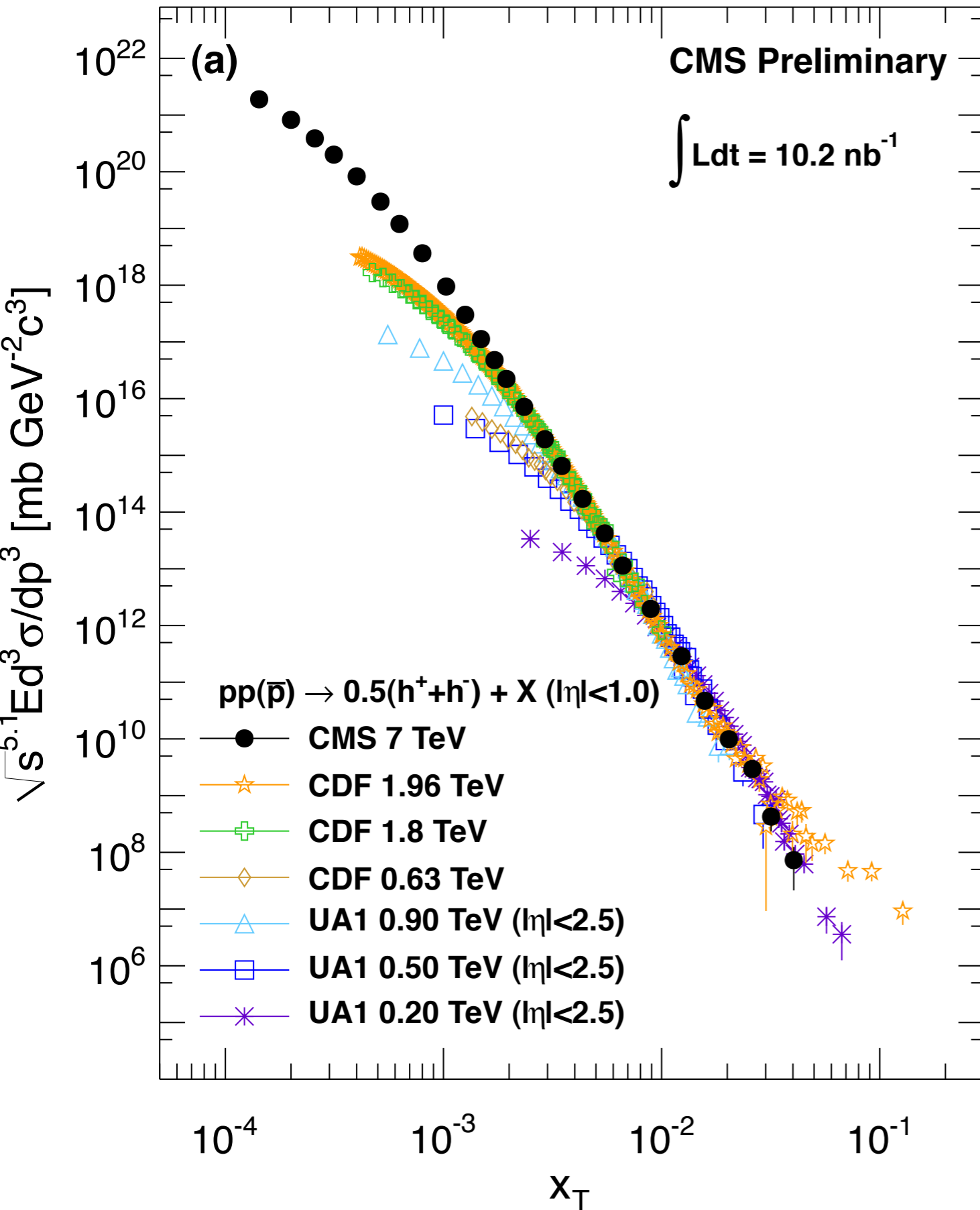
## PHENIX results

Scaling exponents from  $\sqrt{s} = 500$  GeV preliminary data

[ A. Bezilevsky, APS Meeting



- Magnitude of  $\Delta$  and its  $x_{\perp}$ -dependence consistent with predictions



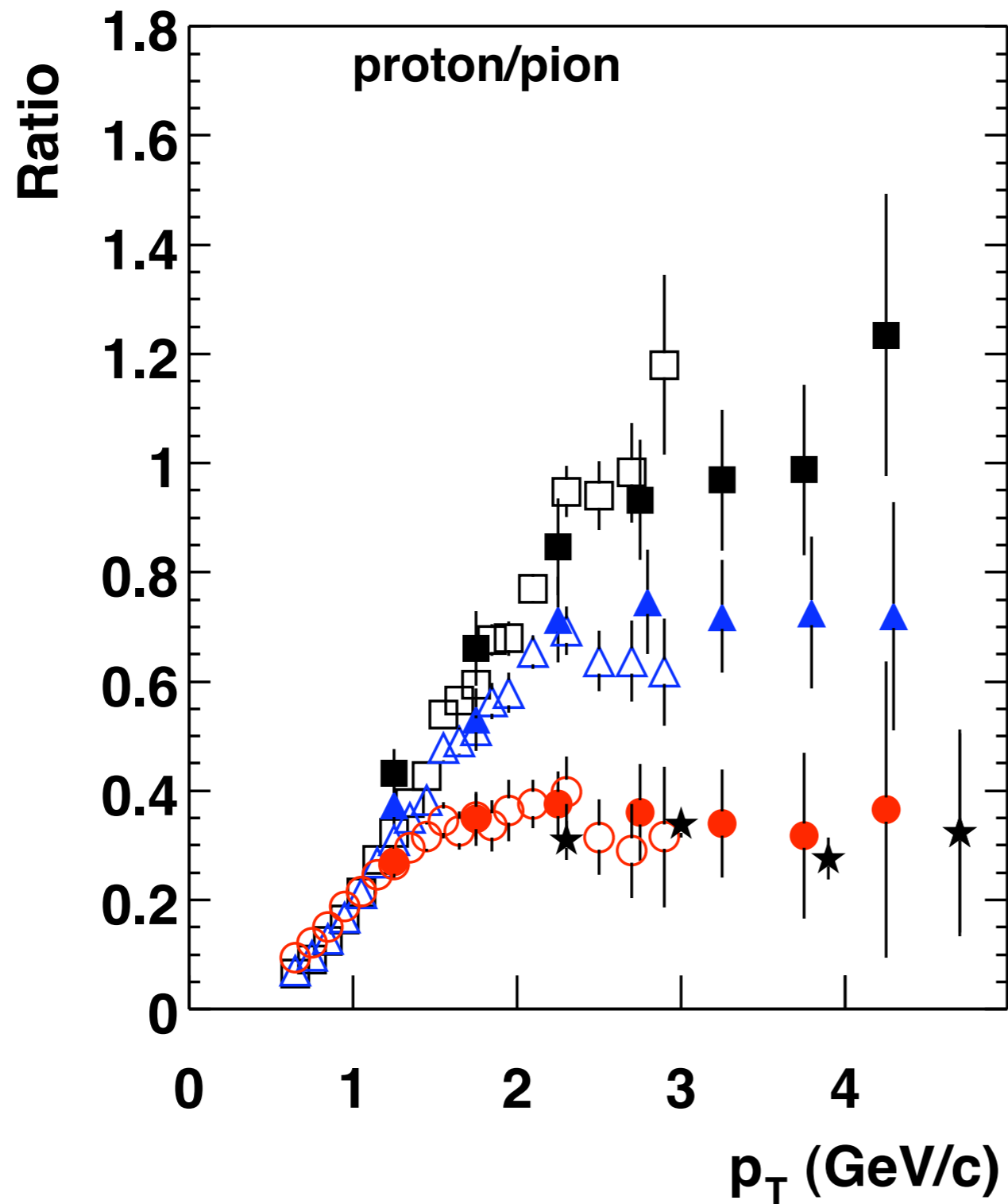
Jet-triggered charged particle transverse momentum spectra in pp collisions at 7 TeV

The CMS Collaboration

$x_T$  scaling fails  
at the LHC

Inclusive invariant cross sections, scaled by  $\sqrt{s}^{5.1}$

*Particle ratio changes with centrality!*



*Protons less absorbed  
in nuclear collisions than pions  
because of  
color-transparent higher-twist process*

← **Central**

- ■ Au+Au 0-10%
- △ ▲ Au+Au 20-30%
- ● Au+Au 60-92%
- ★ p+p,  $\sqrt{s} = 53$  GeV, ISR
- e<sup>+</sup>e<sup>-</sup>, gluon jets, DELPHI
- ..... e<sup>+</sup>e<sup>-</sup>, quark jets, DELPHI

← **Peripheral**

*Tannenbaum:  
Baryon Anomaly:*

*Baryon can be made directly within hard subprocess*

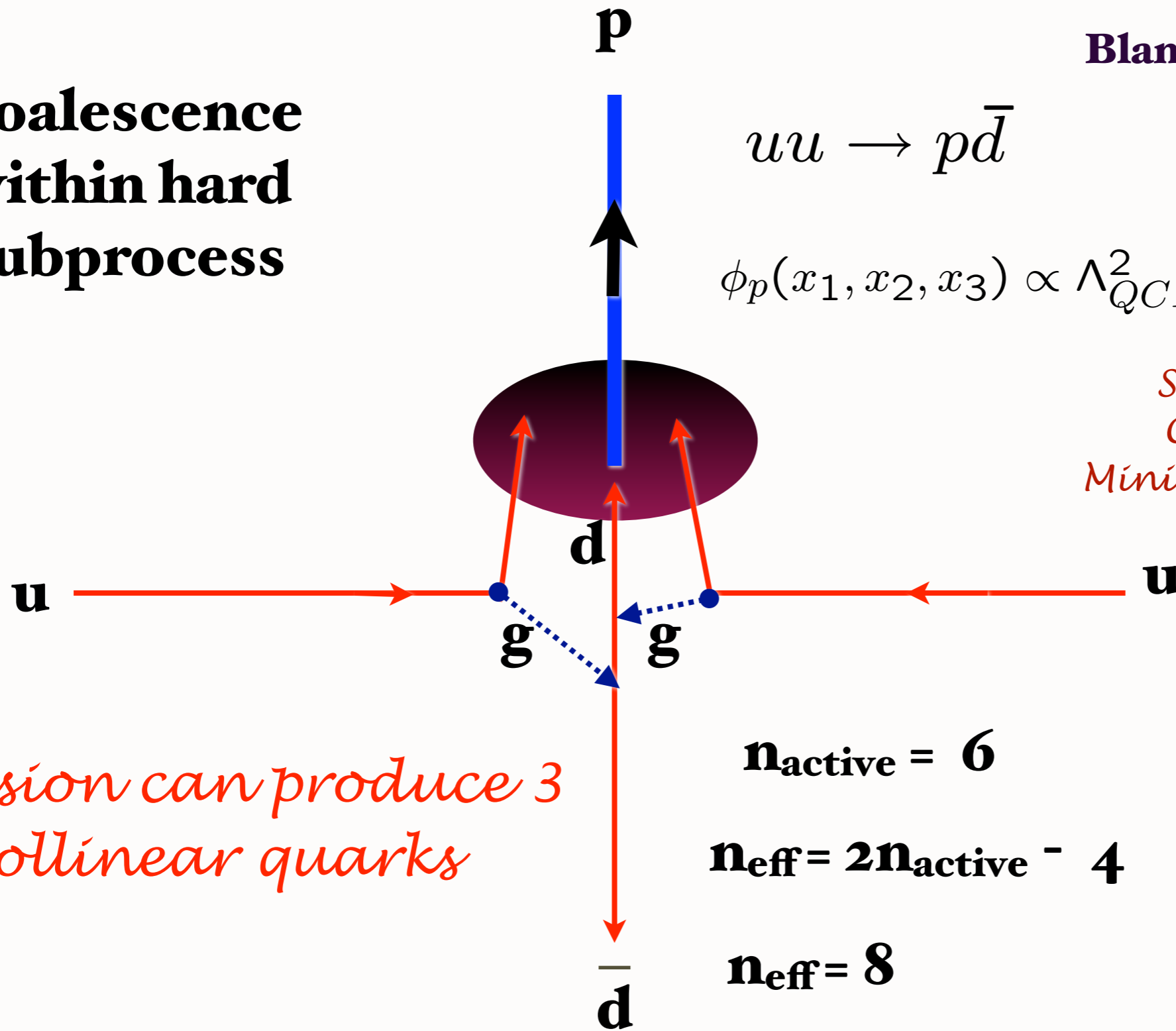
**Coalescence  
within hard  
subprocess**

**Bjorken  
Blankenbecler, Gunion, sjb  
Berger, sjb  
Sickles, Sjb**

$$uu \rightarrow p\bar{d}$$

$$\phi_p(x_1, x_2, x_3) \propto \Lambda_{QCD}^2$$

*Small color-singlet  
Color Transparent  
Minimal same-side energy*



*Collision can produce 3  
collinear quarks*

$$\mathbf{n}_{\text{active}} = 6$$

$$\mathbf{n}_{\text{eff}} = 2\mathbf{n}_{\text{active}} - 4$$

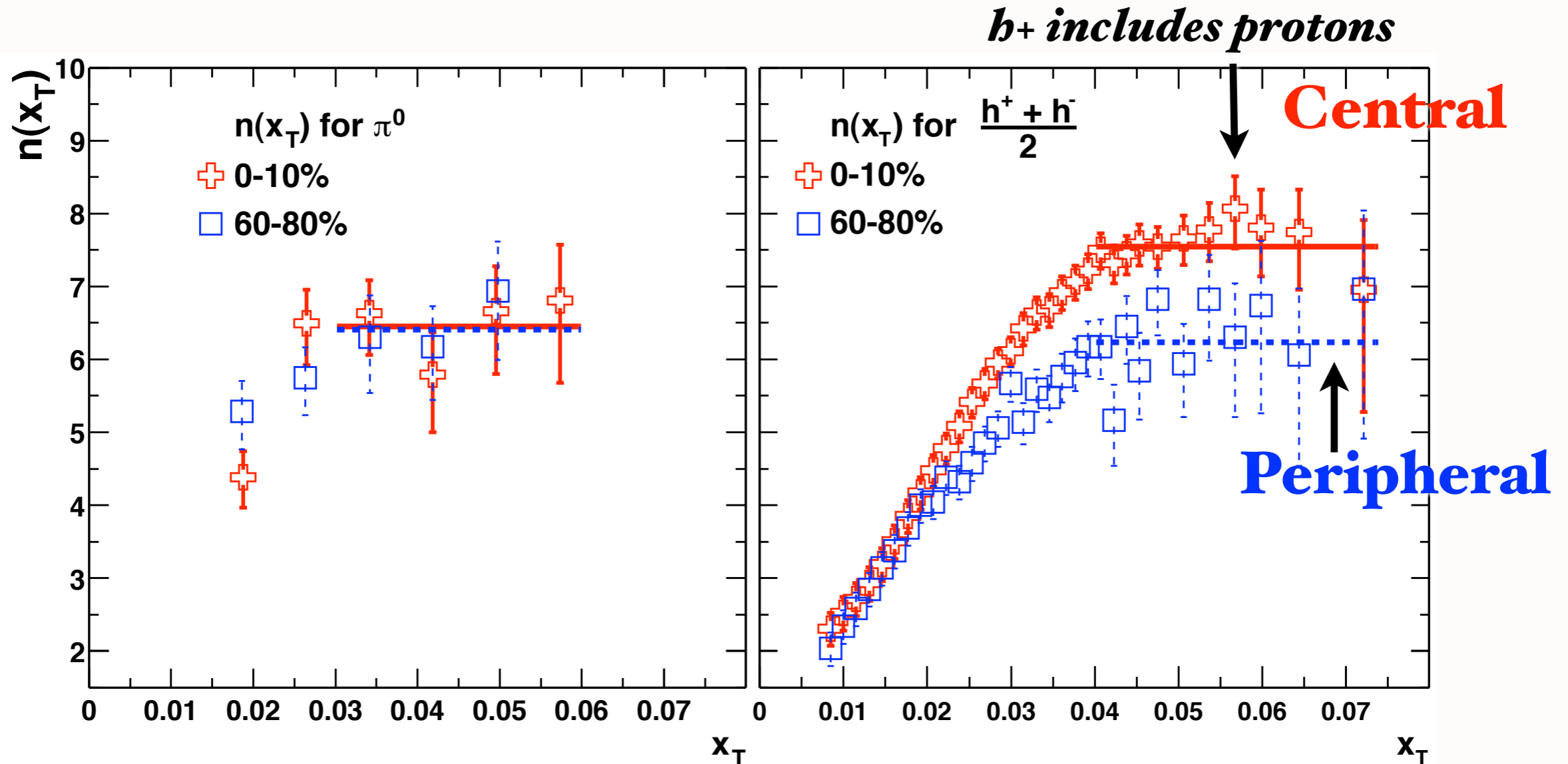
$$\mathbf{n}_{\text{eff}} = 8$$

$$qq \rightarrow B\bar{q}$$

*Arleo, Hwang, Sickles, sjb*

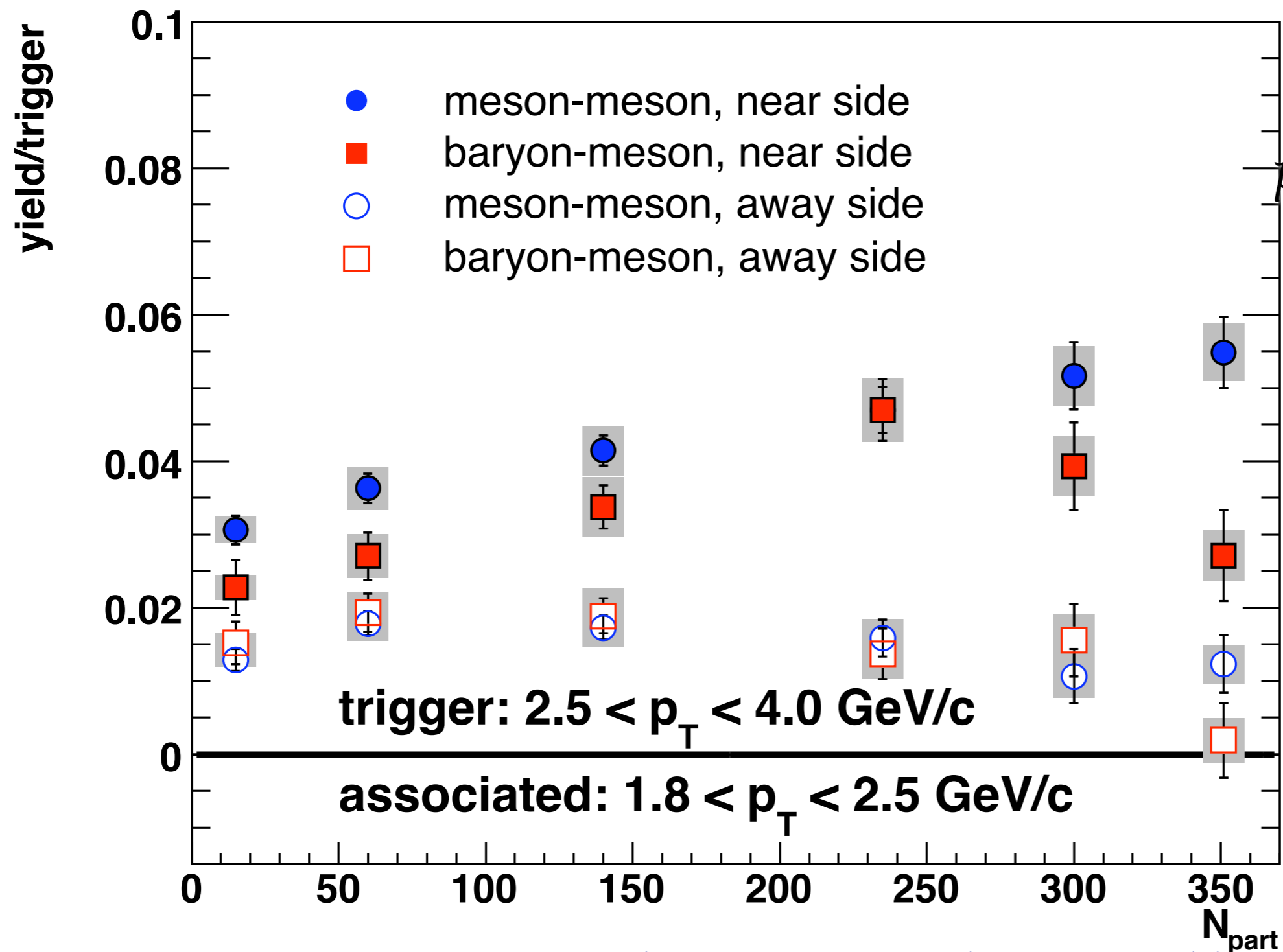
Power-law exponent  $n(x_T)$  for  $\pi^0$  and  $h$  spectra in central and peripheral Au+Au collisions at  $\sqrt{s_{NN}} = 130$  and 200 GeV

S. S. Adler, *et al.*, PHENIX Collaboration, *Phys. Rev. C* **69**, 034910 (2004) [nucl-ex/0308006].



*Proton power changes with centrality !*

*Proton production dominated by color-transparent direct high  $n_{eff}$  subprocesses*



*proton trigger:  
# same-side  
particles *decreases*  
with centrality*



**Proton production more dominated by  
color-transparent direct high- $n_{eff}$  subprocesses**

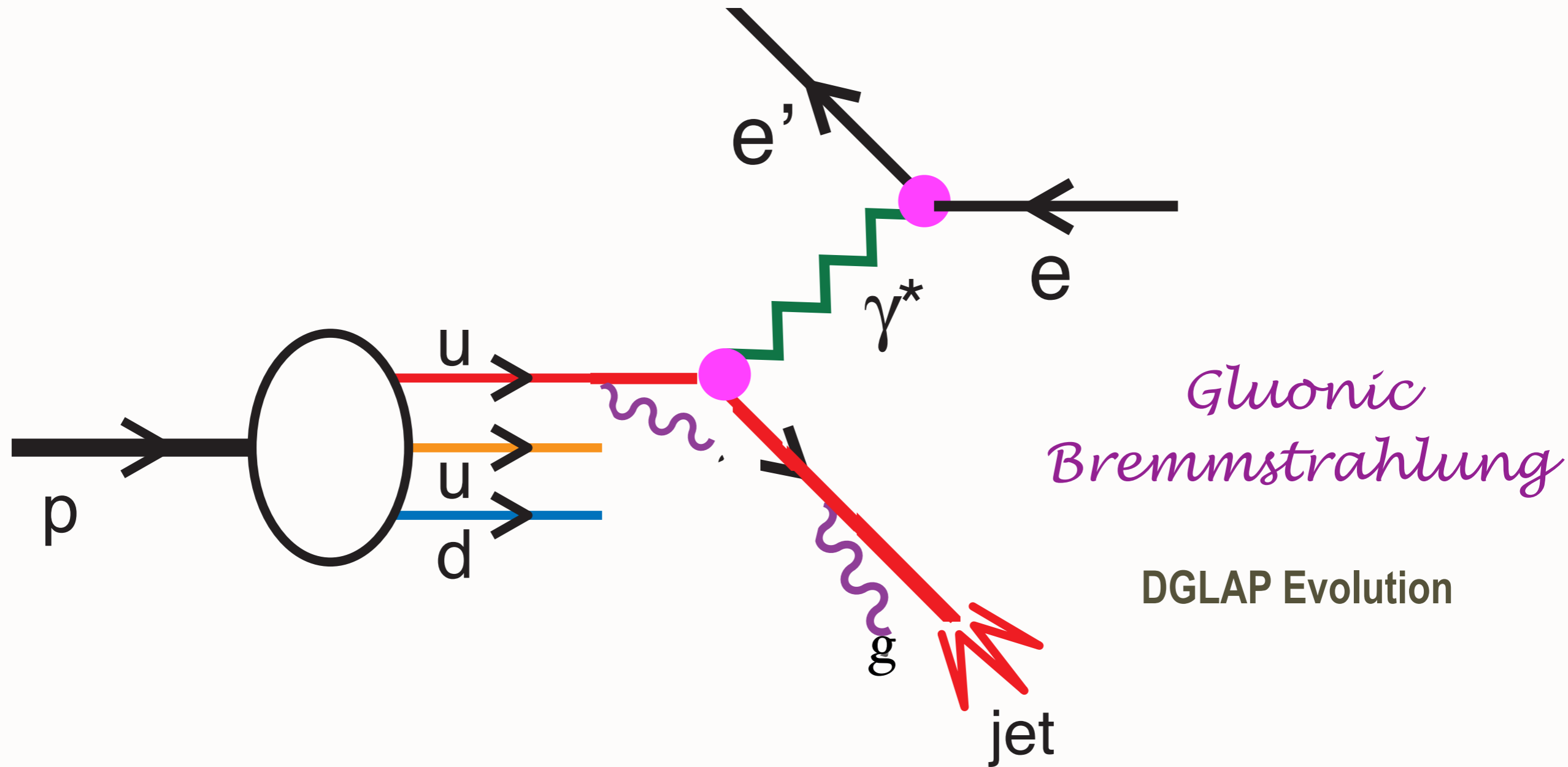


# *Evidence for Direct, Higher-Twist Subprocesses*

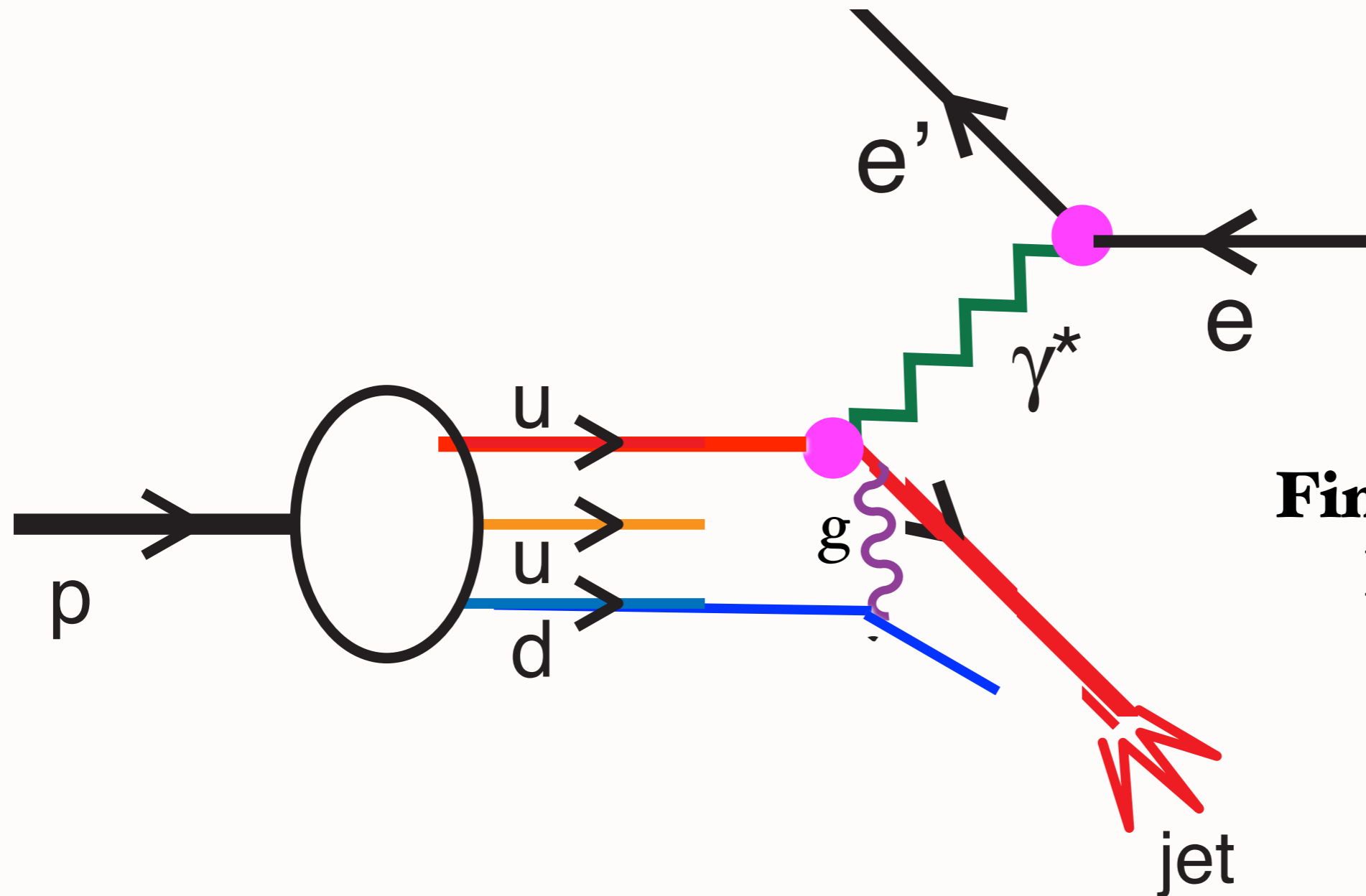
- **Explains anomalous power behavior at fixed  $x_T$**
- **Protons more likely to come from direct higher-twist subprocess than pions**
- **Protons less absorbed than pions in central nuclear collisions because of color transparency**
- **Predicts increasing proton to pion ratio in central collisions** *Baryon Anomaly Explained*
- **Proton power  $n_{\text{eff}}$  increases with centrality since leading twist contribution absorbed**
- **Fewer same-side hadrons for proton trigger at high centrality**
- **Exclusive-inclusive connection at  $x_T = 1$**

*Arleo, Hwang, Sickles, sjb*

# Deep Inelastic Electron-Proton Scattering



# Deep Inelastic Electron-Proton Scattering



**Final-State QCD  
Interaction**

*Conventional wisdom:  
Final-state interactions of struck quark can be neglected*

*Single-spin asymmetries*

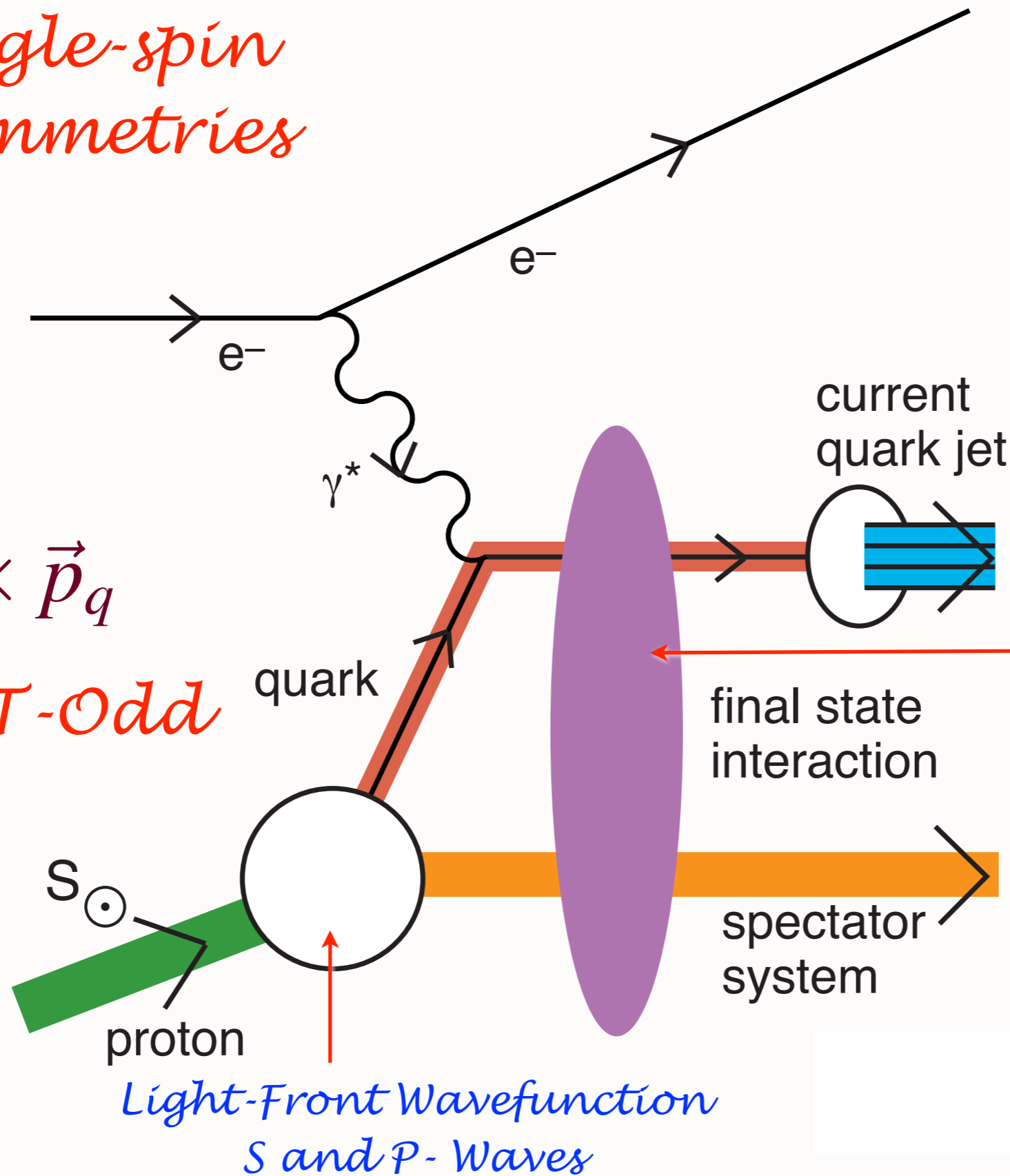
**Leading Twist  
Sivers Effect**

Dae Sung Hwang, Ivan Schmidt, sjb

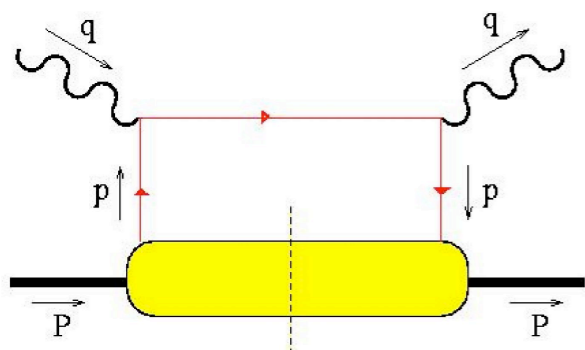
$i \vec{S}_p \cdot \vec{q} \times \vec{p}_q$   
*Pseudo-T-Odd*

*QCD S- and P-Coulomb Phases  
--Wilson Line*

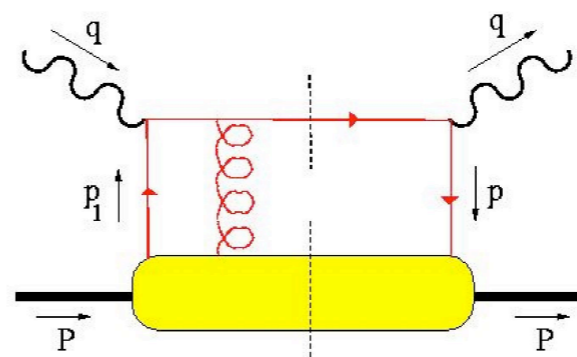
*Leading-Twist  
Rescattering  
Violates pQCD  
Factorization!*



*Light-Front Wavefunction  
S and P-Waves*



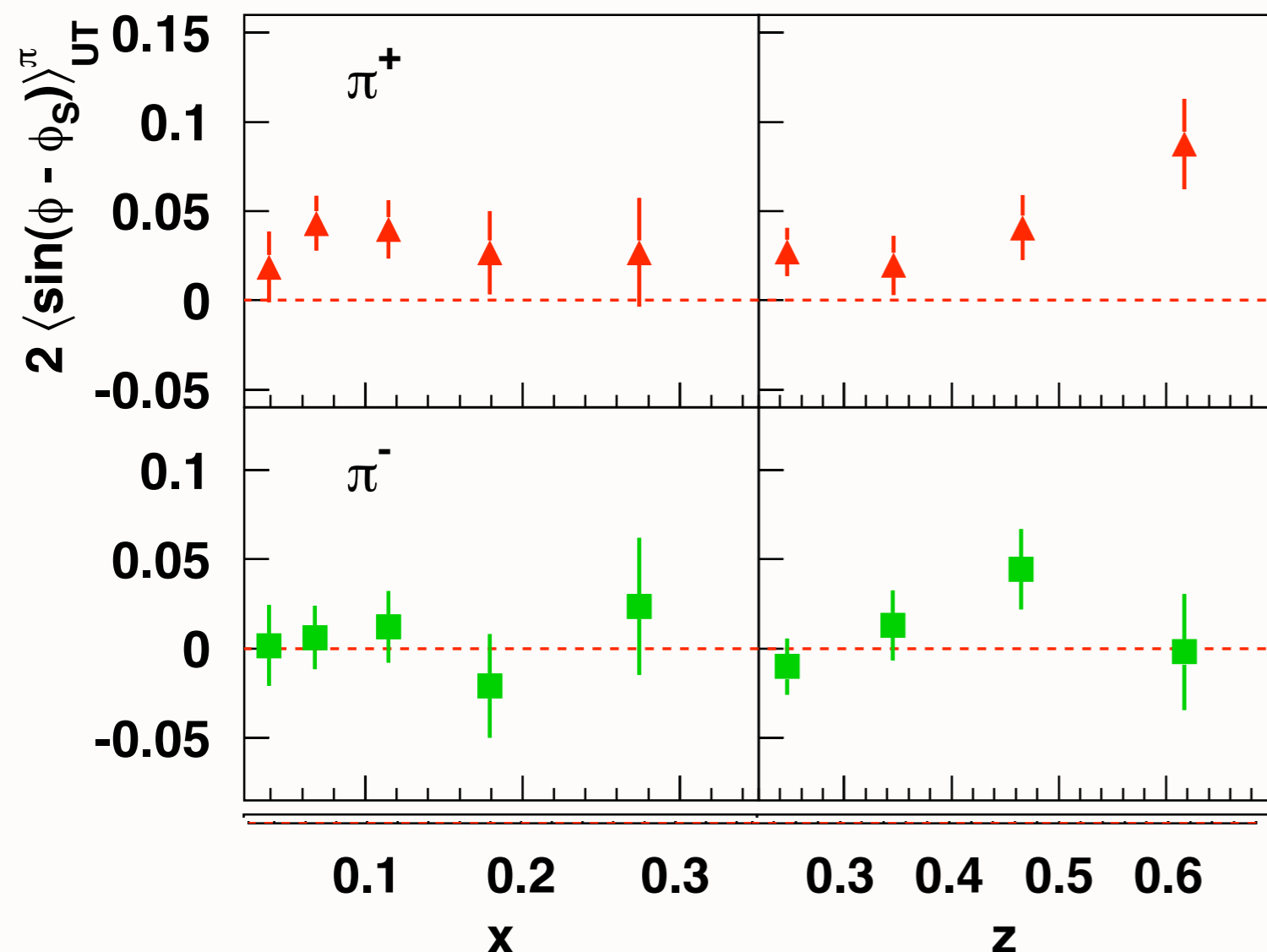
can interfere with



and produce a T-odd effect!  
(also need  $L_z \neq 0$ )

HERMES coll., A. Airapetian et al., Phys. Rev. Lett. 94 (2005) 012002.

## Sivers asymmetry from HERMES

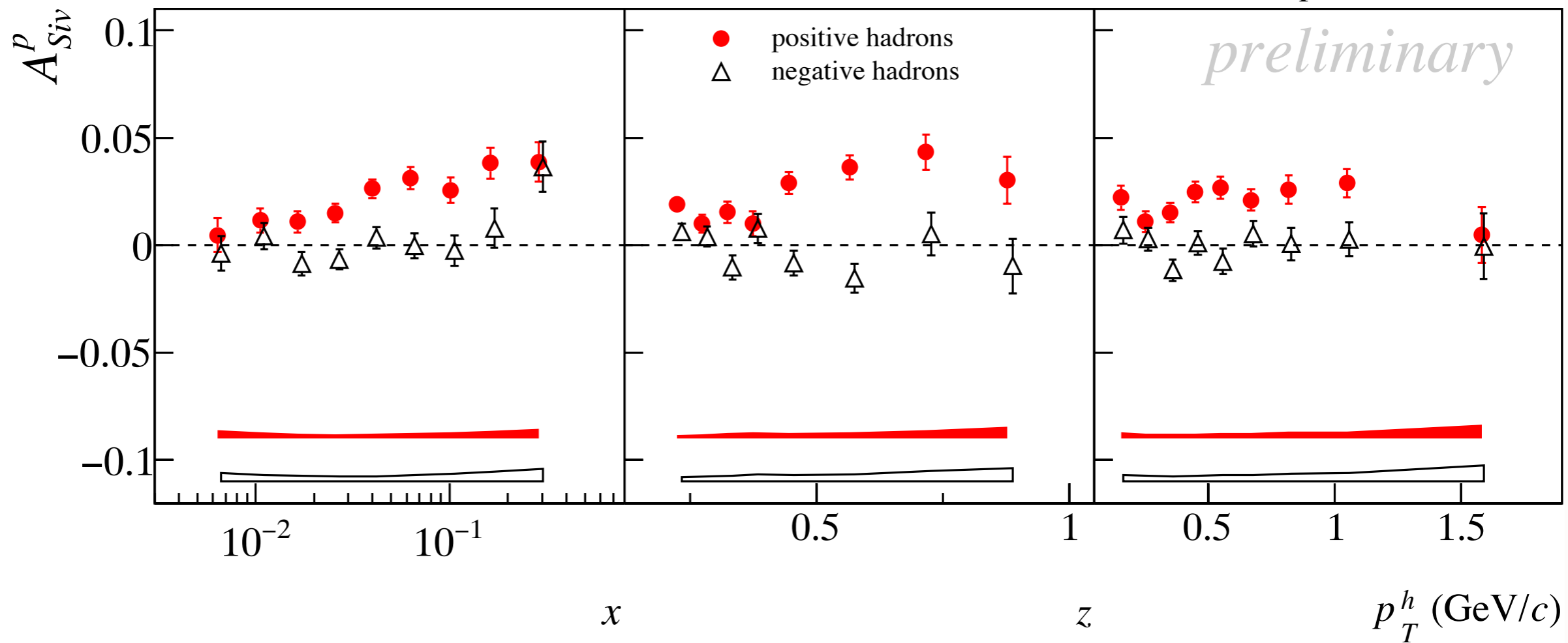


- First evidence for non-zero Sivers function!
- $\Rightarrow$  presence of non-zero quark orbital angular momentum!
- **Positive** for  $\pi^+$  ...
- **Consistent with zero** for  $\pi^-$  ...

**Gamberg:** Hermes data compatible with BHS model

**Schmidt, Lu:**  
*Asymmetry ratios should follow quark contributions to anomalous moment*

COMPASS 2010 proton data

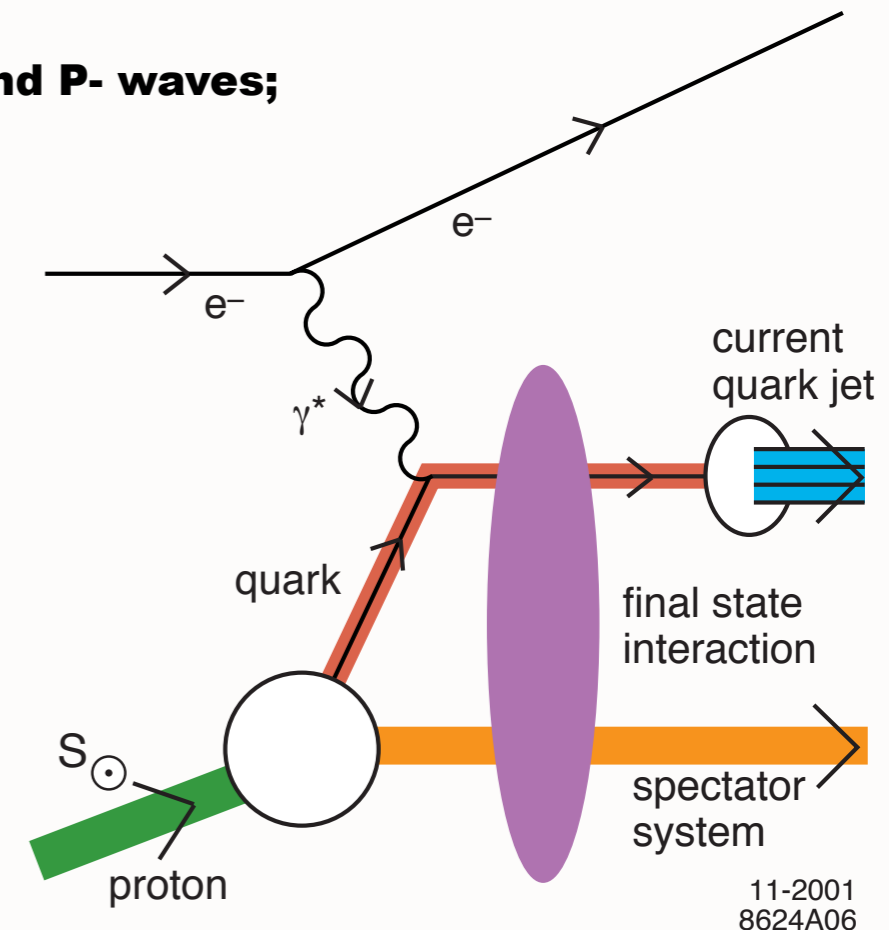


# Final-State Interactions Produce Pseudo T-Odd (Sivers Effect)

Hwang, Schmidt, sjb  
Collins

- **Leading-Twist Bjorken Scaling!**
- **Requires nonzero orbital angular momentum of quark**
- **Arises from the interference of Final-State QCD Coulomb phases in S- and P- waves;**
- **Wilson line effect -- gauge independent**
- **Relate to the quark contribution to the target proton anomalous magnetic moment and final-state QCD phases**
- **QCD phase at soft scale!**
- **New window to QCD coupling and running gluon mass in the IR**
- **QED S and P Coulomb phases infinite -- difference of phases finite!**
- **Alternate: Retarded and Advanced Gauge: Augmented LFWFs**

$$i \vec{S} \cdot \vec{p}_{jet} \times \vec{q}$$



Pasquini, Xiao, Yuan, sjb  
Mulders, Boer Qiu, Sterman

Warsaw  
July 6, 2012

Hot Topics in QCD Phenomenology

127

Stan Brodsky

SLAC  
NATIONAL ACCELERATOR LABORATORY

## Recent COMPASS data on deuteron: small Sivers effect

- The anomalous magnetic moment, the Sivers function, and the generalized parton distribution  $E$  can all be connected to matrix elements involving the orbital angular momentum of the nucleon's constituents.
- The SSA can be generated by either a quark or gluon mechanism, and the isospin structure of the two mechanisms is distinct. The approximate cancellation of the SSA measured on a deuterium target suggests that the gluon mechanism, and thus the orbital angular momentum carried by gluons in the nucleon, is small.
- Studies of the SSA in  $\phi$  or  $K^+K^-$  production, via  $\gamma^*g \rightarrow s\bar{s} \rightarrow \phi + X$  or  $\gamma^*g \rightarrow s\bar{s} \rightarrow K^+K^- + X$  should provide additional constraints on the gluon mechanism.

Gardner, sjb



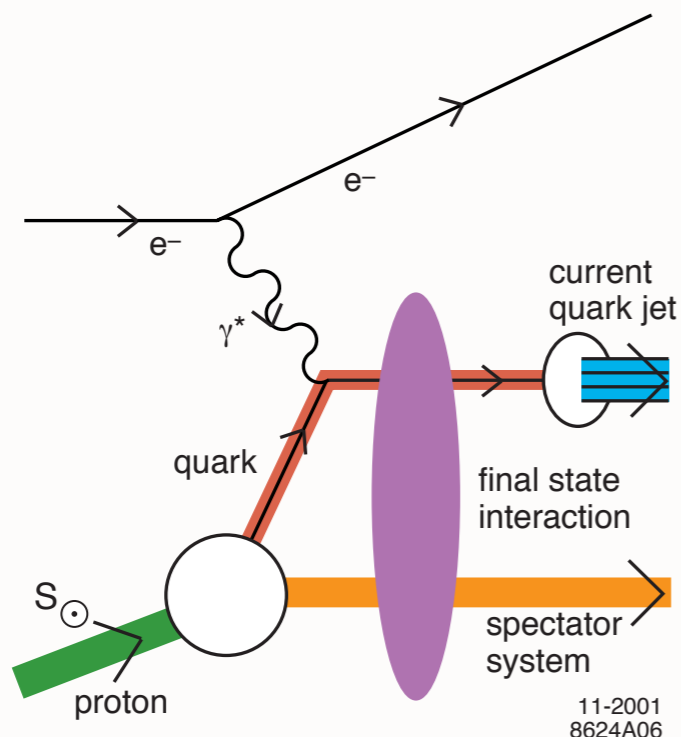
# Connection between the Sivers function and the anomalous magnetic moment

Zhun Lu\* and Ivan Schmidt†

*Departamento de Física, Universidad Técnica Federico, Santa María, Casilla 110-V, Valparaíso, Chile  
and Center of Subatomic Physics, Valparaíso, Chile*

(Received 8 January 2007; revised manuscript received 14 February 2007; published 9 April 2007)

The same light-front wave functions of the proton are involved in both the anomalous magnetic moment of the nucleon and the Sivers function. Using the diquark model, we derive a simple relation between the anomalous magnetic moment and the Sivers function, which should hold in general with good approximation. This relation can be used to provide constraints on the Sivers single spin asymmetries from the data on anomalous magnetic moments. Moreover, the relation can be viewed as a direct connection between the quark orbital angular momentum and the Sivers function.



$$\kappa_p = (2)(2/3)\kappa_{u/p} + (-1/3)\kappa_{d/p},$$

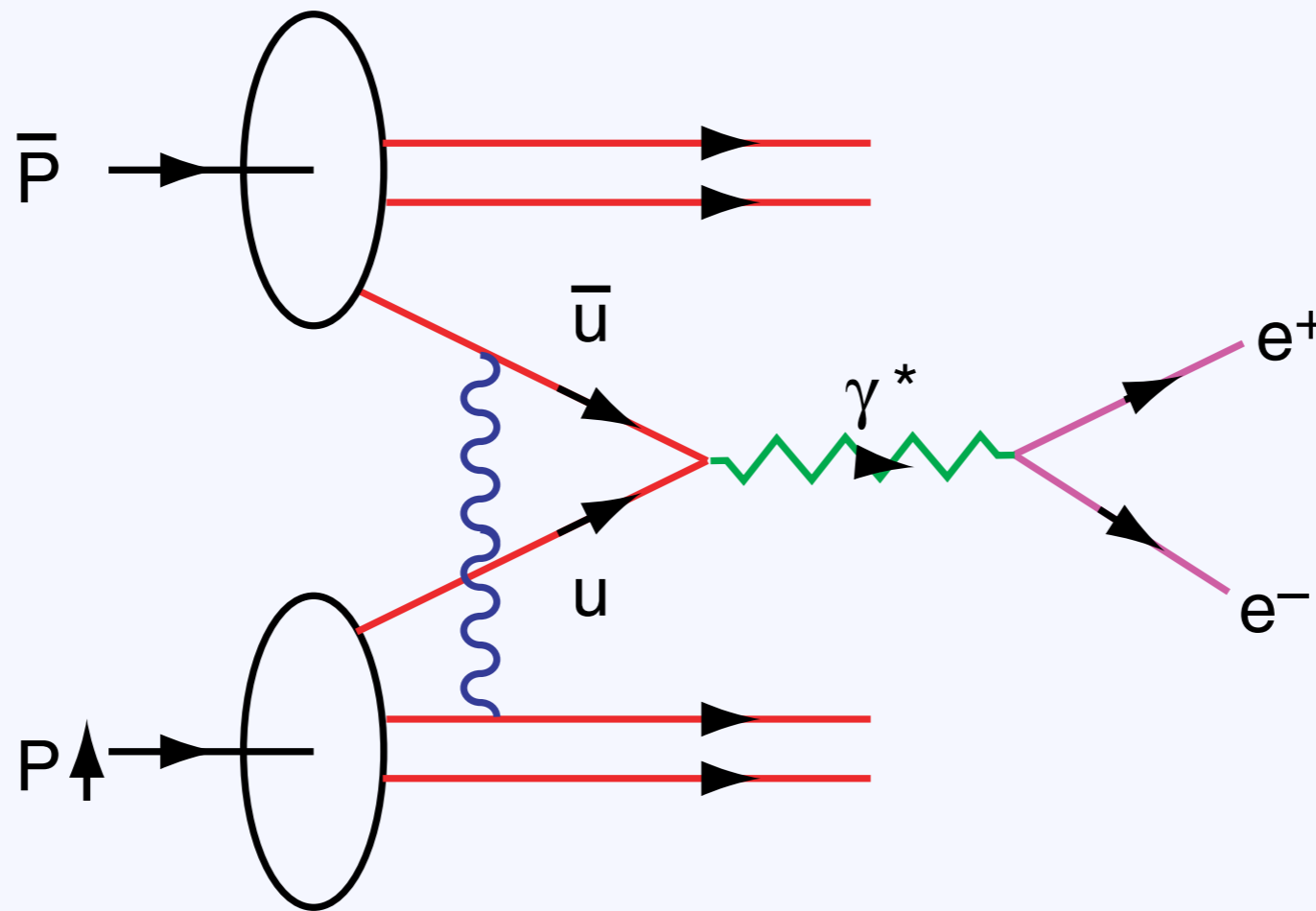
$$\kappa_n = (2)(-1/3)\kappa_{u/p} + (2/3)\kappa_{d/p}.$$

$$\frac{A_{UT}^{\text{Siv}}(\pi^+)}{A_{UT}^{\text{Siv}}(\pi^-)} \approx \frac{2e_u^2 f_{1T}^{\perp u} D_1^{\pi^+/u}}{e_d^2 f_{1T}^{\perp d} D_1^{\pi^-/d}} \approx \frac{2e_u^2 \kappa_u}{e_d^2 \kappa_d} = -3.3.$$

$$\frac{A_{UT}^{\text{Siv}}(\pi^0)}{A_{UT}^{\text{Siv}}(\pi^-)} \approx \frac{2e_u^2 f_{1T}^{\perp u} D_1^{\pi^0/u} + e_d^2 f_{1T}^{\perp d} D_1^{\pi^0/d}}{e_d^2 f_{1T}^{\perp d} D_1^{\pi^-/d}} \approx \frac{2e_u^2 \kappa_u + e_d^2 \kappa_d}{2e_d^2 \kappa_d} = -1.15,$$

$$\frac{A_{UT}^{\text{Siv}}(K^+)}{A_{UT}^{\text{Siv}}(K^0)} \approx \frac{2e_u^2 f_{1T}^{\perp u} D_1^{K^+/u}}{e_d^2 f_{1T}^{\perp d} D_1^{K^0/d}} \approx \frac{4e_u^2 \kappa_u}{e_d^2 \kappa_d} = -6.6.$$

# Predict Opposite Sign SSA in DY !



Collins

Hwang  
Schmidt  
sjb

Single Spin Asymmetry In the Drell Yan Process

$$\vec{S}_p \cdot \vec{p} \times \vec{q}_{\gamma^*}$$

Quarks Interact in the Initial State

Interference of Coulomb Phases for  $S$  and  $P$  states

Produce Single Spin Asymmetry [Siver's Effect] Proportional  
to the Proton Anomalous Moment and  $\alpha_s$ .

Opposite Sign to DIS! No Factorization

Warsaw  
July 6, 2012

Hot Topics in QCD Phenomenology  
130

Stan Brodsky

SLAC  
NATIONAL ACCELERATOR LABORATORY

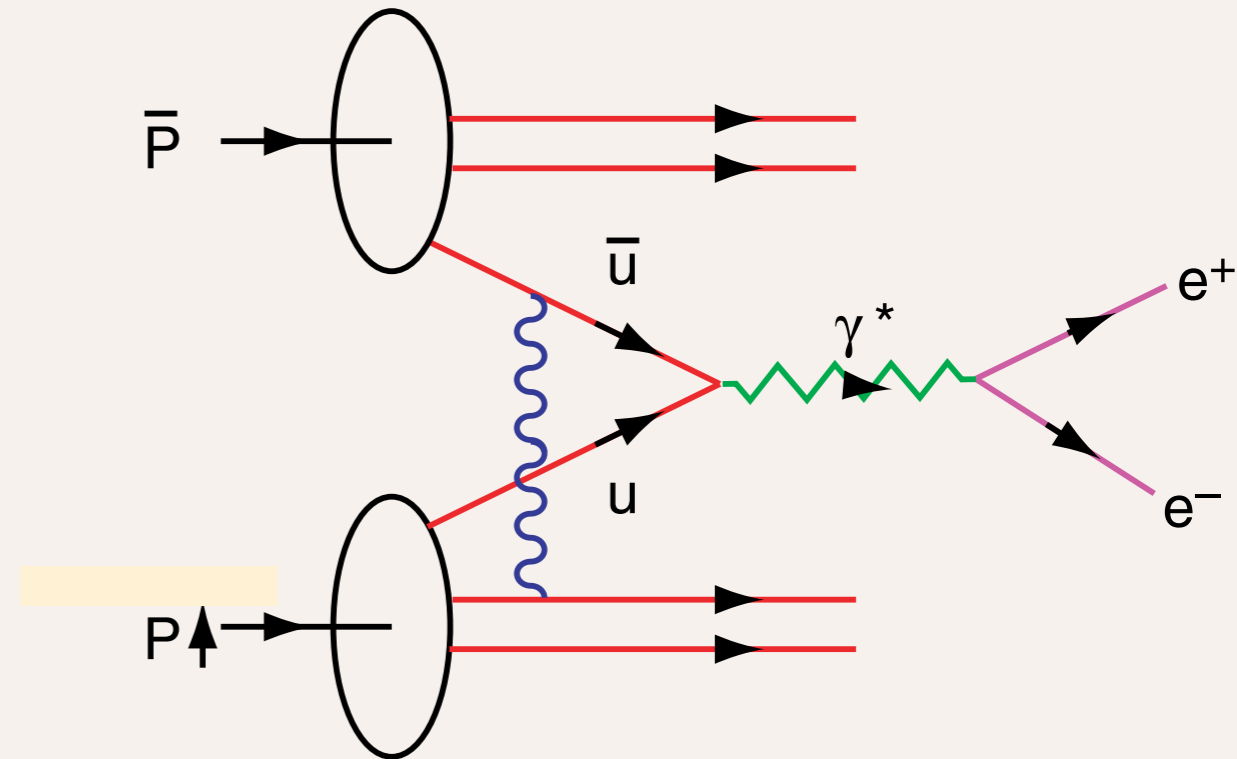
# Key QCD Experiment

Collins;  
Hwang, Schmidt.  
sjb

Measure single-spin asymmetry  $A_N$   
in Drell-Yan reactions

Leading-twist Bjorken-scaling  $A_N$   
from  $S, P$ -wave  
initial-state gluonic interactions

Predict:  $A_N(DY) = -A_N(DIS)$   
Opposite in sign!



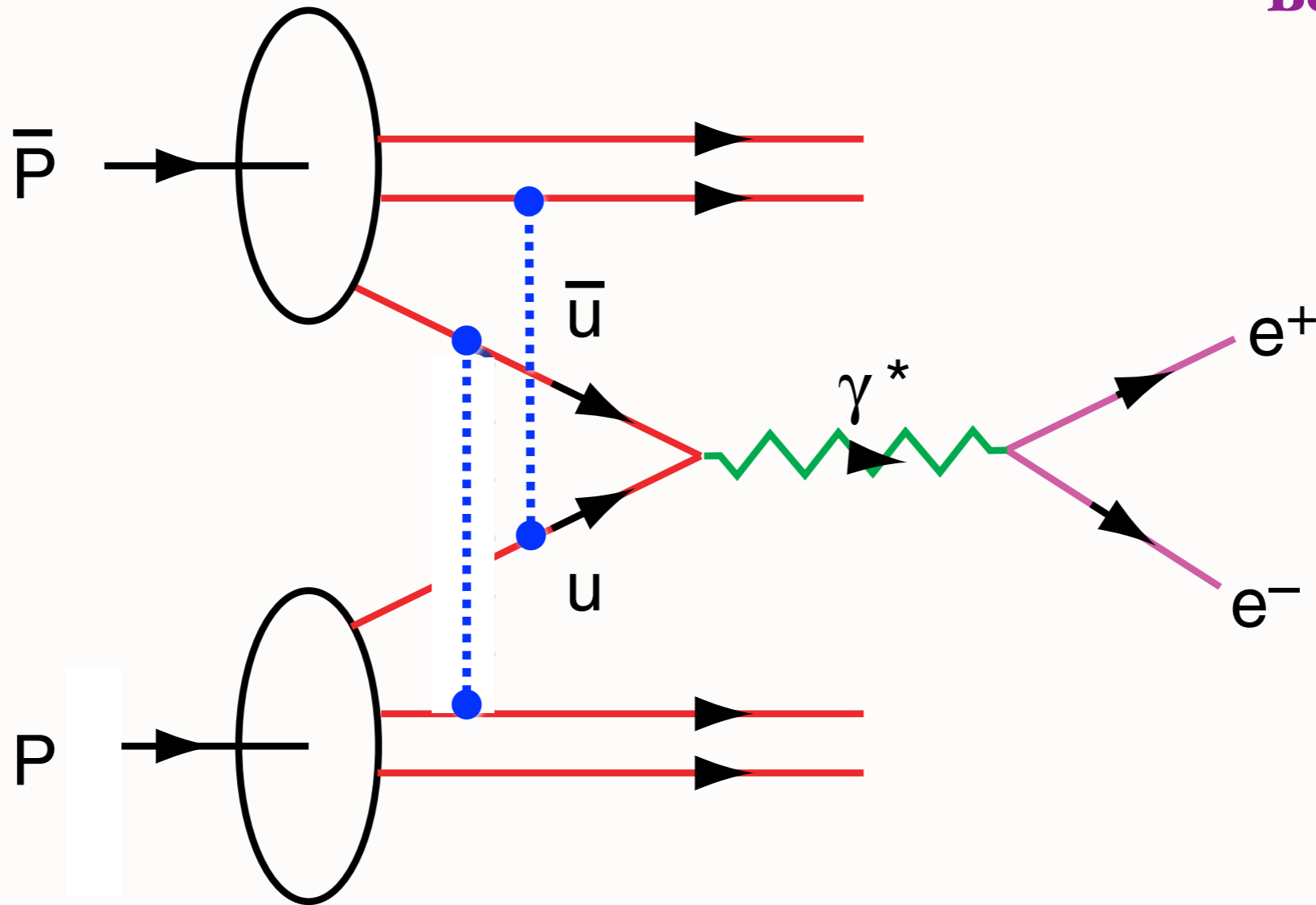
$$\bar{p} p_{\uparrow} \rightarrow l^{+} l^{-} X$$

$$\vec{S} \cdot \vec{q} \times \vec{p} \text{ correlation}$$

## Recent COMPASS data on deuteron: small Sivers effect

- The anomalous magnetic moment, the Sivers function, and the generalized parton distribution  $E$  can all be connected to matrix elements involving the orbital angular momentum of the nucleon's constituents.
- The SSA can be generated by either a quark or gluon mechanism, and the isospin structure of the two mechanisms is distinct. The approximate cancellation of the SSA measured on a deuterium target suggests that the gluon mechanism, and thus the orbital angular momentum carried by gluons in the nucleon, is small.
- Studies of the SSA in  $\phi$  or  $K^+K^-$  production, via  $\gamma^*g \rightarrow s\bar{s} \rightarrow \phi + X$  or  $\gamma^*g \rightarrow s\bar{s} \rightarrow K^+K^- + X$  should provide additional constraints on the gluon mechanism.

Gardner, sjb



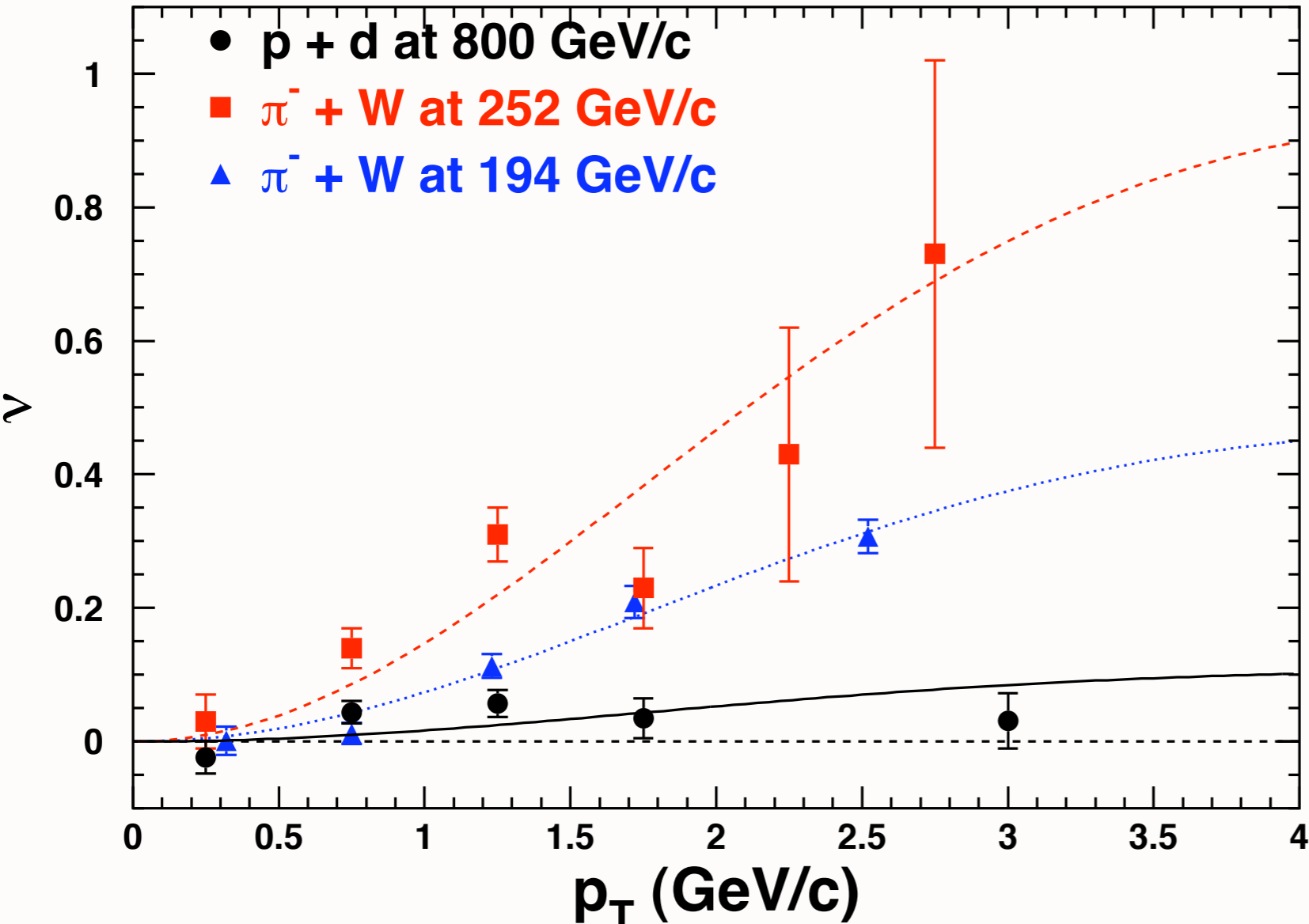
**$DY \cos 2\phi$  correlation at leading twist from double ISI**

*Product of Boer - Mulders Functions*

$$h_1^\perp(x_1, \mathbf{p}_\perp^2) \times \bar{h}_1^\perp(x_2, \mathbf{k}_\perp^2)$$

# Measurement of Angular Distributions of Drell-Yan Dimuons in $p + d$ Interaction at 800 GeV/c

(FNAL E866/NuSea Collaboration)



Huge Effect in  
 $\pi W \rightarrow \mu^+ \mu^- X$   
 Negligible Effect  
 $pd \rightarrow \mu^+ \mu^- X$

Parameter  $\nu$  vs.  $p_T$  in the Collins-Soper frame for three Drell-Yan measurements. Fits to the data using Eq. 3 and  $M_C = 2.4 \text{ GeV}/c^2$  are also shown.

*Single-spin asymmetries in exclusive channels*

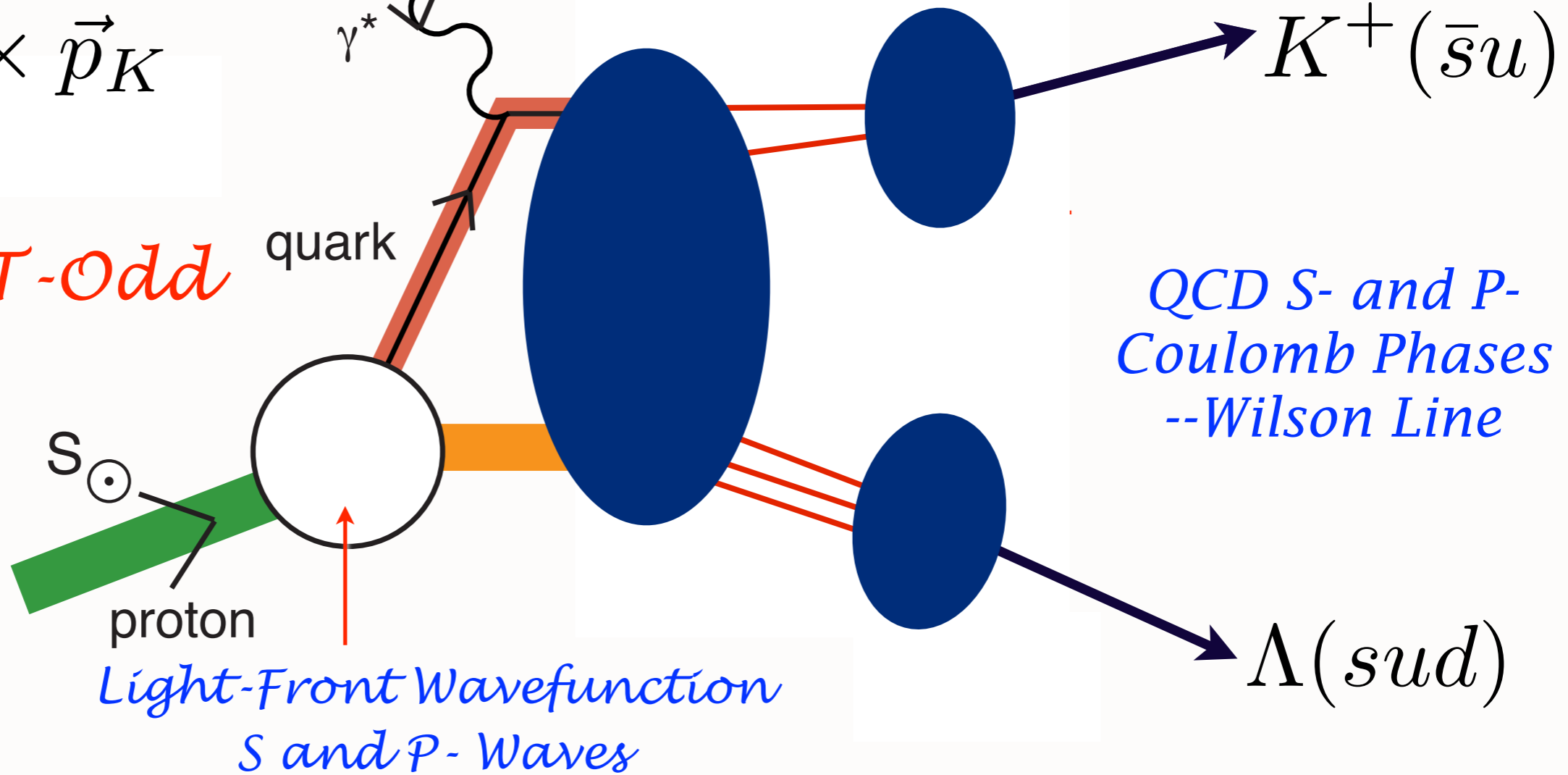
**Exclusive  
Sivers Effect  
connects to  
Inclusive Effect**

$$i\vec{S}_\Lambda \cdot \vec{q} \times \vec{p}_K$$

$$i\vec{S}_p \cdot \vec{q} \times \vec{p}_K$$

$$e^- \gamma^* p_\uparrow \rightarrow K^+ \Lambda$$

*Pseudo-T-Odd*



*QCD S- and P-  
Coulomb Phases  
--Wilson Line*

$$\Lambda(sud)$$

# Double Initial-State Interactions

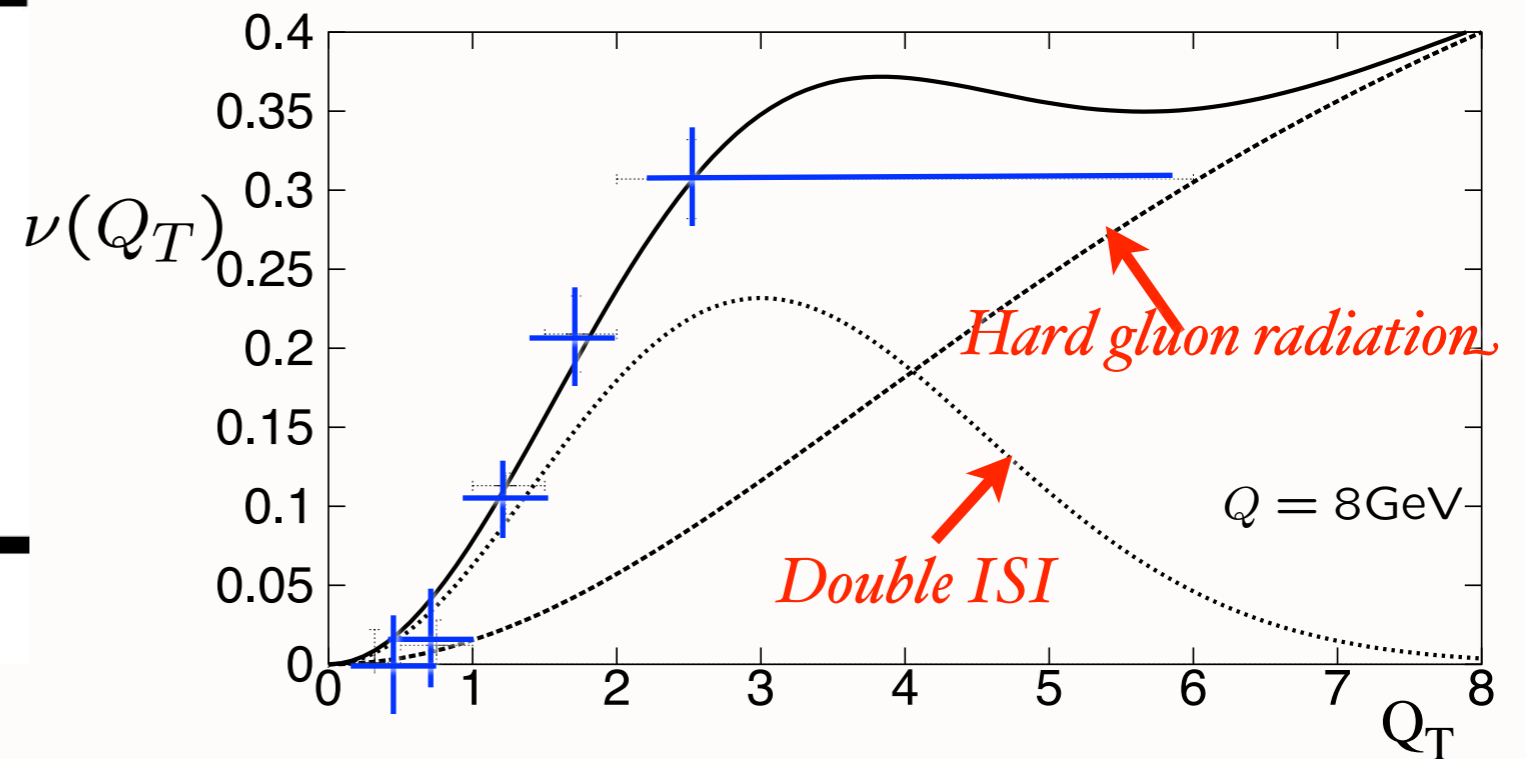
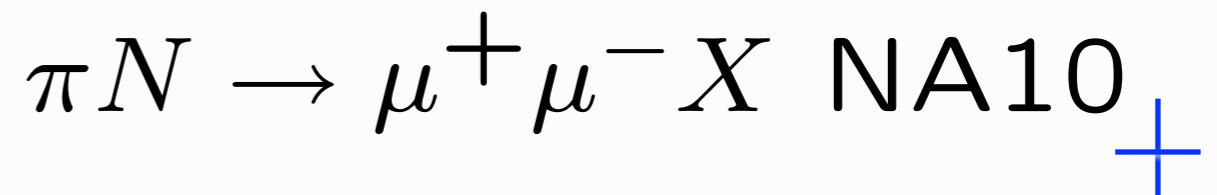
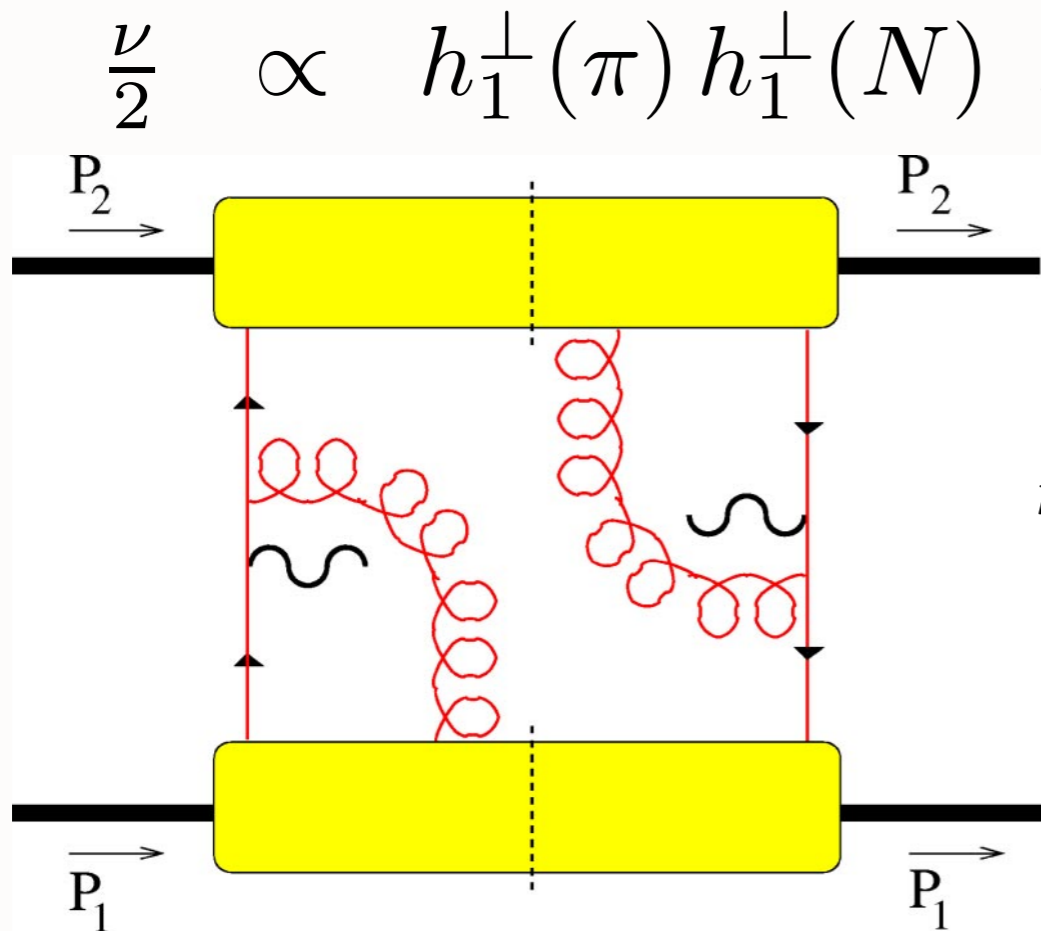
generate anomalous  $\cos 2\phi$

Boer, Hwang, sjb

## Drell-Yan planar correlations

$$\frac{1}{\sigma} \frac{d\sigma}{d\Omega} \propto \left( 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right)$$

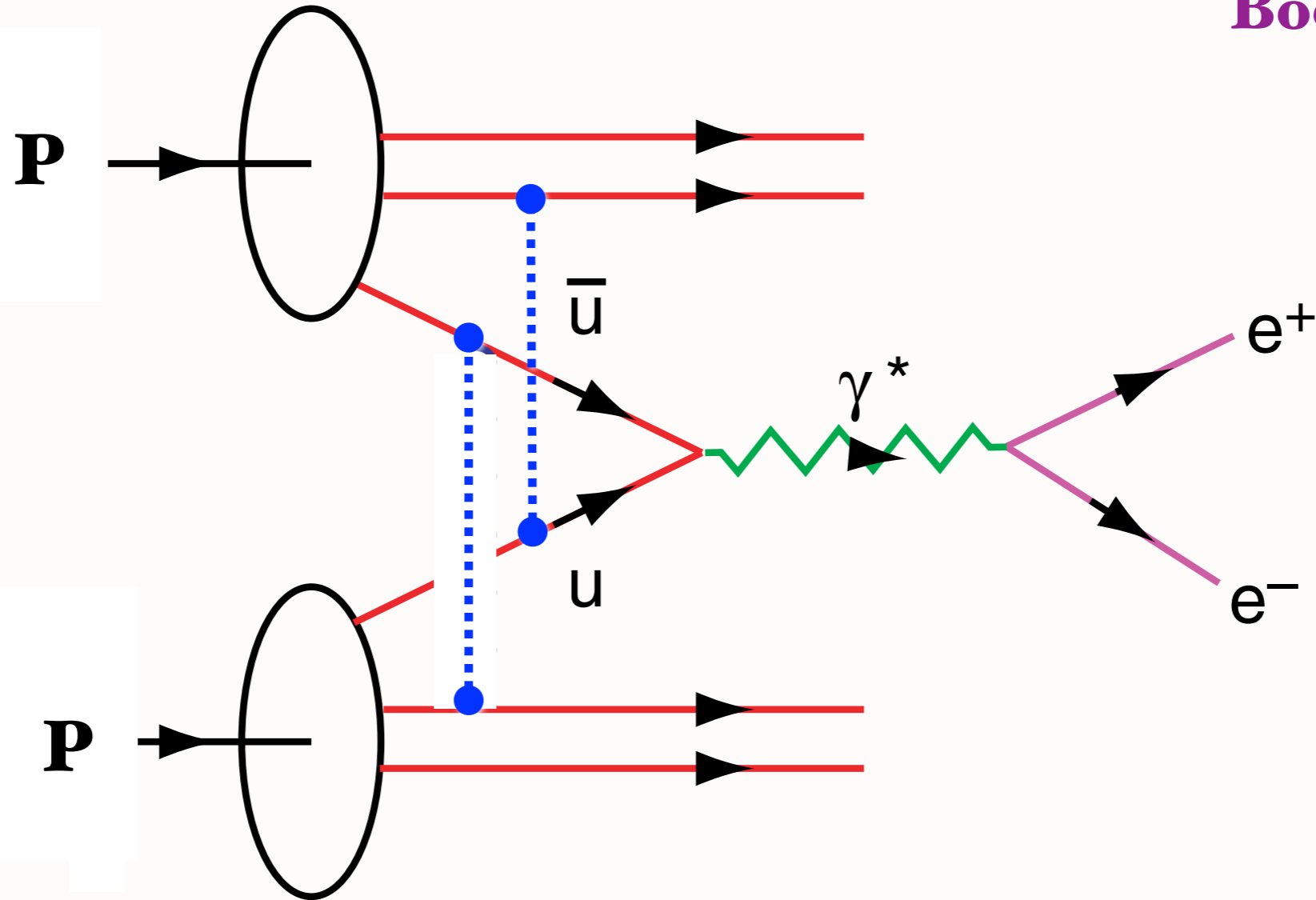
PQCD Factorization (Lam Tung):  $1 - \lambda - 2\nu = 0$



Violates Lam-Tung relation!

Model: Boer,

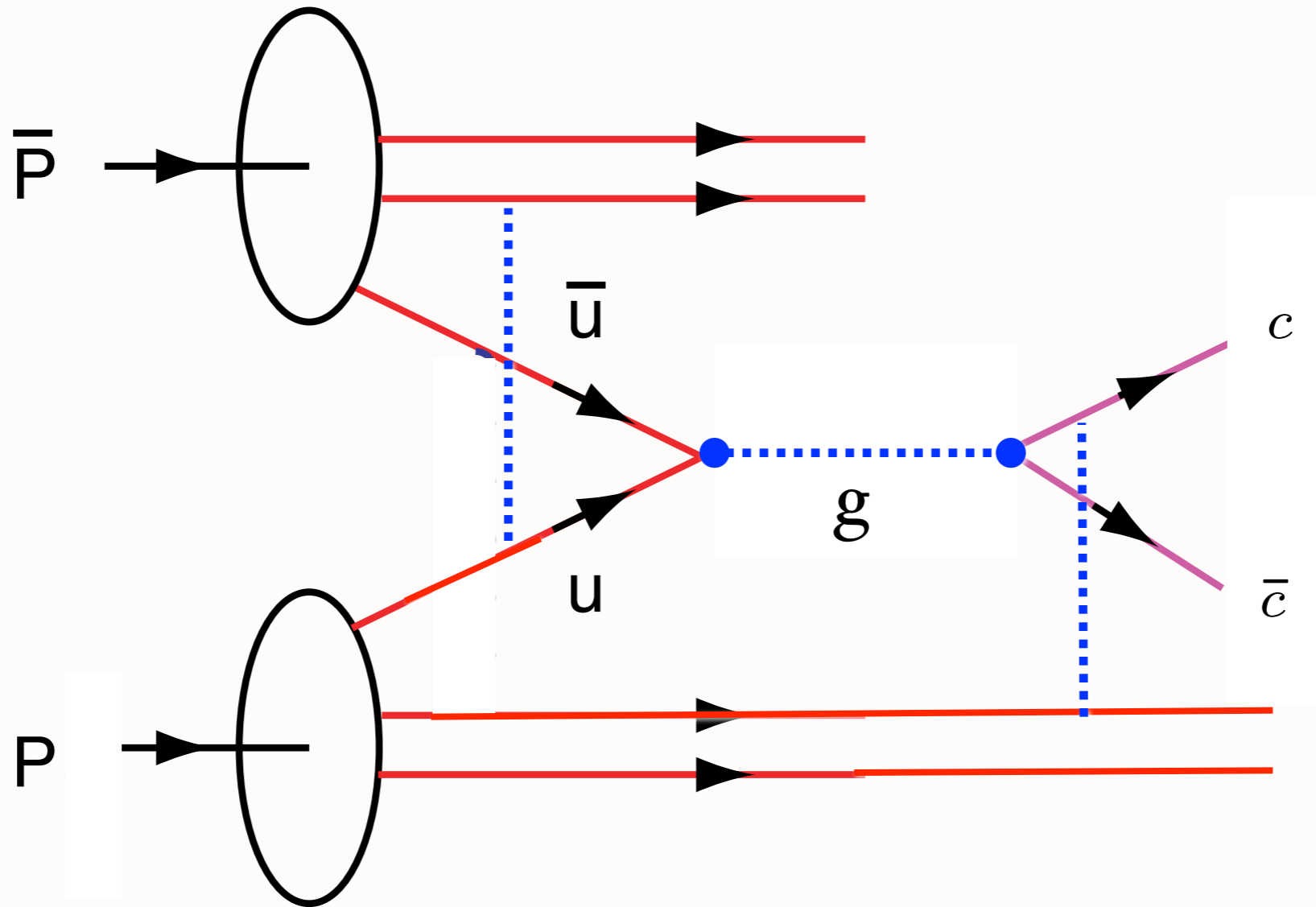




**DY  $\cos 2\phi$  correlation at leading twist from double ISI**

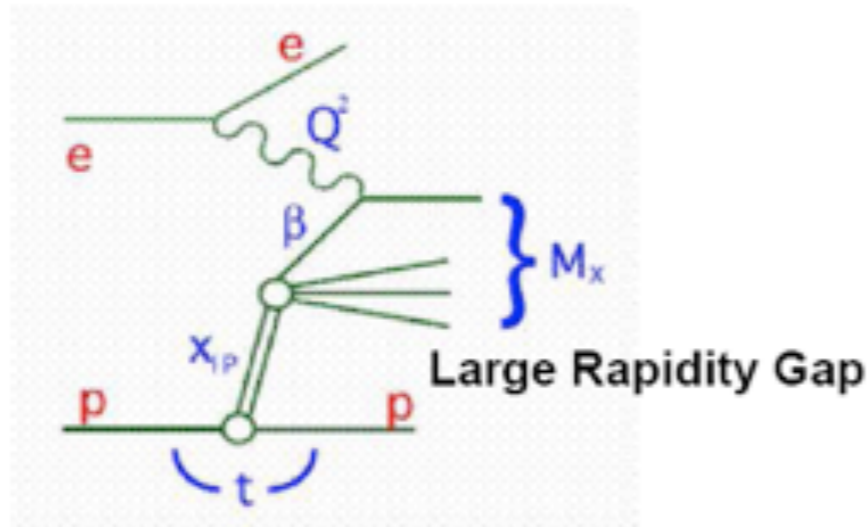
*Product of Boer - Mulders Functions*

$$h_1^\perp(x_1, \mathbf{p}_\perp^2) \times \bar{h}_1^\perp(x_2, \mathbf{k}_\perp^2)$$



*Problem for factorization when both ISI and FSI occur!*

# Diffractive Structure Function $F_2^D$



Diffractive inclusive cross section

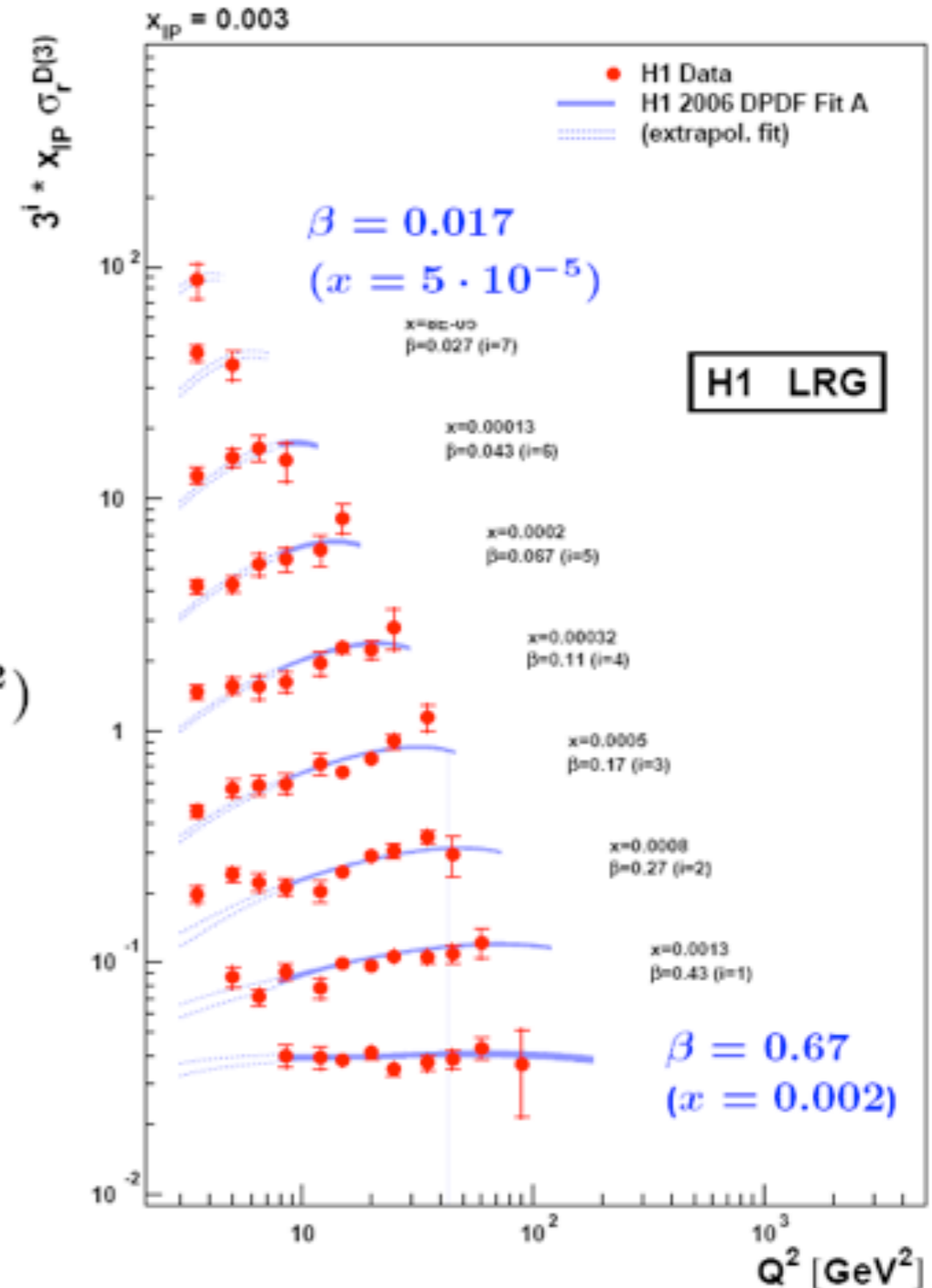
$$\frac{d^3 \sigma_{NC}^{diff}}{dx_{IP} d\beta dQ^2} \propto \frac{2\pi\alpha^2}{xQ^4} F_2^{D(3)}(x_{IP}, \beta, Q^2)$$

$$F_2^D(x_{IP}, \beta, Q^2) = f(x_{IP}) \cdot F_2^{IP}(\beta, Q^2)$$

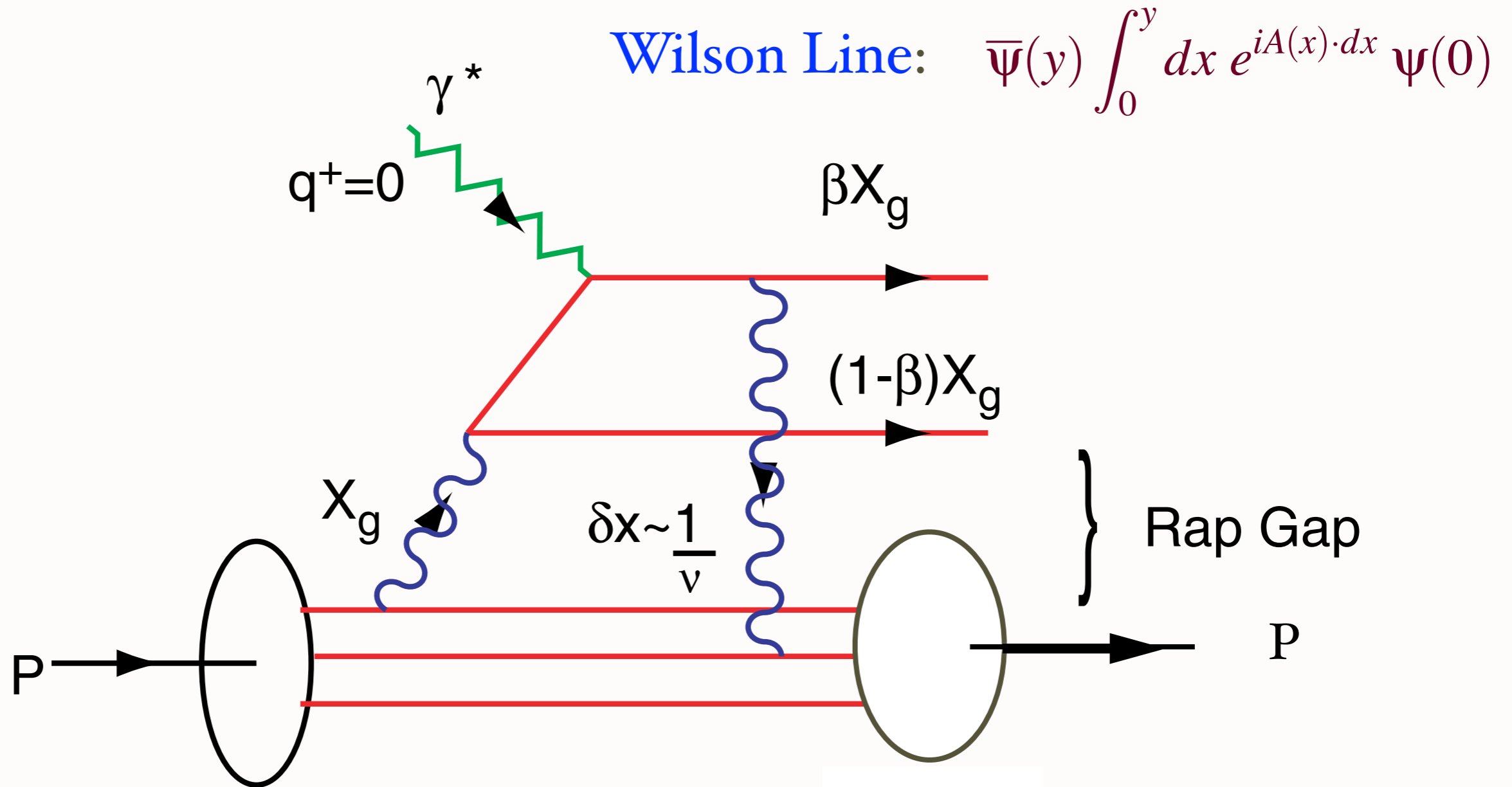
extract DPDF and  $xg(x)$  from scaling violation

Large kinematic domain  $3 < Q^2 < 1600 \text{ GeV}^2$

Precise measurements sys 5%, stat 5–20%



# QCD Mechanism for Rapidity Gaps



**Reproduces lab-frame color dipole approach**

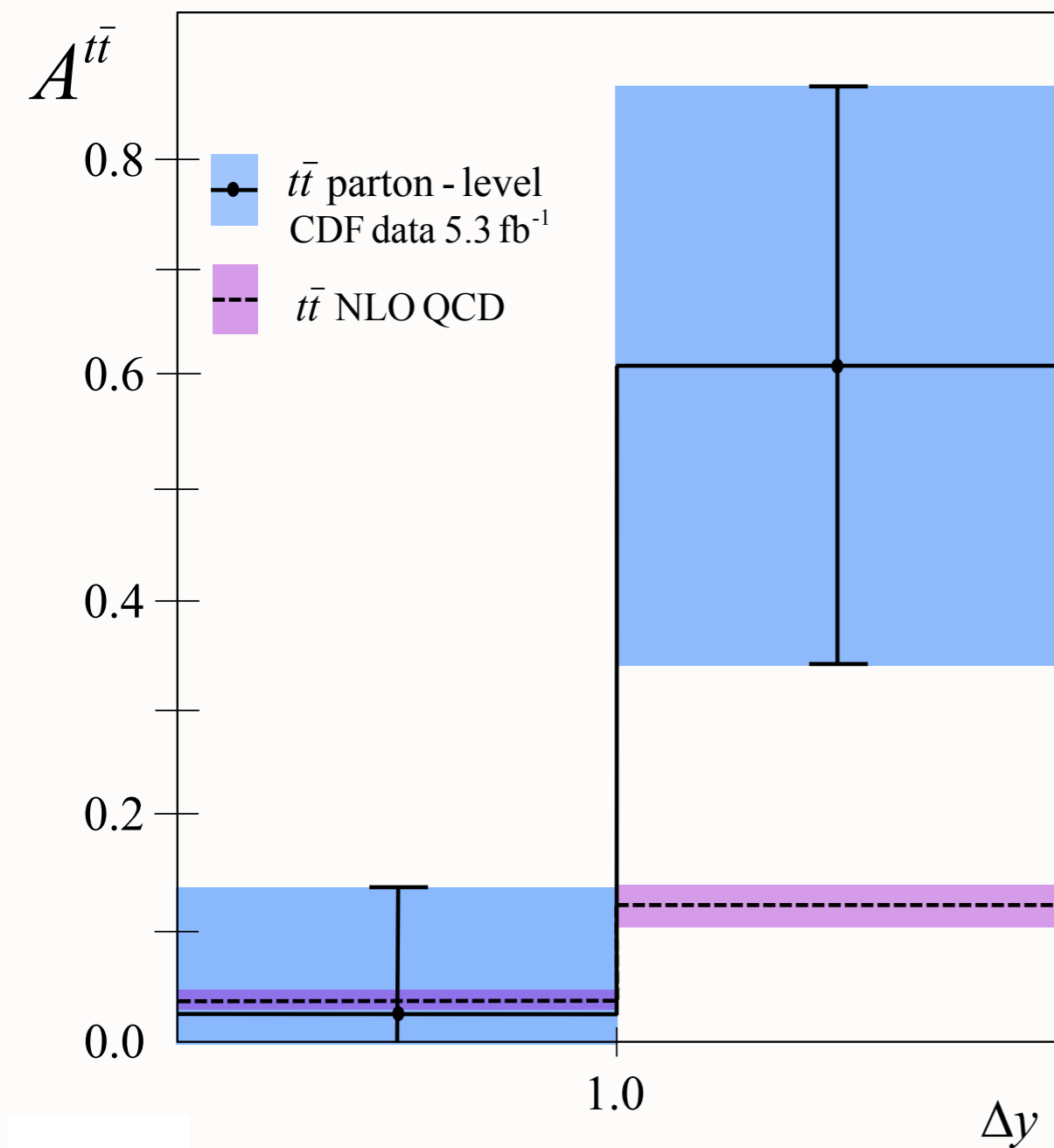
# Physics of Rescattering

- Sivers Asymmetry and Diffractive DIS: New Insights into Final State Interactions in QCD
- Origin of Hard Pomeron
- Structure Functions not Probability Distributions!  
*Not square of LFWFs*
- T-odd SSAs, Shadowing, Antishadowing
- Diffractive dijets/ trijets, doubly diffractive Higgs
- Novel Effects: Color Transparency, Color Opacity, Intrinsic Charm, Odderon

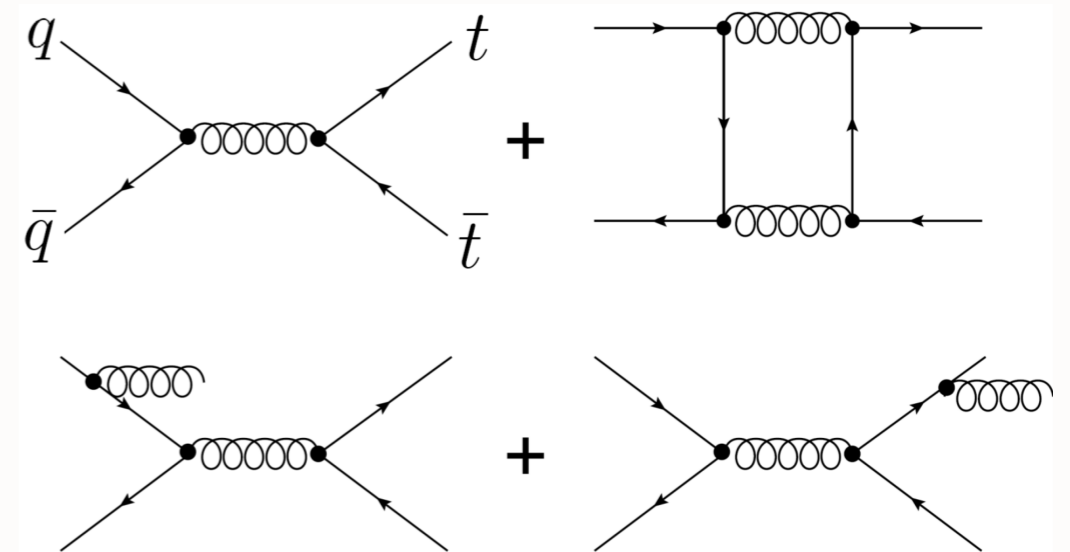
# Heavy Quark Asymmetries

$$A^{t\bar{t}}(\Delta y_i) = \frac{N(\Delta y_i) - N(-\Delta y_i)}{N(\Delta y_i) + N(-\Delta y_i)}$$

Asymmetries in  $\Delta y$  are identical to those in the  $t$  production angle in the  $t\bar{t}$  rest frame. We find a parton-level asymmetry of  $A^{t\bar{t}} = 0.158 \pm 0.075$  (stat+sys), which is somewhat higher than, but not inconsistent with, the NLO QCD expectation of  $0.058 \pm 0.009$ .



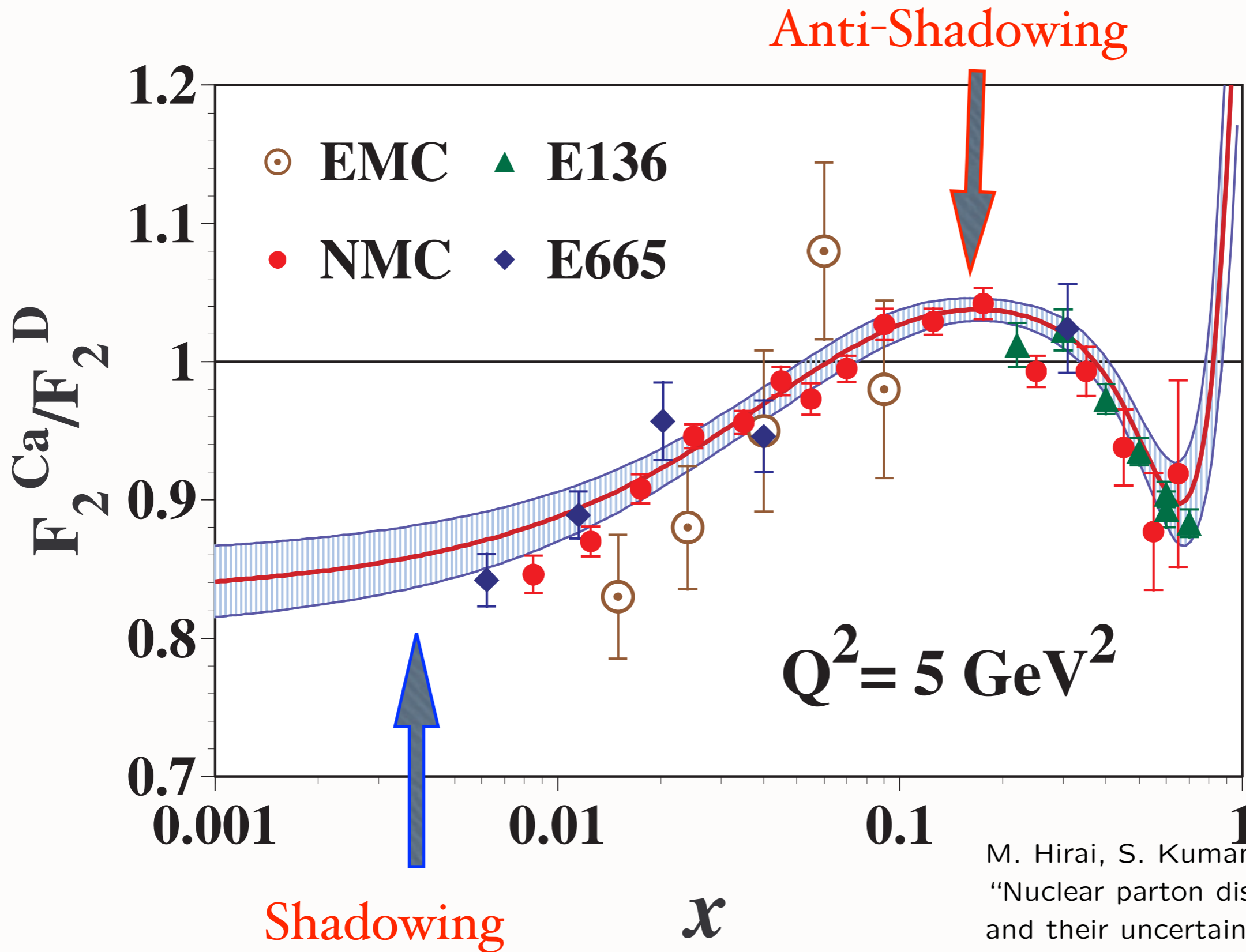
Parton level asymmetries at small and large  $\Delta y$  compared to SM prediction of MCFM. The shaded bands represent the total uncertainty in each bin. The negative going uncertainty for  $\Delta y < 1.0$  is suppressed.



Fermilab-Pub-10-525-E

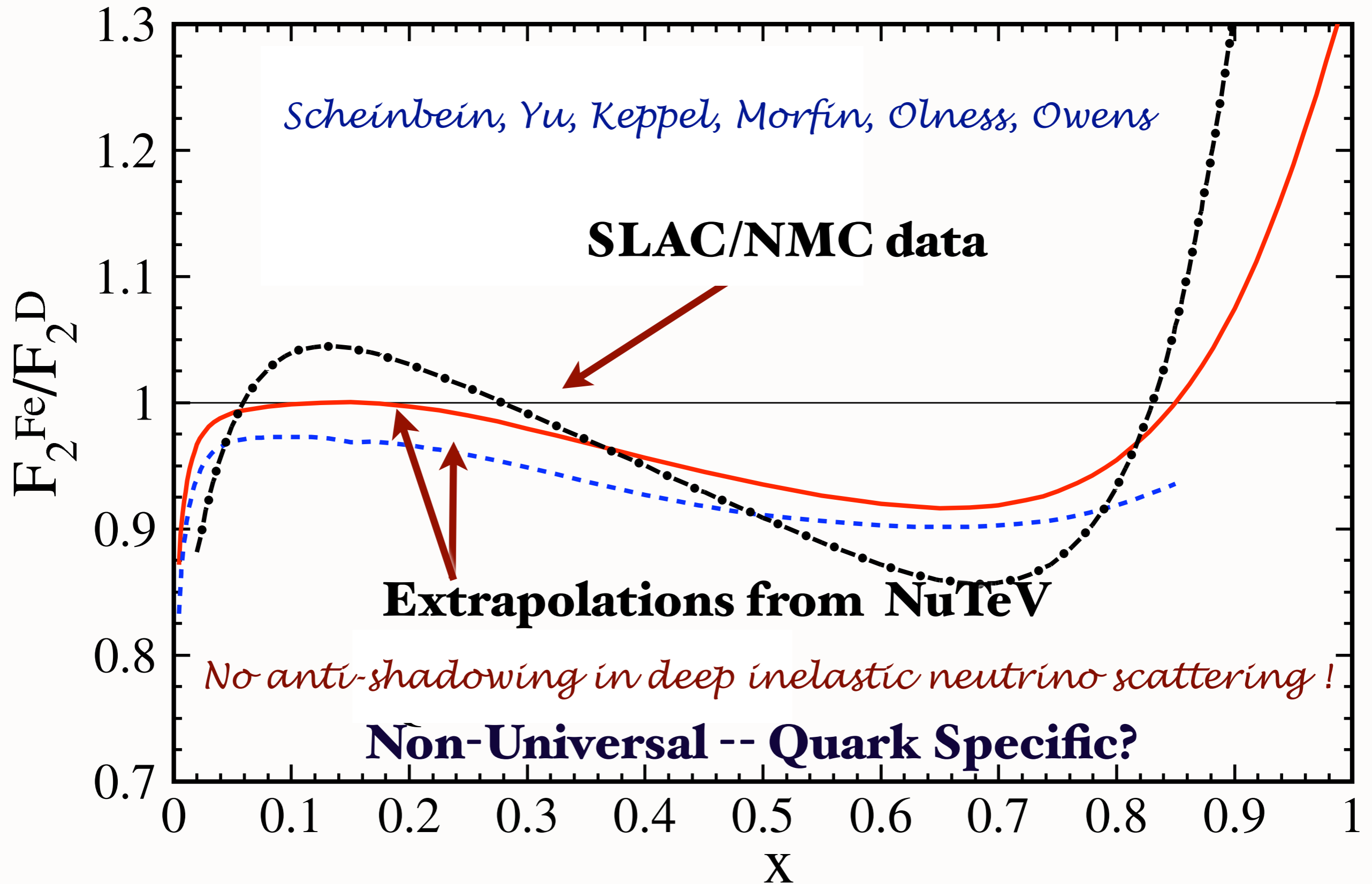
**Evidence for a Mass Dependent Forward-Backward Asymmetry  
in Top Quark Pair Production**

**CDF Collaboration**



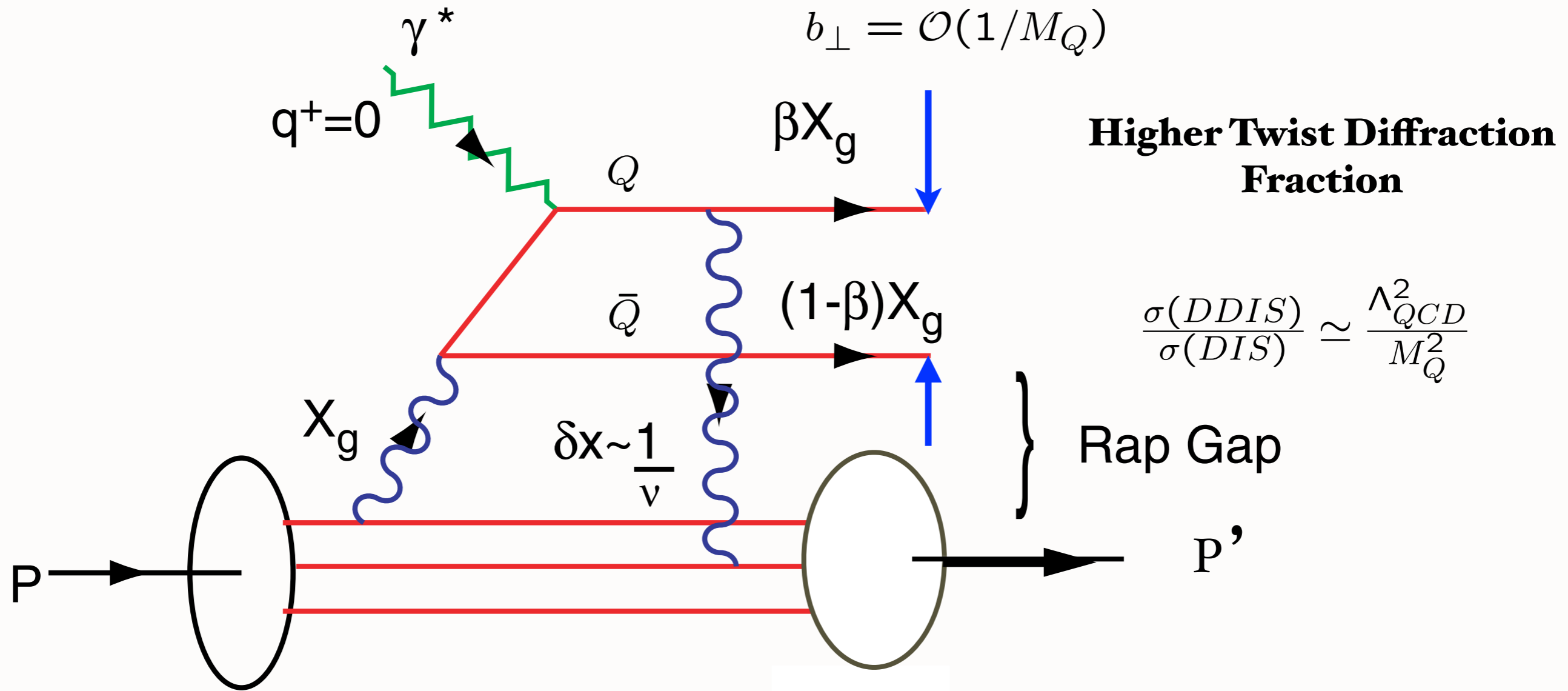
M. Hirai, S. Kumano and T. H. Nagai,  
 "Nuclear parton distribution functions  
 and their uncertainties,"  
 Phys. Rev. C **70**, 044905 (2004)  
 [arXiv:hep-ph/0404093].

$$Q^2 = 5 \text{ GeV}^2$$





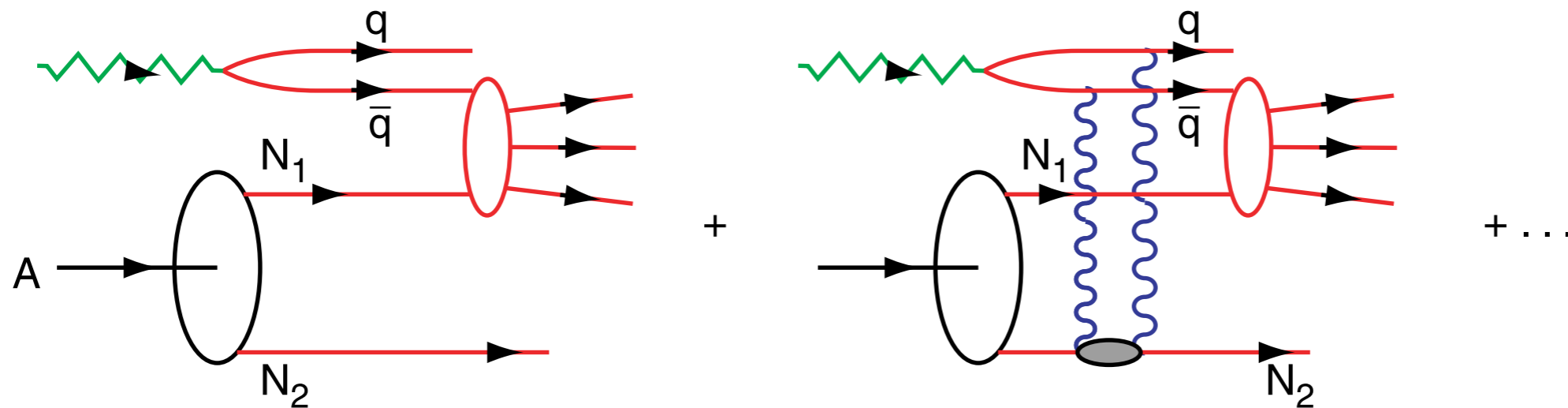
# Predict: Reduced DDIS/DIS for Heavy Quarks



**Kopeliovitch, Schmidt, sjb**

**Reproduces lab-frame color dipole approach**

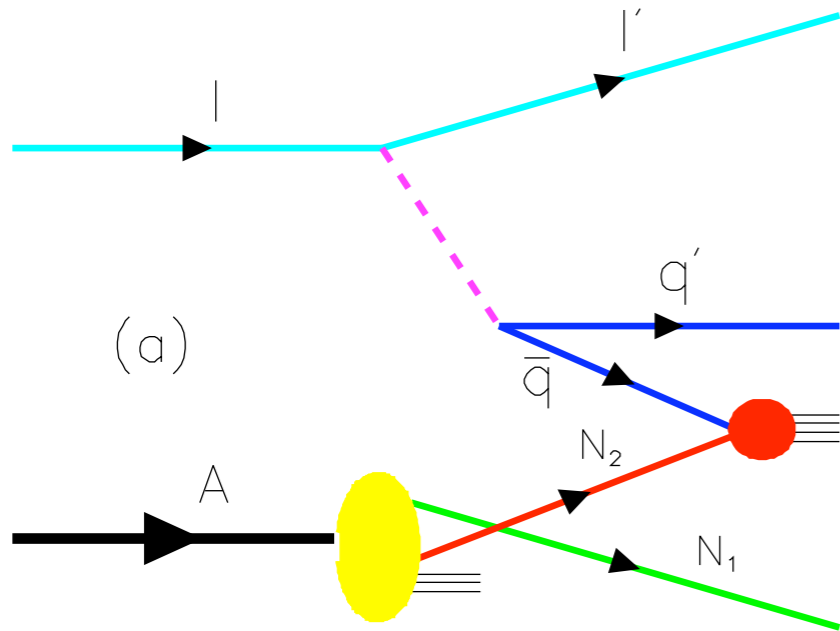
# Nuclear Shadowing in QCD



*Shadowing depends on understanding leading twist-diffraction in DIS*

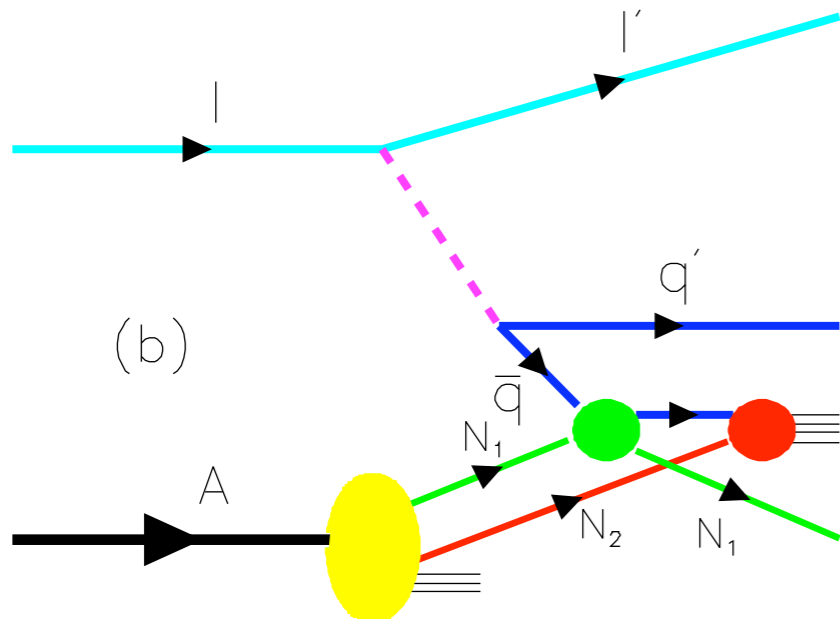
**Nuclear Shadowing not included in nuclear LFWF !**

**Dynamical effect due to virtual photon interacting in nucleus**



The one-step and two-step processes in DIS on a nucleus.

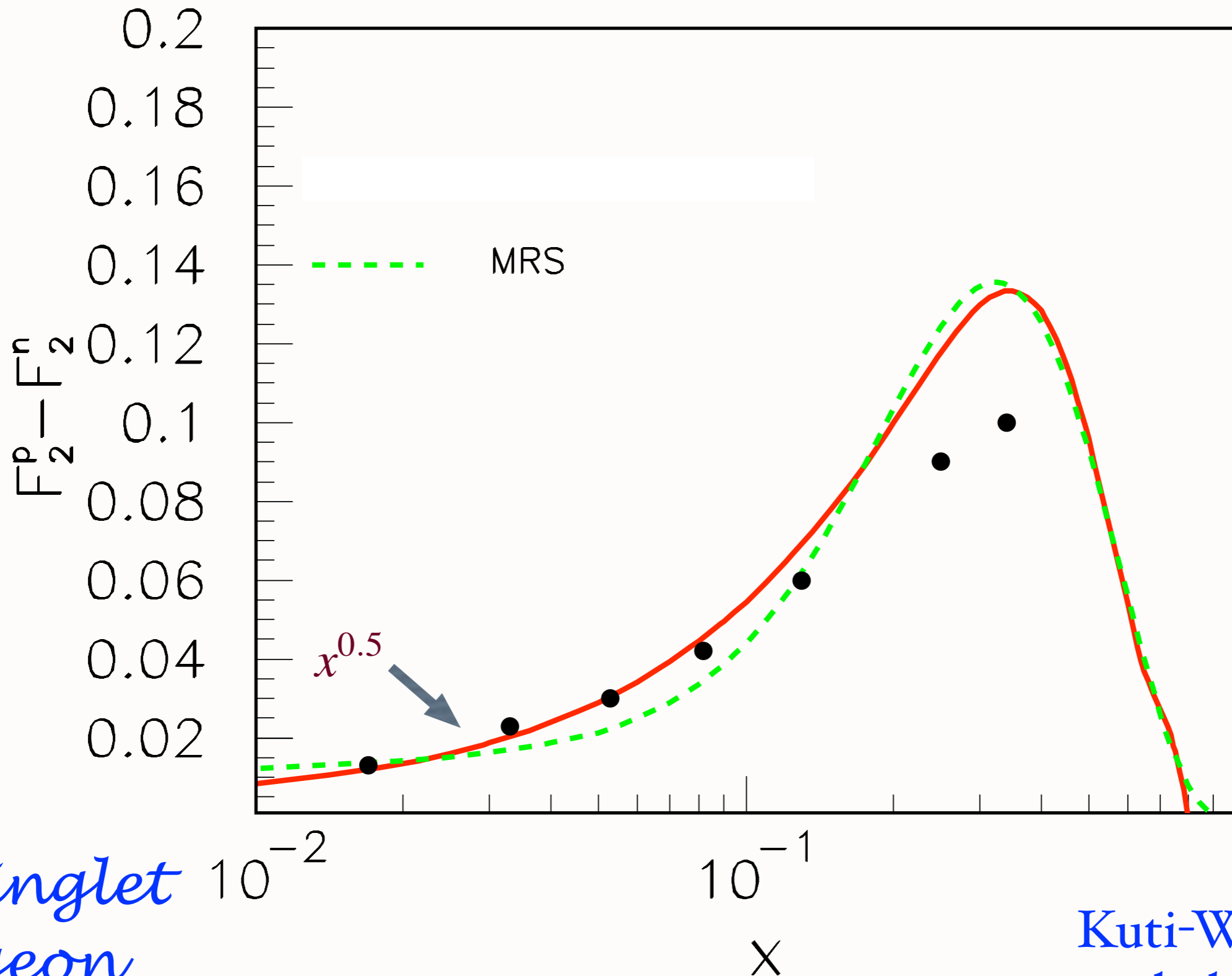
Coherence at small Bjorken  $x_B$  :  
 $1/Mx_B = 2\nu/Q^2 \geq L_A$ .



If the scattering on nucleon  $N_1$  is via pomeron exchange, the one-step and two-step amplitudes are opposite in phase, thus diminishing the  $\bar{q}$  flux reaching  $N_2$ .

→ Shadowing of the DIS nuclear structure functions.

## Observed HERA DDIS produces nuclear shadowing



*Non-singlet  
Reggeon  
Exchange*

*Kuti-Weisskopf  
behavior*

**Warsaw  
July 6, 2012**

**Hot Topics in QCD Phenomenology  
I48**

**Stan Brodsky**



# Reggeon Exchange

Phase of two-step amplitude relative to one step:

$$\frac{1}{\sqrt{2}}(1 - i) \times i = \frac{1}{\sqrt{2}}(i + 1)$$

Constructive Interference

Depends on quark flavor!

Thus antishadowing is not universal

Different for couplings of  $\gamma^*$ ,  $Z^0$ ,  $W^\pm$

*Critical test: Tagged Drell-Yan*

# Origin of Regge Behavior of Deep Inelastic Structure Functions

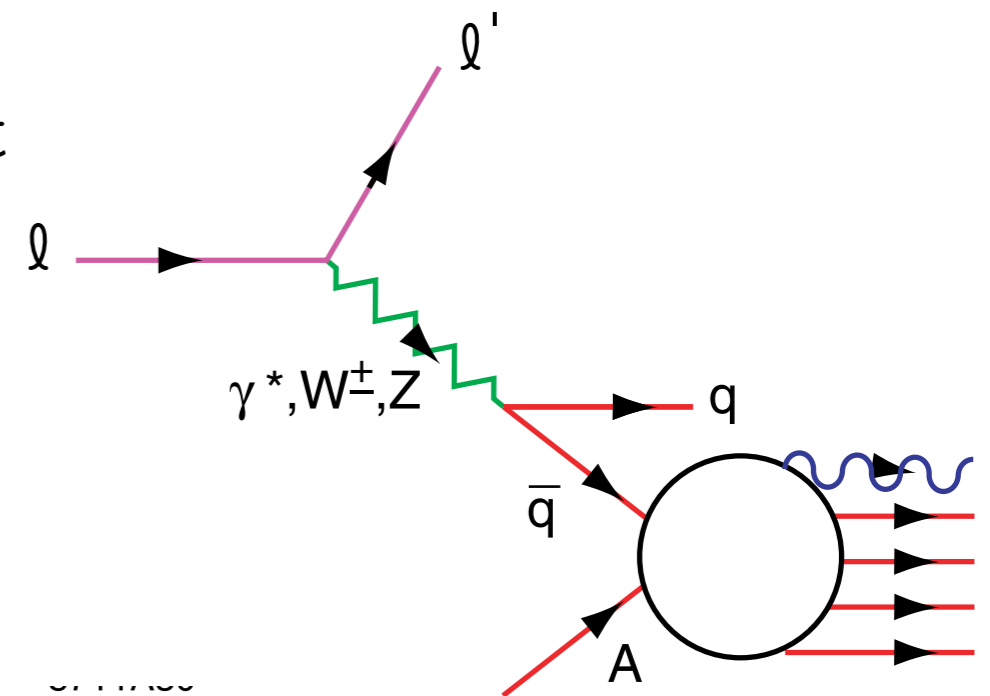
$$F_{2p}(x) - F_{2n}(x) \propto x^{1/2}$$

Antiquark interacts with target nucleus at energy  $\hat{s} \propto \frac{1}{x_{bj}}$

Regge contribution:  $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R - 1}$

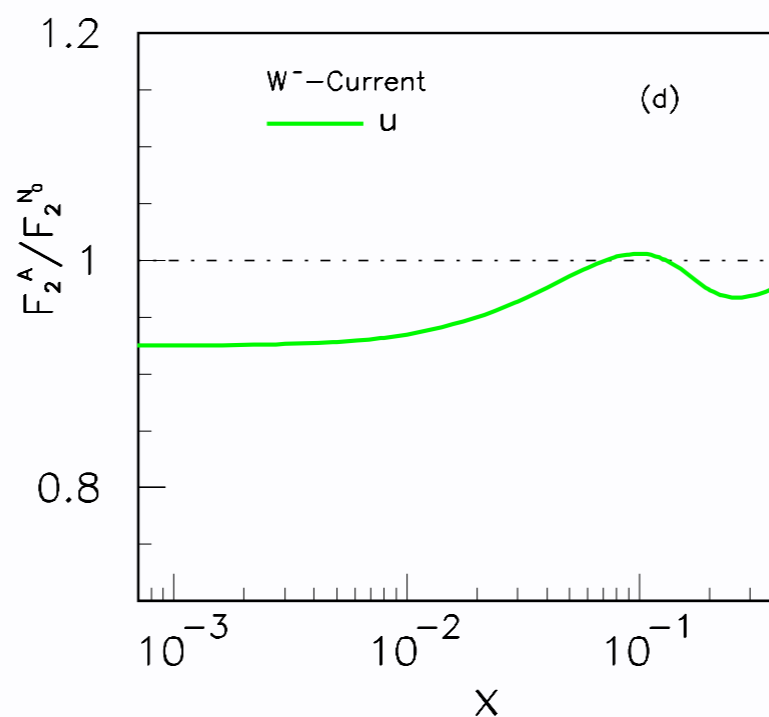
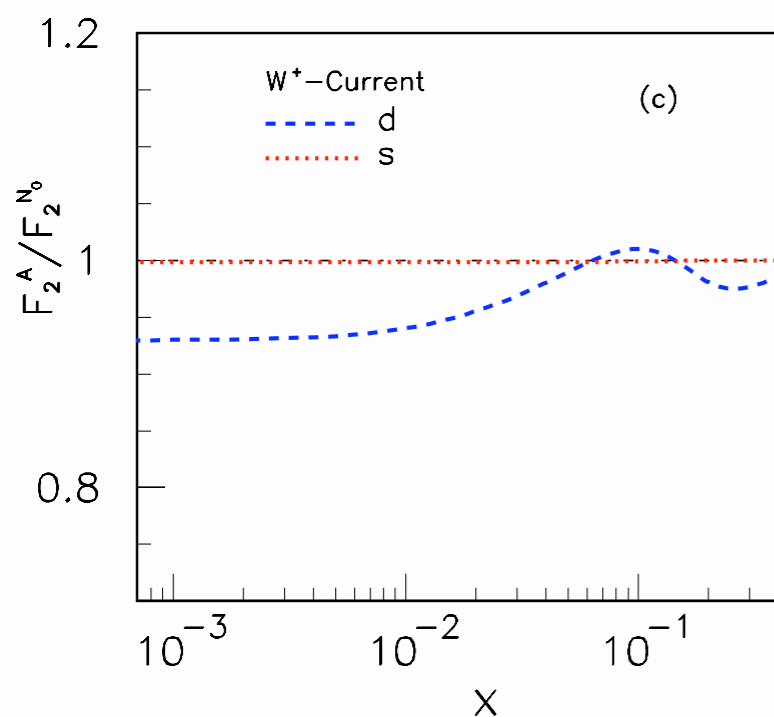
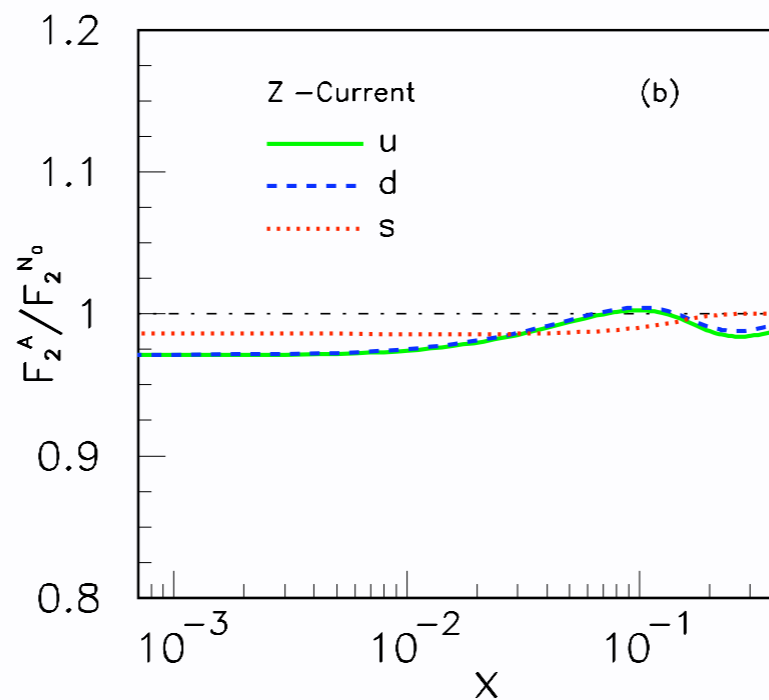
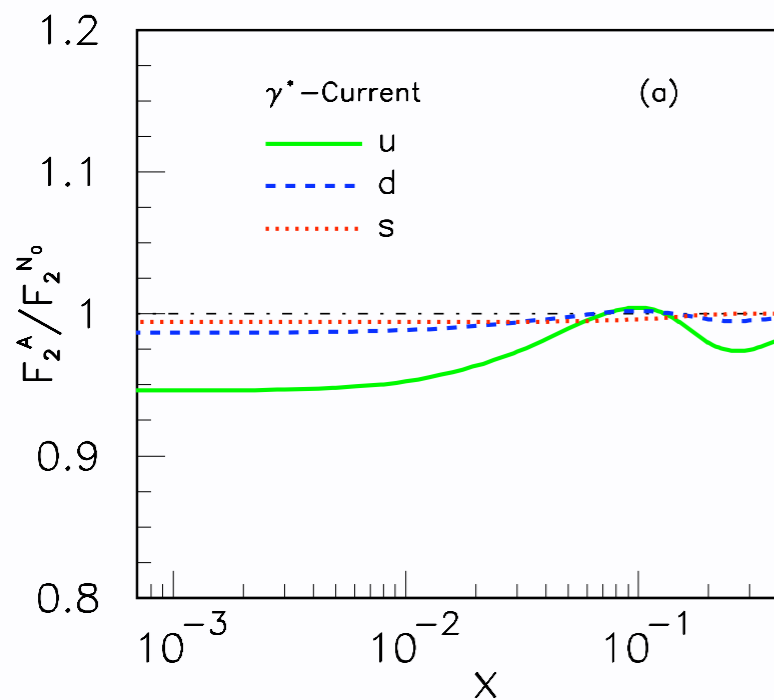
Nonsinglet Kuti-Weisskoff  $F_{2p} - F_{2n} \propto \sqrt{x_{bj}}$  at small  $x_{bj}$ .

Shadowing of  $\sigma_{\bar{q}M}$  produces shadowing of nuclear structure function.



**Landshoff,  
Polkinghorne, Short  
Close, Gunion, sjb  
Schmidt, Yang, Lu,  
sjb**

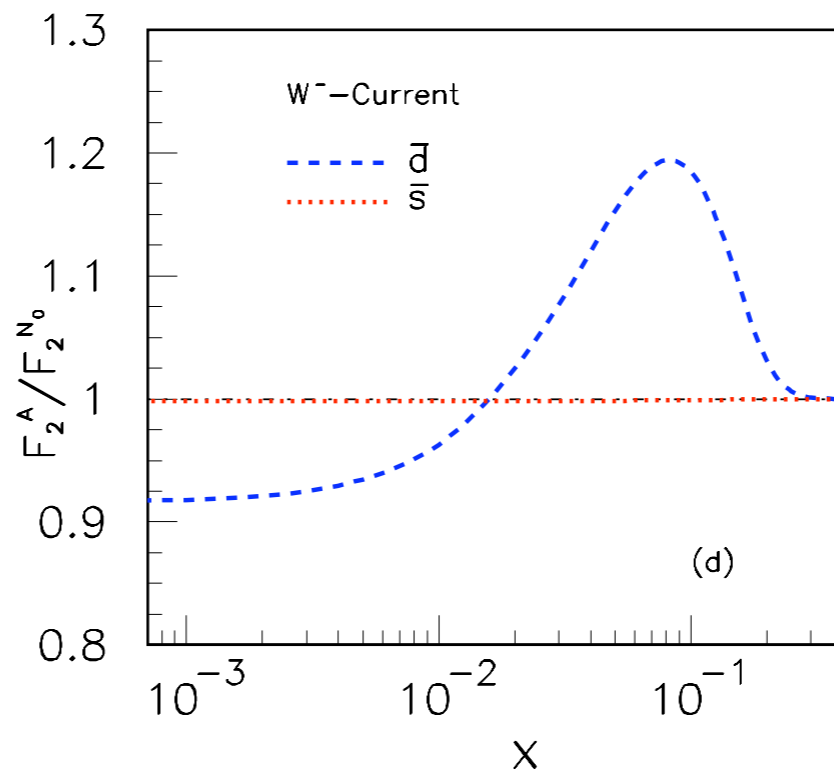
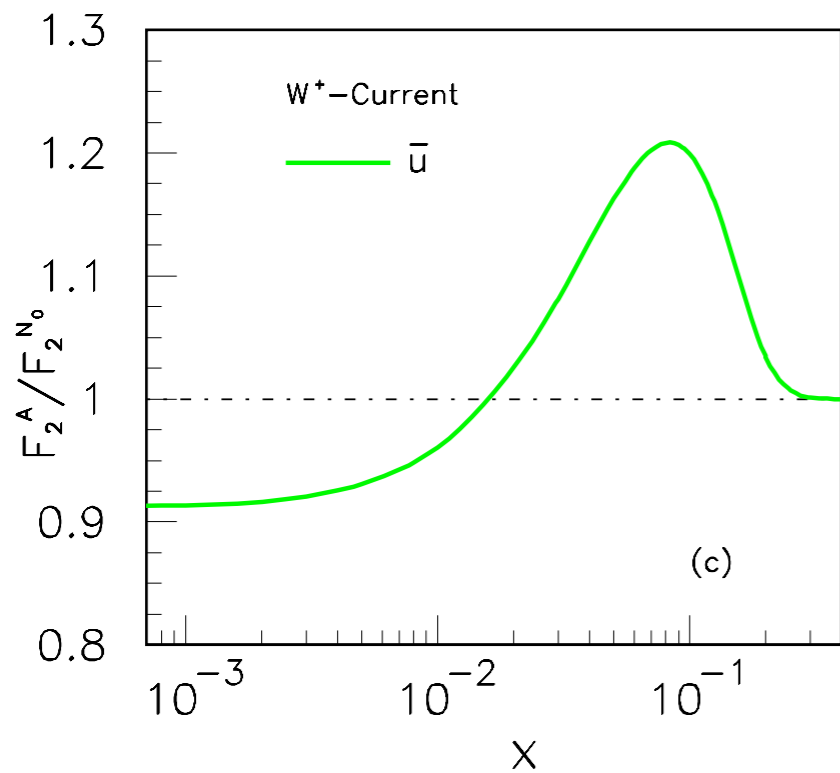
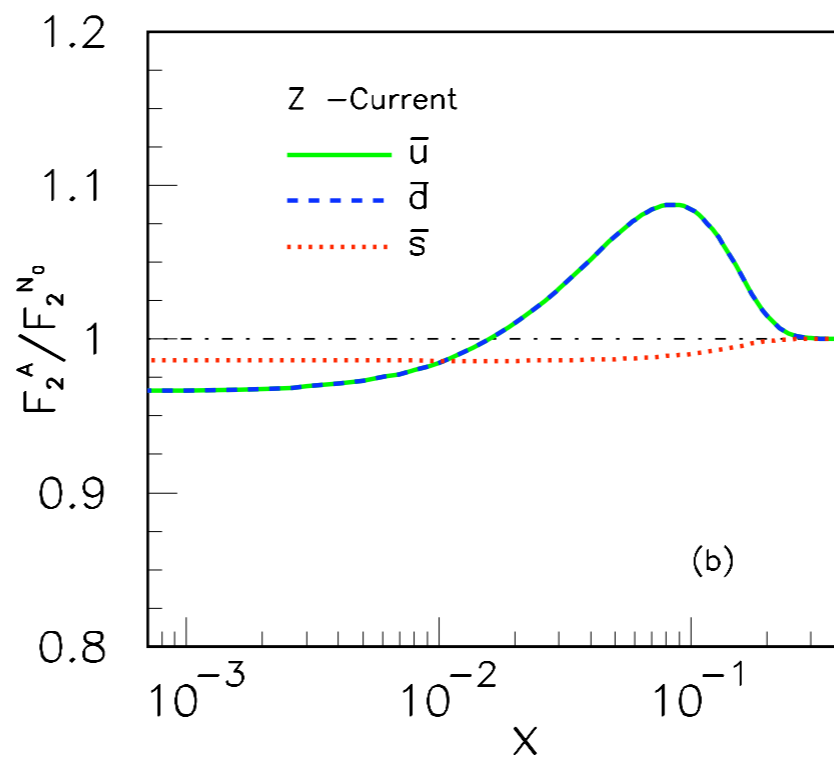
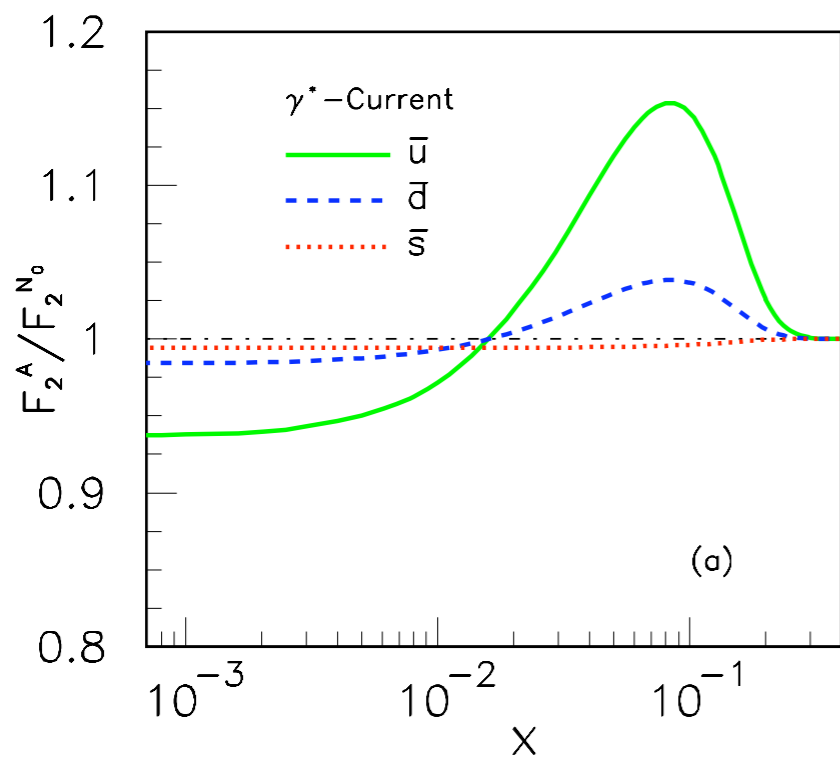
# Shadowing and Antishadowing of DIS Structure Functions



S. J. Brodsky, I. Schmidt and J. J. Yang,  
 “Nuclear Antishadowing in  
 Neutrino Deep Inelastic Scattering,”  
 Phys. Rev. D 70, 116003 (2004)  
 [arXiv:hep-ph/0409279].

**Modifies**  
**NuTeV extraction of**  
 $\sin^2 \theta_W$

**Test in flavor-tagged  
 lepton-nucleus collisions**

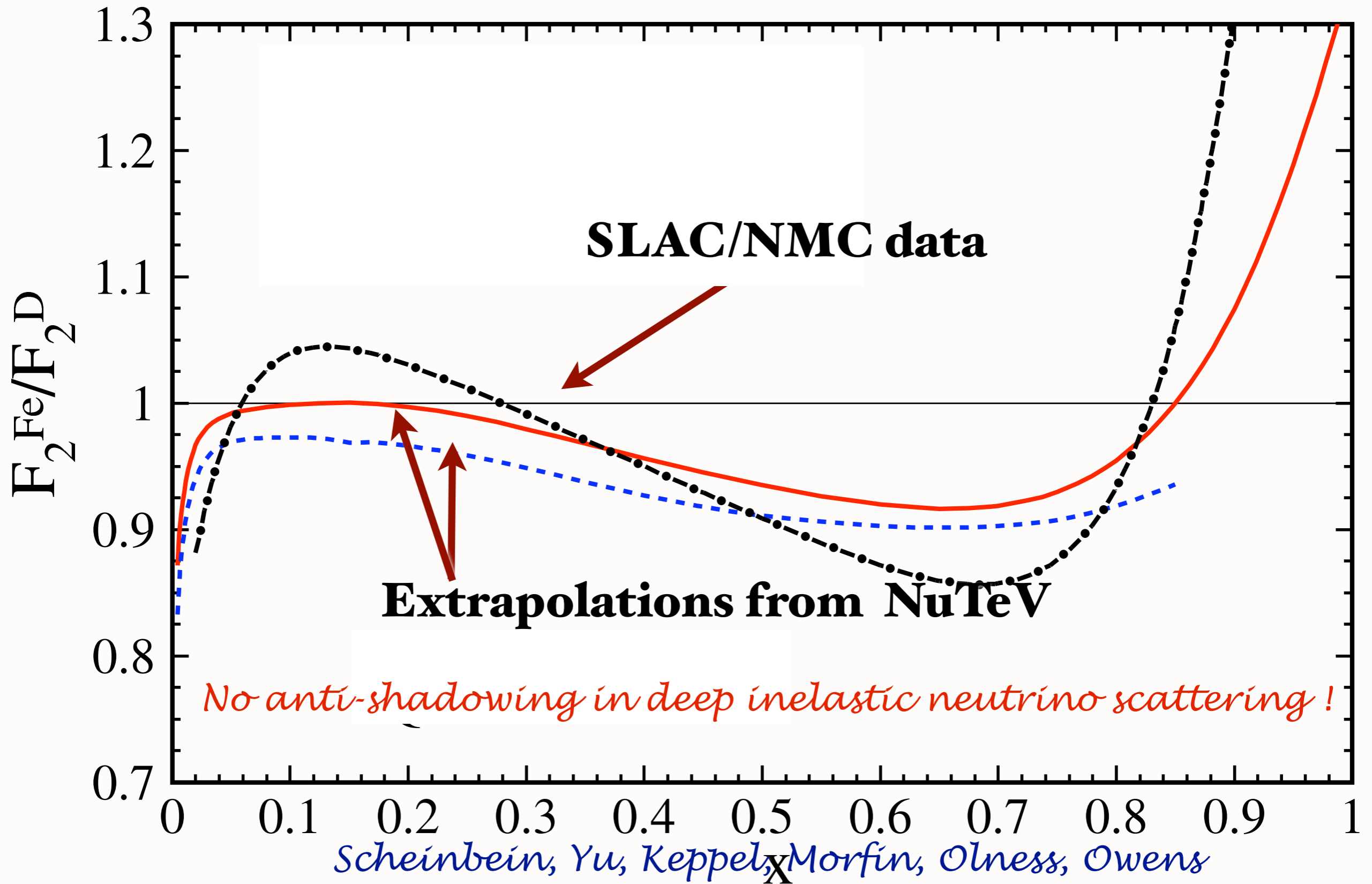


Schmidt, Yang; sjb

*Nuclear Antishadowing not universal!*

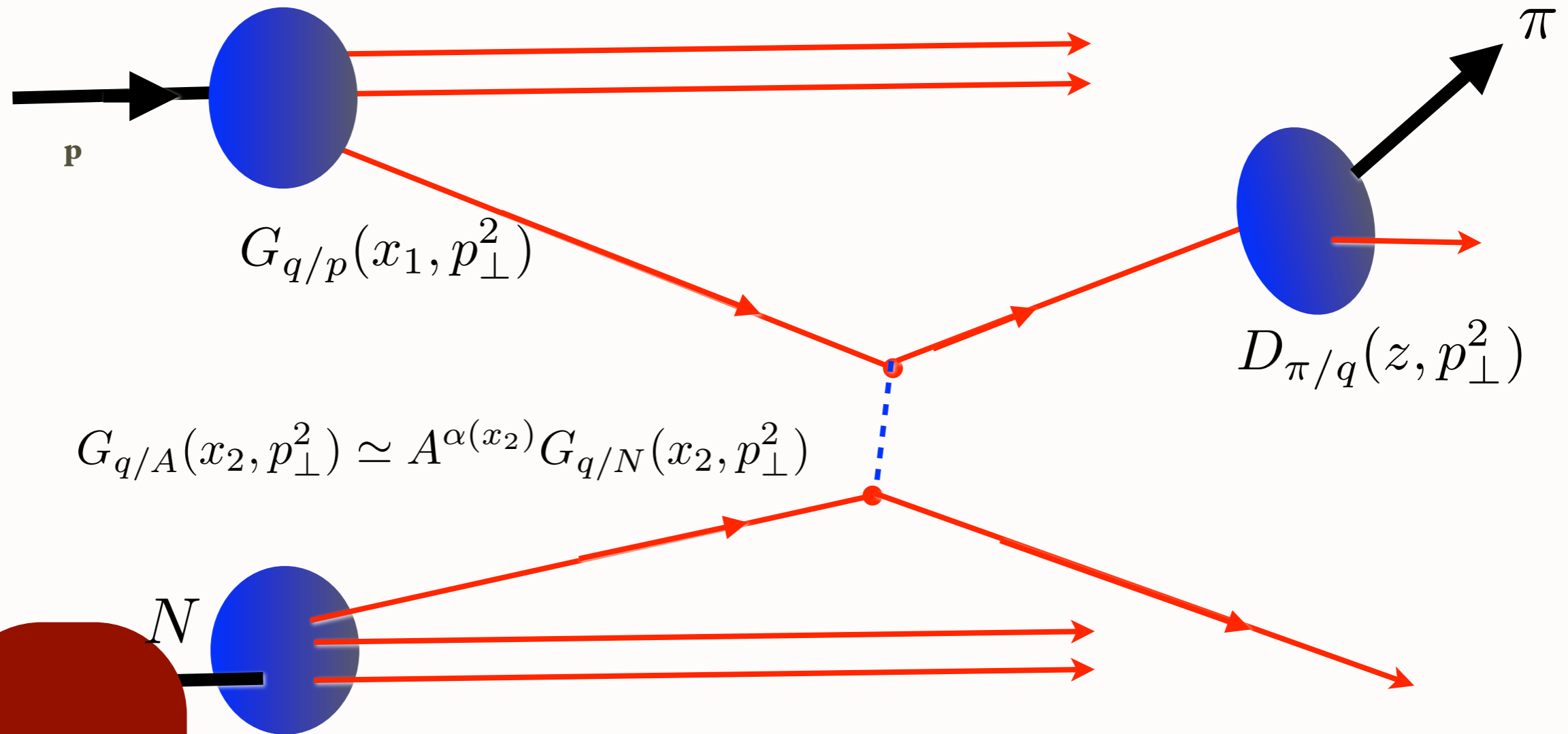


$$Q^2 = 5 \text{ GeV}^2$$



# LHC $p$ - $A$ Collisions

Leading-Twist Contribution to Hadron Production on Nuclei



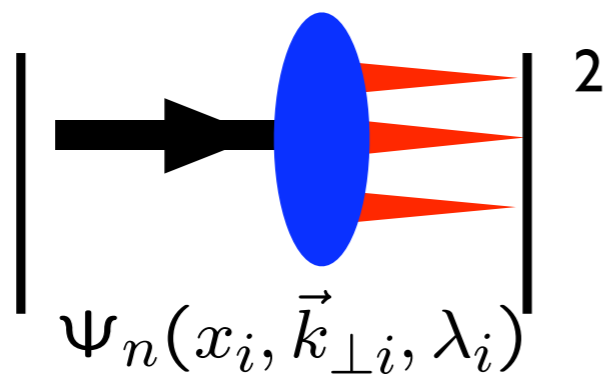
$$G_{q/A}(x_2, p_{\perp}^2) \simeq A^{\alpha(x_2)} G_{q/N}(x_2, p_{\perp}^2)$$

$$\frac{d\sigma}{d^3p/E}(pA \rightarrow \pi X) = A^{\alpha}(x_2) \frac{d\sigma}{d^3p/E}(pN \rightarrow \pi X)$$

*Test: Anti-shadowing is quark specific?*

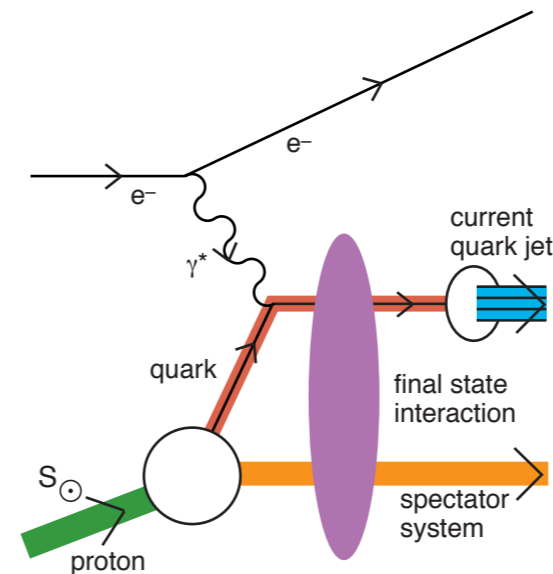
# Static

- Square of Target LFWFs
- No Wilson Line
- Probability Distributions
- Process-Independent
- T-even Observables
- No Shadowing, Anti-Shadowing
- Sum Rules: Momentum and  $J^z$
- DGLAP Evolution; mod. at large  $x$
- No Diffractive DIS

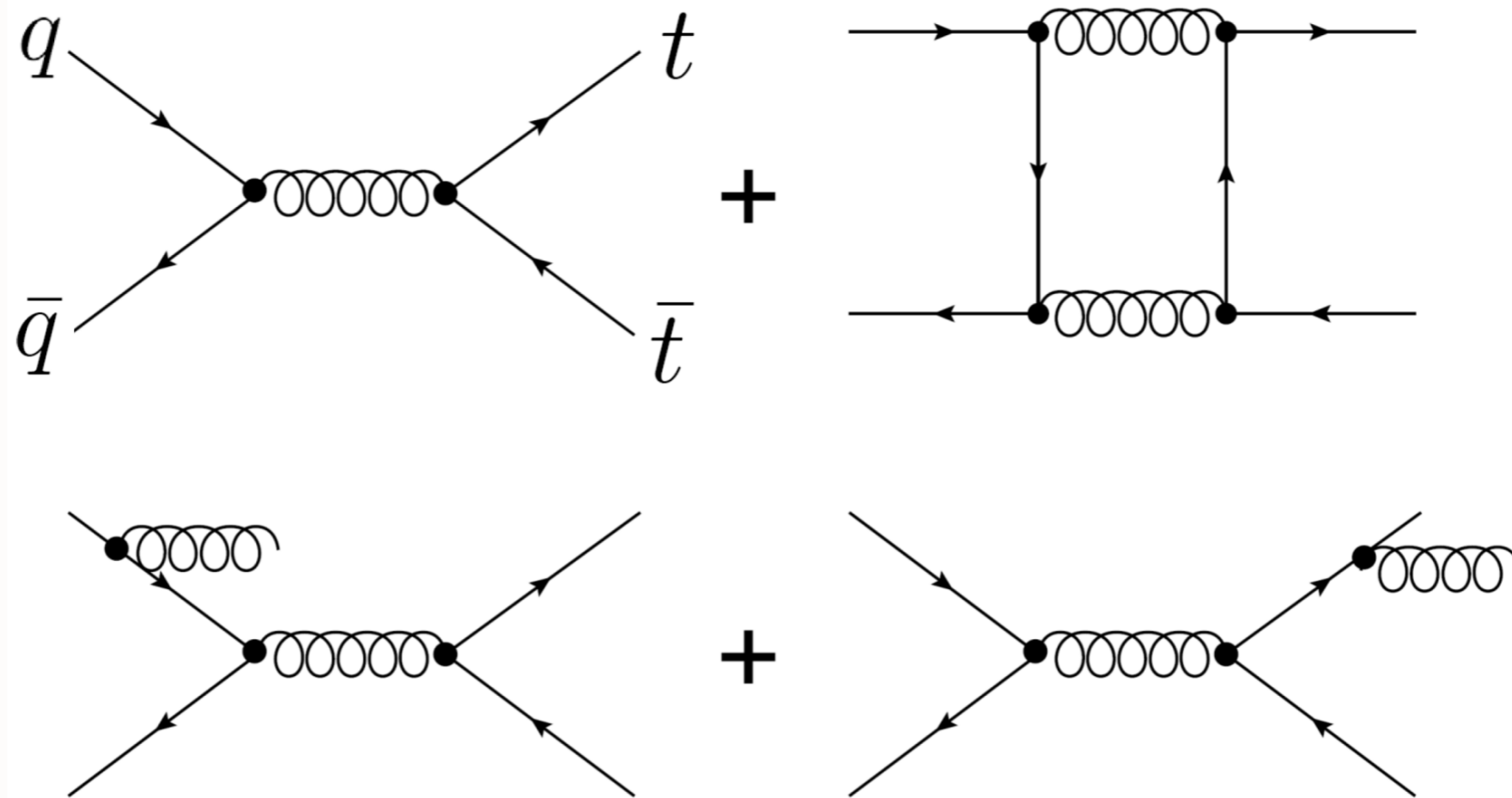


# Dynamic

- Modified by Rescattering: ISI & FSI
- Contains Wilson Line, Phases
- No Probabilistic Interpretation
- Process-Dependent - From Collision
- T-Odd (Sivers, Boer-Mulders, etc.)
- Shadowing, Anti-Shadowing, Saturation
- Sum Rules Not Proven
- DGLAP Evolution
- Hard Pomeron and Odderon Diffractive DIS



**Hwang,  
Schmidt, sjb,  
Mulders, Boer  
Qiu, Sterman  
Collins, Qiu  
Pasquini, Xiao,  
Yuan, sjb**

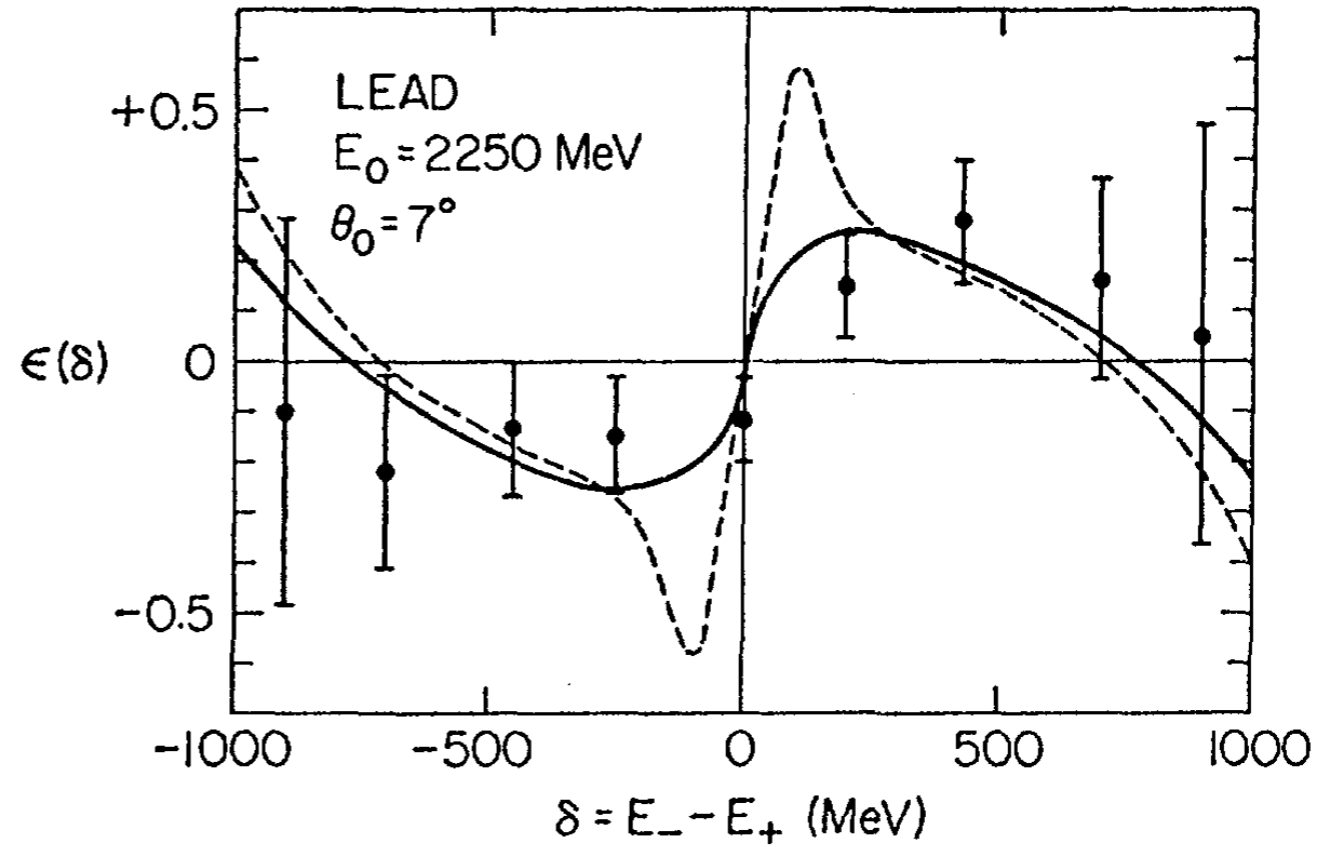
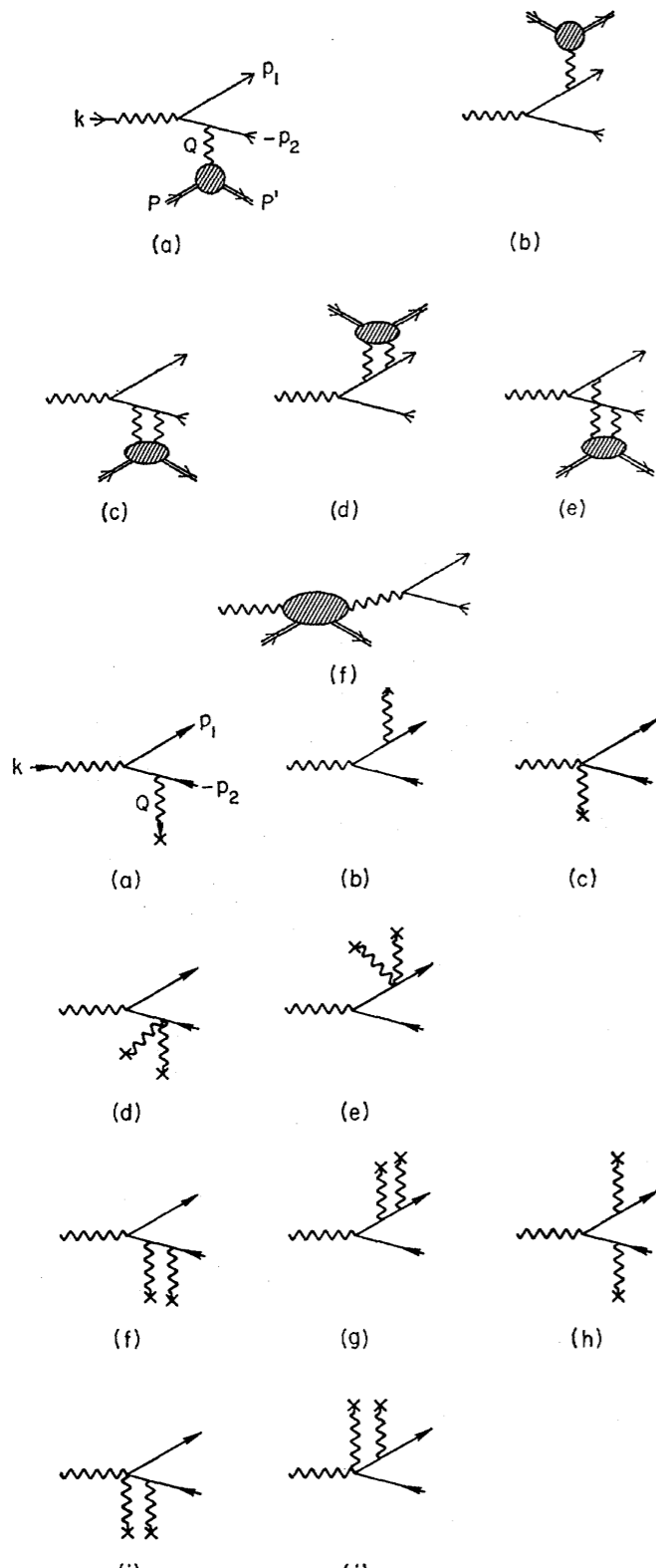


*Conventional pQCD approach*

# Second Born Corrections to Wide-Angle High-Energy Electron Pair Production and Bremsstrahlung\*

J. Gillespie and sjb

PR 173 1011 (1968)



\* J. G. Asbury, W. K. Bertram, U. Becker, P. Joos, M. Rohde, A. J. S. Smith, S. Friedlander, C. L. Jordan, and S. C. C. Ting, Phys. Rev. **161**, 1344 (1967), and references therein.

$$R \equiv \frac{d\sigma_{\text{int}}}{d\sigma_{\text{Born}}} = \frac{1}{4} Z\alpha\pi |Q| \times \left[ \frac{(E_2 - E_1)Q^2 + 2E_2 k \cdot p_2 - 2E_1 k \cdot p_1}{E_1 E_2 Q^2 + (k \cdot p_1)(k \cdot p_2)} \right] + O(Z\alpha)^3$$

(spin zero, point nucleus). (4.9)

# *QCD Analysis of heavy quark asymmetries*

B. von Harling, Y. Zhao, sjb

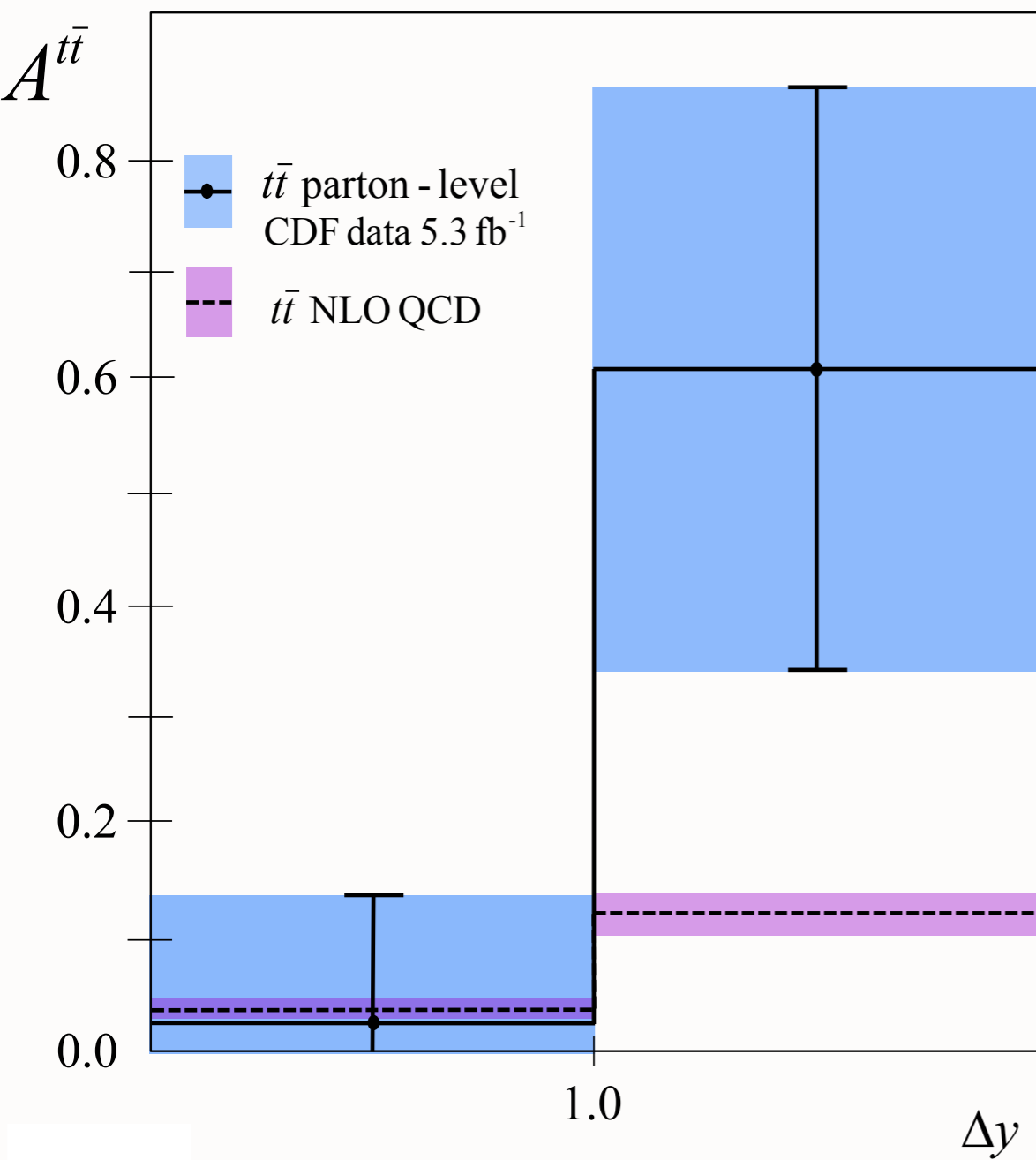
- **Include Radiation Diagrams**

- **FSI similar to Sivers Effect**

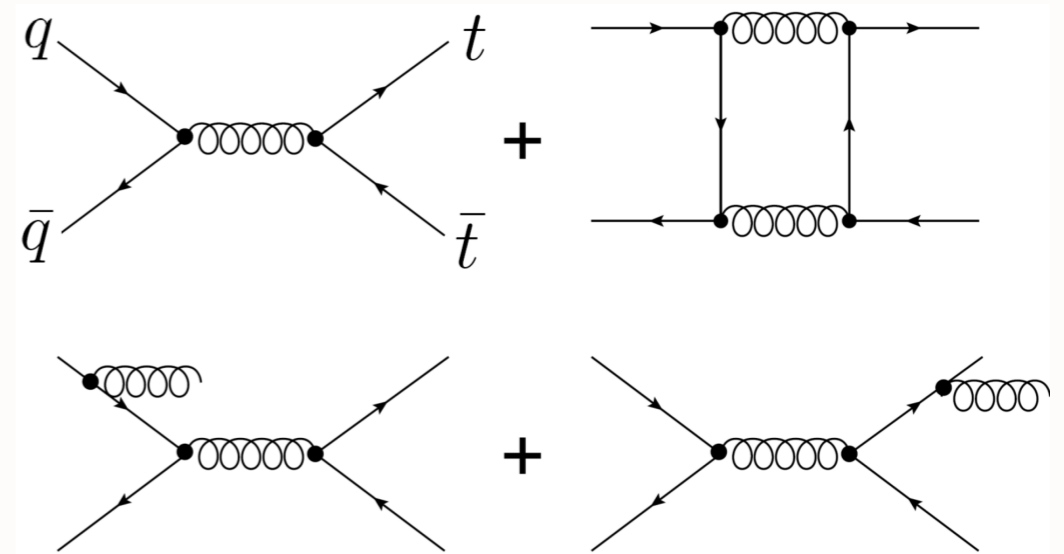
$$\pi Z \alpha \longrightarrow \pi C_F \alpha_s$$

- **Renormalization scale relatively soft**

*Large  $t\bar{t}$  asymmetries seen at CDF*

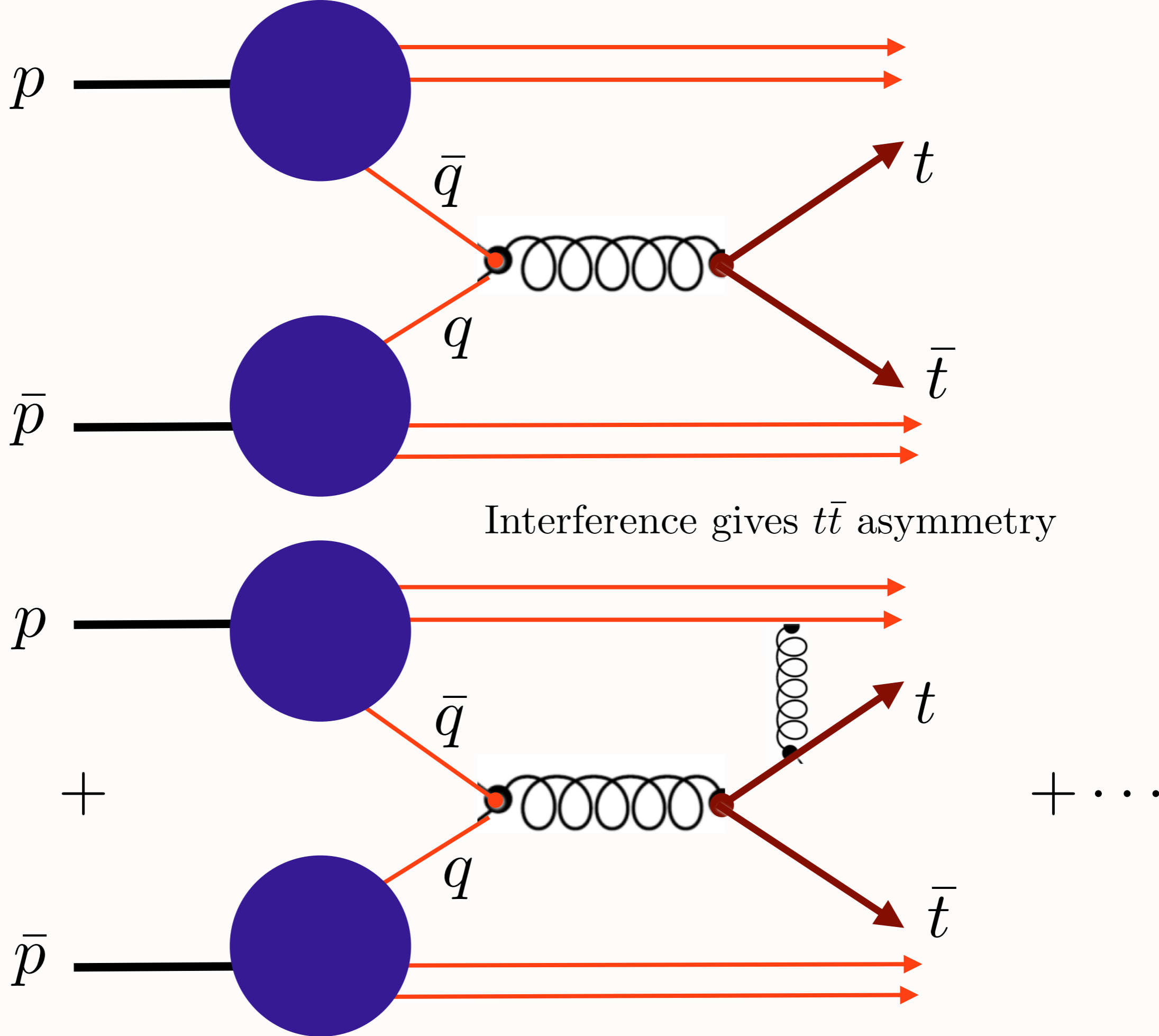


$$A^{t\bar{t}}(\Delta y_i) = \frac{N(\Delta y_i) - N(-\Delta y_i)}{N(\Delta y_i) + N(-\Delta y_i)}$$



Fermilab-Pub-10-525-E

Evidence for a Mass Dependent Forward-Backward Asymmetry  
in Top Quark Pair Production



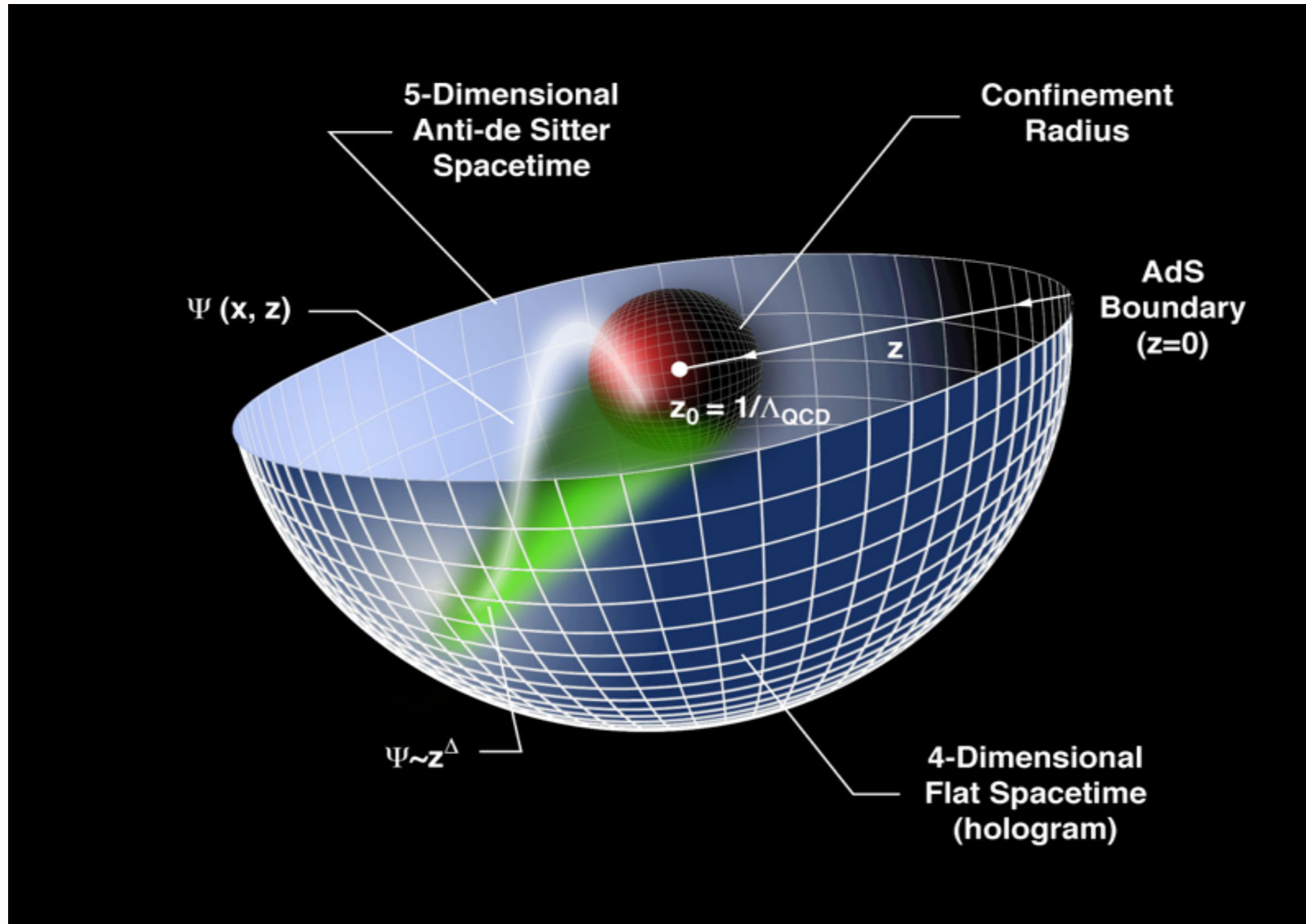


# *QCD Analysis of heavy quark asymmetries*

B. von Harling, Y. Zhao, sjb

- **Rescattering Corrections analogous to QED**  
$$\pi Z \alpha \rightarrow \pi C_F \alpha_s$$
- **Include Radiation Diagrams**
- **Top Decay truncates gluon radiation**
- **FSI similar to Sivers Effect**
- **Renormalization scale relatively soft**

# Applications of AdS/CFT to QCD



*Changes in physical length scale mapped to evolution in the 5th dimension  $z$*

**in collaboration with Guy de Teramond**

Warsaw  
July 6, 2012

Hot Topics in QCD Phenomenology  
162

Stan Brodsky

SLAC  
NATIONAL ACCELERATOR LABORATORY

## Soft-Wall Model

$$S = \int d^4x dz \sqrt{g} e^{\varphi(z)} \mathcal{L}, \quad \varphi(z) = \pm \kappa^2 z^2$$

**Retain conformal AdS metrics but introduce smooth cutoff which depends on the profile of a dilaton background field**

Karch, Katz, Son and Stephanov (2006)]

- Equation of motion for scalar field  $\mathcal{L} = \frac{1}{2} (g^{\ell m} \partial_\ell \Phi \partial_m \Phi - \mu^2 \Phi^2)$

$$[z^2 \partial_z^2 - (3 \mp 2\kappa^2 z^2) z \partial_z + z^2 \mathcal{M}^2 - (\mu R)^2] \Phi(z) = 0$$

with  $(\mu R)^2 \geq -4$ .

- LH holography requires 'plus dilaton'  $\varphi = +\kappa^2 z^2$ . Lowest possible state  $(\mu R)^2 = -4$

$$\mathcal{M}^2 = 0, \quad \Phi(z) \sim z^2 e^{-\kappa^2 z^2}, \quad \langle r^2 \rangle \sim \frac{1}{\kappa^2}$$

A chiral symmetric bound state of two massless quarks with scaling dimension 2:

*Massless pion*

$$e^{\Phi(z)} = e^{+\kappa^2 z^2}$$

*AdS Soft-Wall Schrodinger Equation for bound state of two scalar constituents:*

$$\left[ -\frac{d^2}{dz^2} - \frac{1 - 4L^2}{4z^2} + U(z) \right] \phi(z) = \mathcal{M}^2 \phi(z)$$

$$U(z) = \kappa^4 z^2 + 2\kappa^2 (L + S - 1)$$

*Derived from variation of Action  
Dilaton-Modified AdS<sub>5</sub>*

## Bosonic Modes and Meson Spectrum

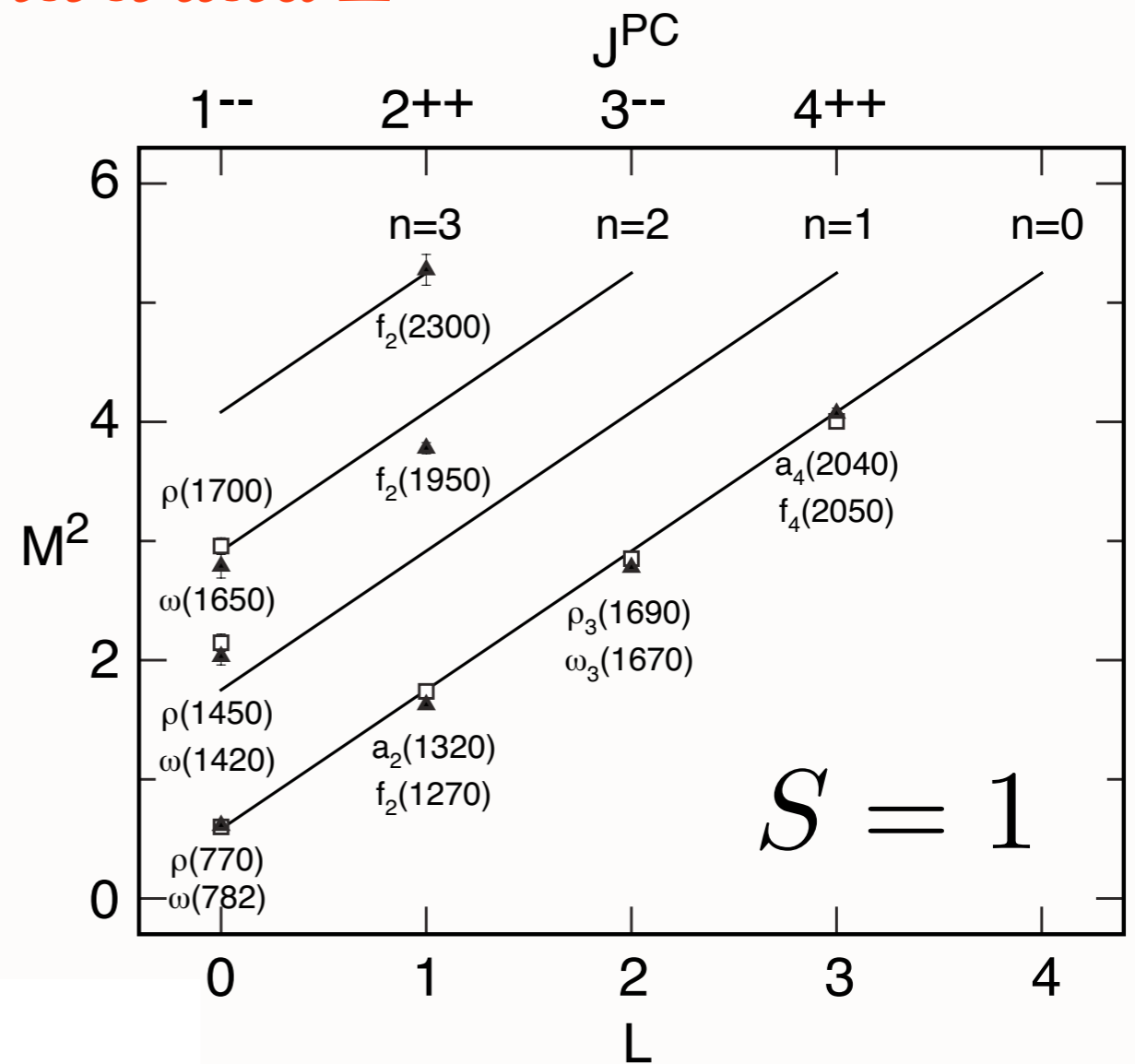
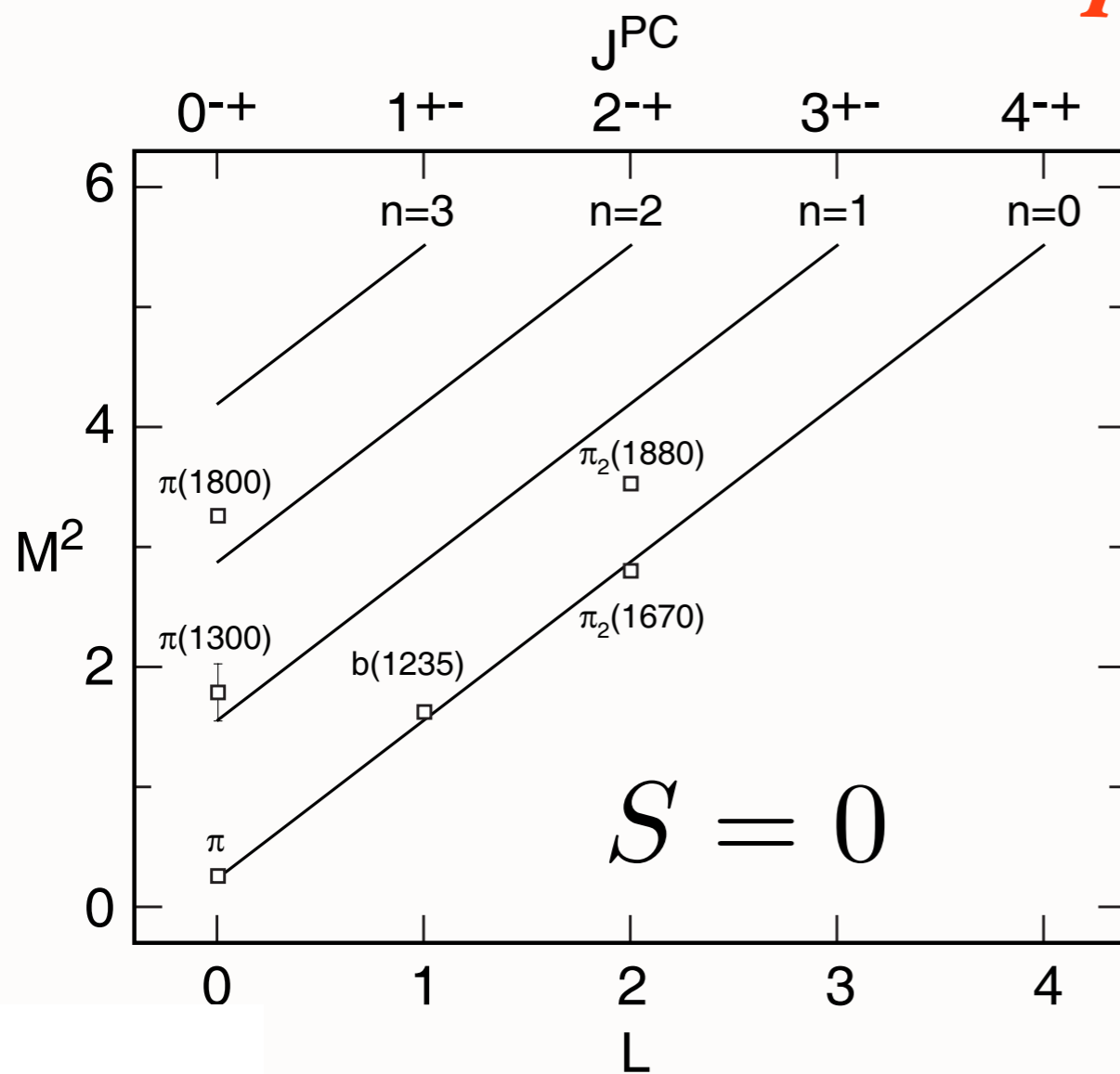
$$\mathcal{M}^2 = 4\kappa^2(n + J/2 + L/2) \rightarrow 4\kappa^2(n + L + S/2)$$

$4\kappa^2$  for  $\Delta n = 1$

$4\kappa^2$  for  $\Delta L = 1$

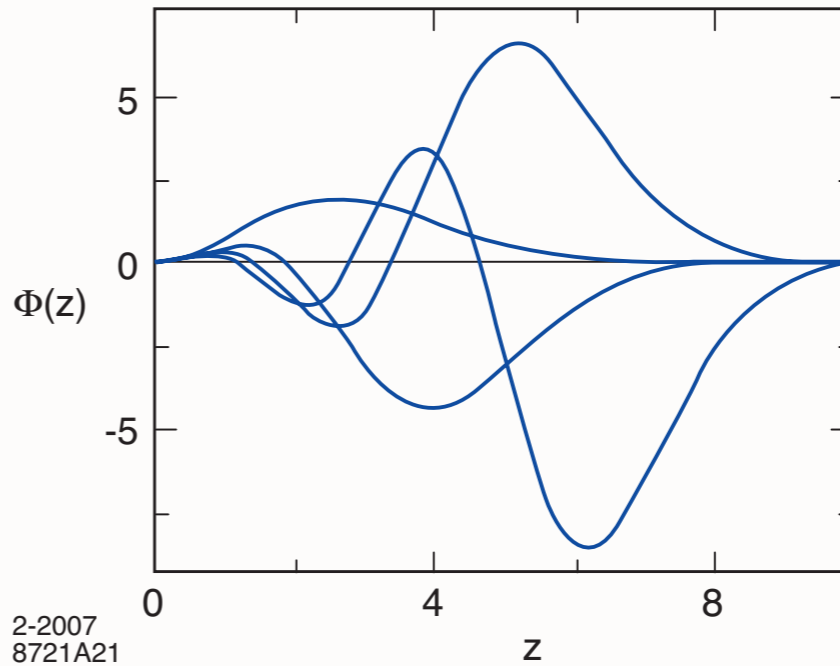
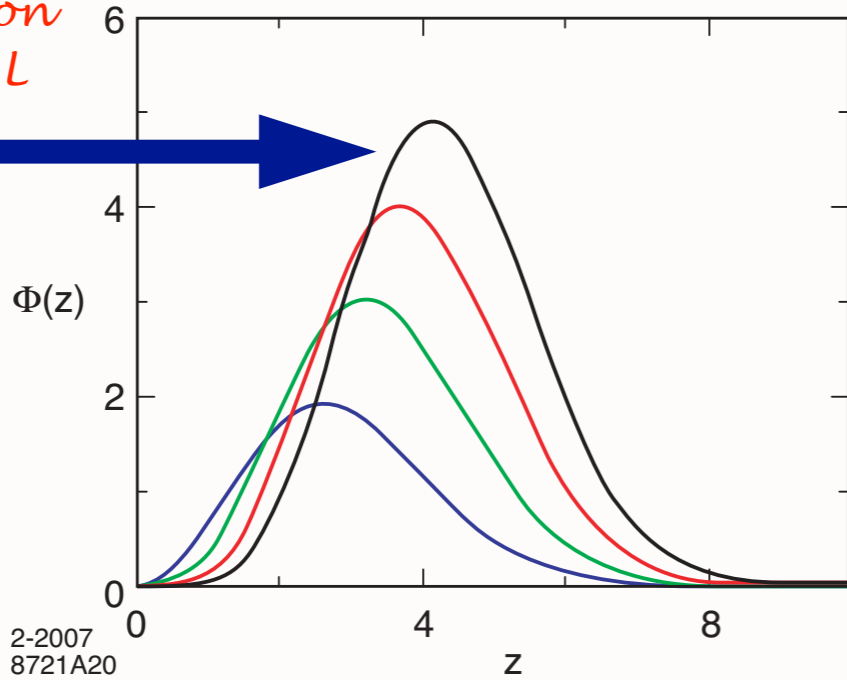
$2\kappa^2$  for  $\Delta S = 1$

*Same slope in  $n$  and  $L$*



Regge trajectories for the  $\pi$  ( $\kappa = 0.6$  GeV) and the  $I = 1$   $\rho$ -meson and  $I = 0$   $\omega$ -meson families ( $\kappa = 0.54$  GeV)

Quark separation increases with  $L$

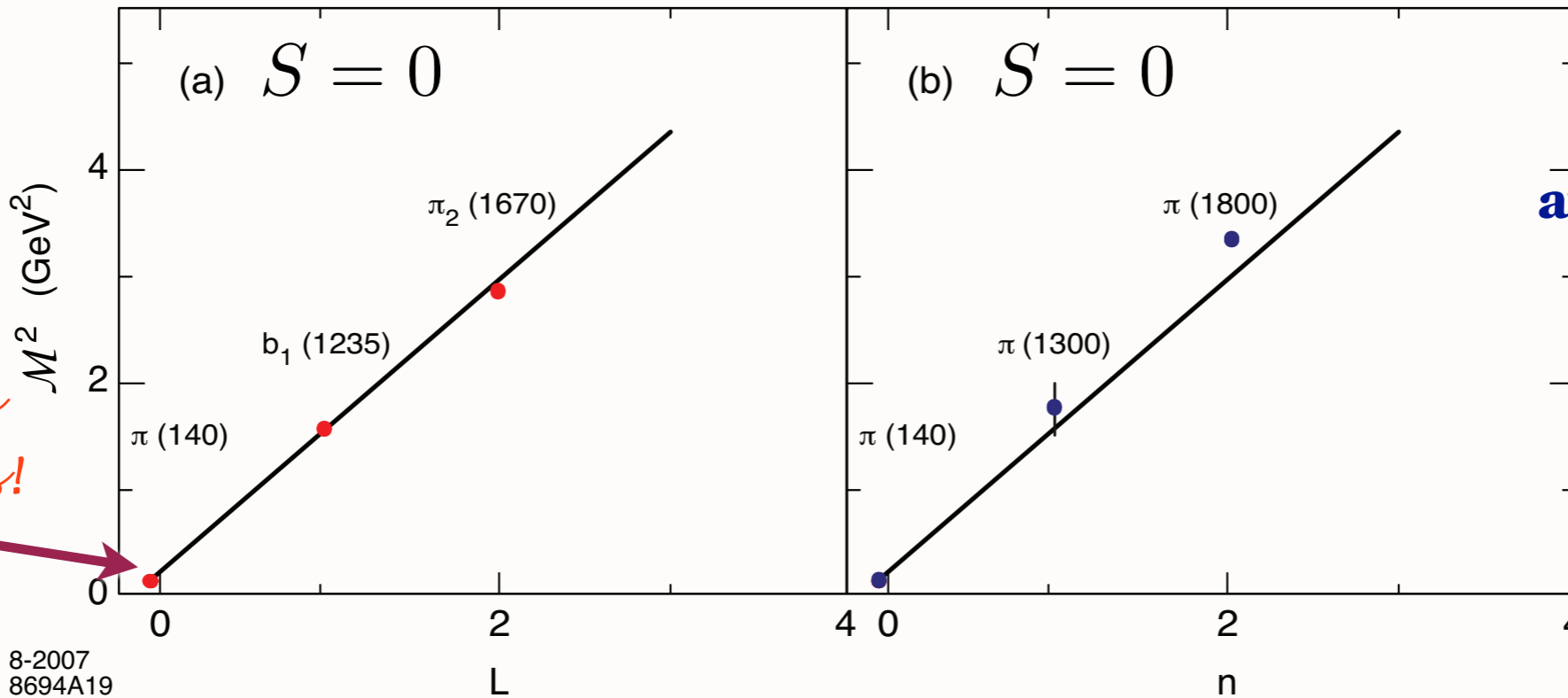


2-2007  
8721A20

2-2007  
8721A21

Fig: Orbital and radial AdS modes in the soft wall model for  $\kappa = 0.6$  GeV .

Soft Wall Model



Pion has zero mass!

8-2007  
8694A19

Pion mass automatically zero

$$m_q = 0$$

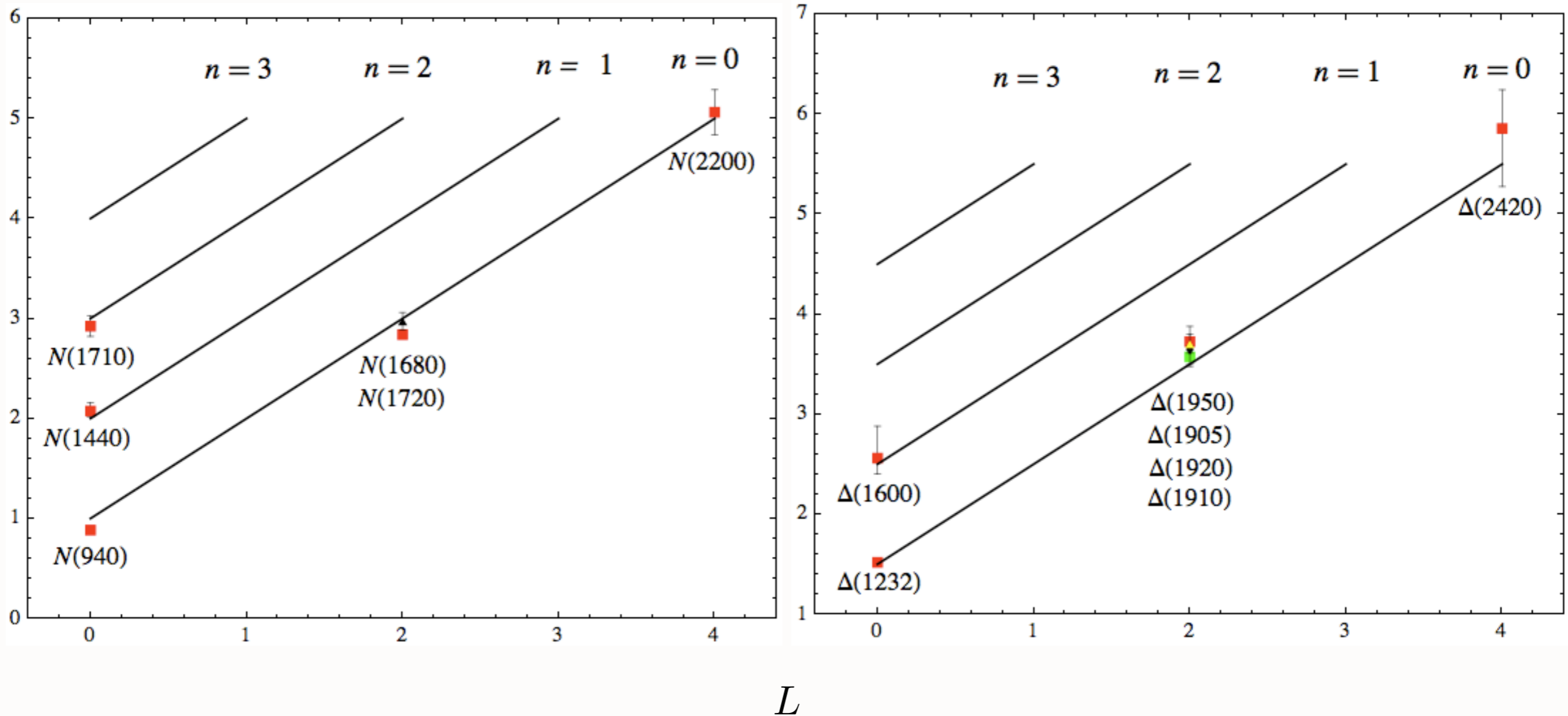
Light meson orbital (a) and radial (b) spectrum for  $\kappa = 0.6$  GeV.

- $\Delta$  spectrum identical to Forkel and Klempt, Phys. Lett. B 679, 77 (2009)

$$4\kappa^2 \text{ for } \Delta n = 1$$

$$4\kappa^2 \text{ for } \Delta L = 1$$

$$2\kappa^2 \text{ for } \Delta S = 1$$

$$\mathcal{M}^2$$


Parent and daughter 56 Regge trajectories for the  $N$  and  $\Delta$  baryon families for  $\kappa = 0.5$  GeV

$LF(3+1)$

$AdS_5$

$$\psi(x, \vec{b}_\perp)$$

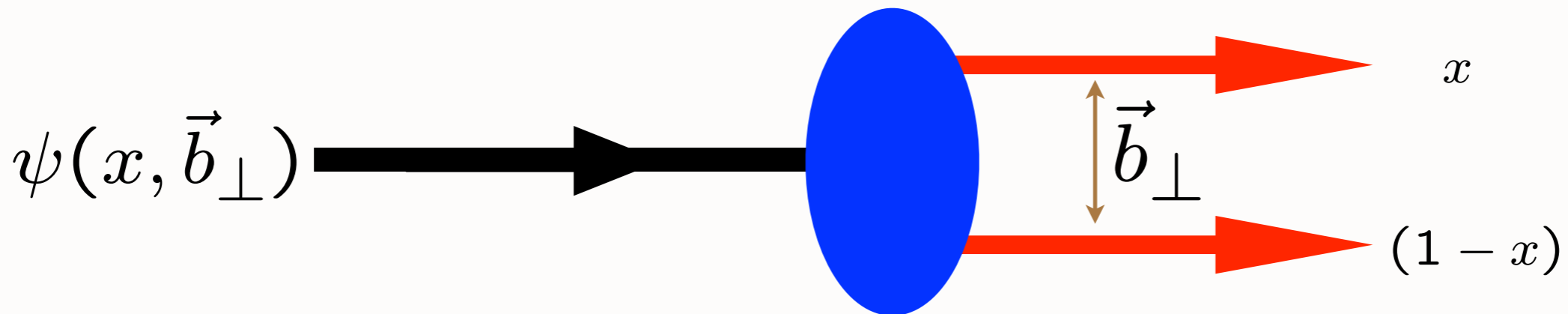


$$\phi(z)$$

$$\zeta = \sqrt{x(1-x)b_\perp^2}$$



$$z$$



$$\psi(x, \zeta) = \sqrt{x(1-x)} \zeta^{-1/2} \phi(\zeta)$$

*Light-Front Holography: Unique mapping derived from equality of LF and AdS formula for current matrix elements*



$H_{QED}$

*QED atoms: positronium and muonium*

$$(H_0 + H_{int}) |\Psi\rangle = E |\Psi\rangle$$

*Coupled Fock states*

$$\left[ -\frac{\Delta^2}{2m_{\text{red}}} + V_{\text{eff}}(\vec{S}, \vec{r}) \right] \psi(\vec{r}) = E \psi(\vec{r})$$

*Effective two-particle equation*

**Includes Lamb Shift, quantum corrections**

$$\left[ -\frac{1}{2m_{\text{red}}} \frac{d^2}{dr^2} + \frac{1}{2m_{\text{red}}} \frac{l(l+1)}{r^2} + V_{\text{eff}}(r, S, l) \right] \psi(r) = E \psi(r)$$

*Spherical Basis*  $r, \theta, \phi$

*Coulomb potential*

**Bohr Spectrum**

$$V_{\text{eff}} \rightarrow V_C(r) = -\frac{\alpha}{r}$$

*Semiclassical first approximation to QED*

$$H_{QCD}^{LF}$$

QCD Meson Spectrum

$$(H_{LF}^0 + H_{LF}^I) |\Psi\rangle = M^2 |\Psi\rangle$$

Coupled Fock states

$$\left[ \frac{\vec{k}_\perp^2 + m^2}{x(1-x)} + V_{\text{eff}}^{LF} \right] \psi_{LF}(x, \vec{k}_\perp) = M^2 \psi_{LF}(x, \vec{k}_\perp)$$

Effective two-particle equation

$$\zeta^2 = x(1-x)b_\perp^2$$

$$\left[ -\frac{d^2}{d\zeta^2} + \frac{-1 + 4L^2}{\zeta^2} + U(\zeta, S, L) \right] \psi_{LF}(\zeta) = M^2 \psi_{LF}(\zeta)$$

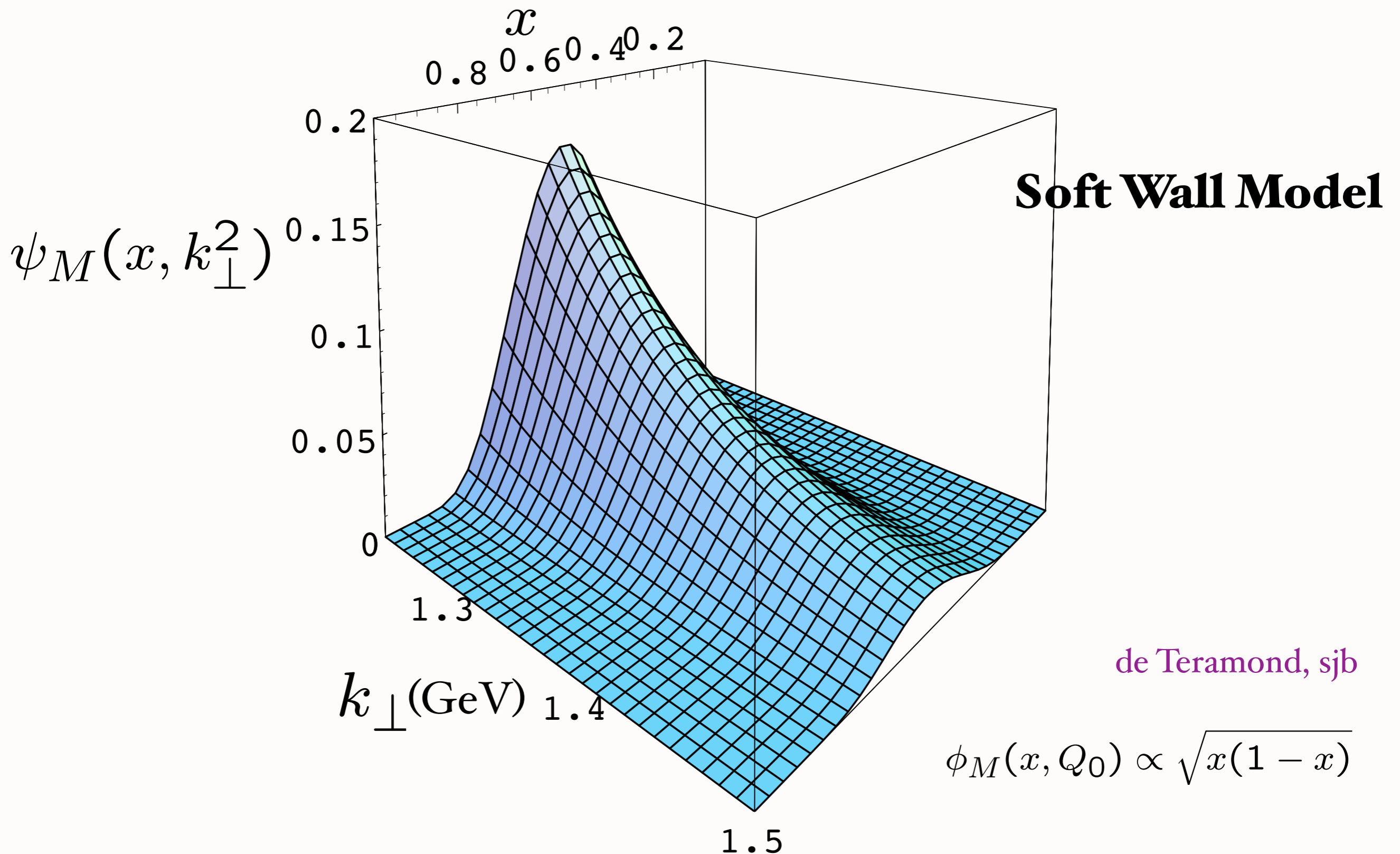
Azimuthal Basis  $\zeta, \phi$

$$U(\zeta, S, L) = \kappa^2 \zeta^2 + \kappa^2 (L + S - 1/2)$$

Semiclassical first approximation to QCD

Confining AdS/QCD potential

# Prediction from AdS/CFT: Meson LFWF



de Teramond, sjb

$$\phi_M(x, Q_0) \propto \sqrt{x(1-x)}$$

Increases PQCD prediction for  $F_{\pi}(Q^2)$  by 16/9

Warsaw  
July 6, 2012

Hot Topics in QCD Phenomenology

171

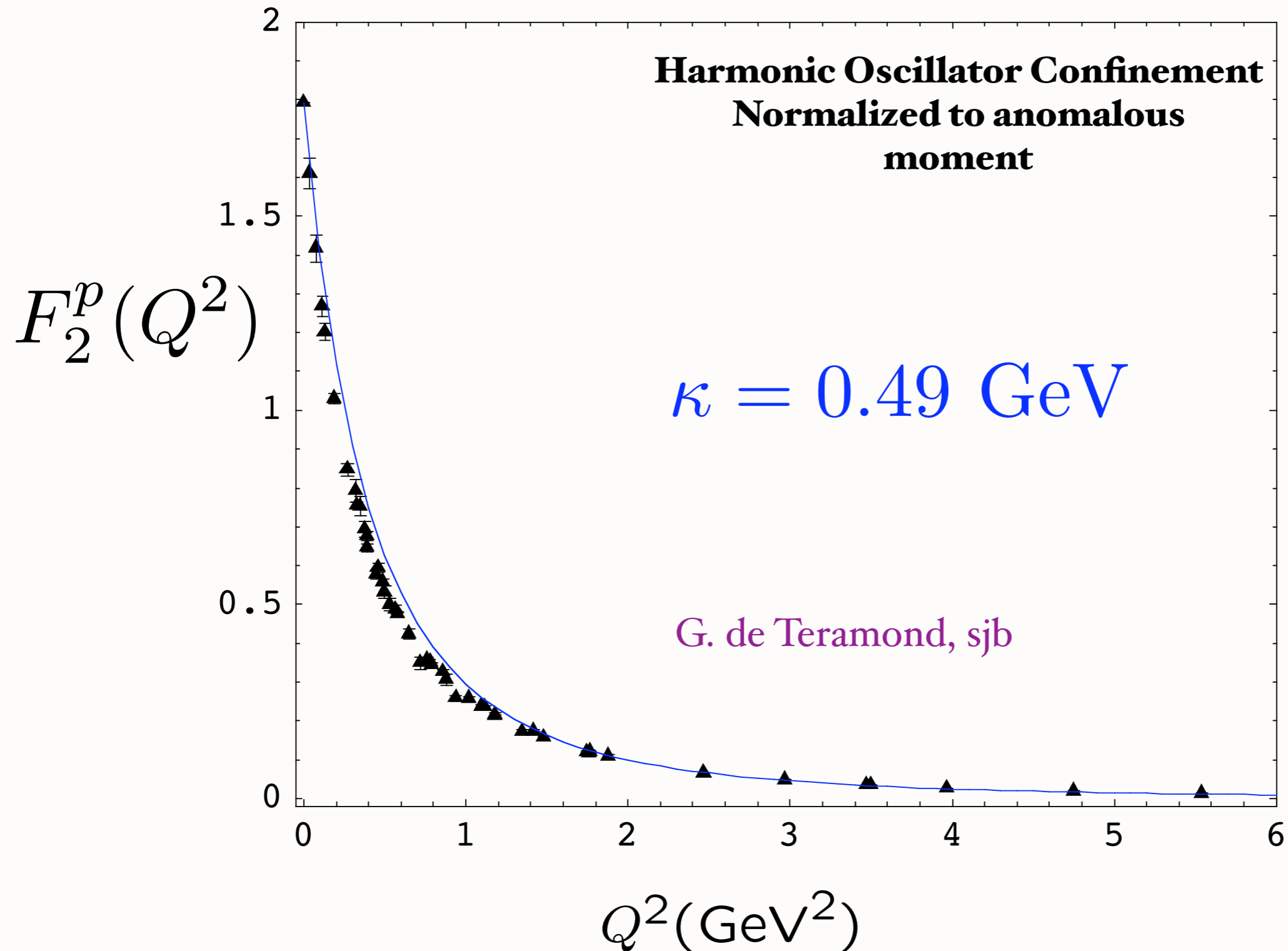
Stan Brodsky

SLAC  
NATIONAL ACCELERATOR LABORATORY

# Spacelike Pauli Form Factor

Preliminary

From overlap of  $L = 1$  and  $L = 0$  LFWFs



Warsaw  
July 6, 2012

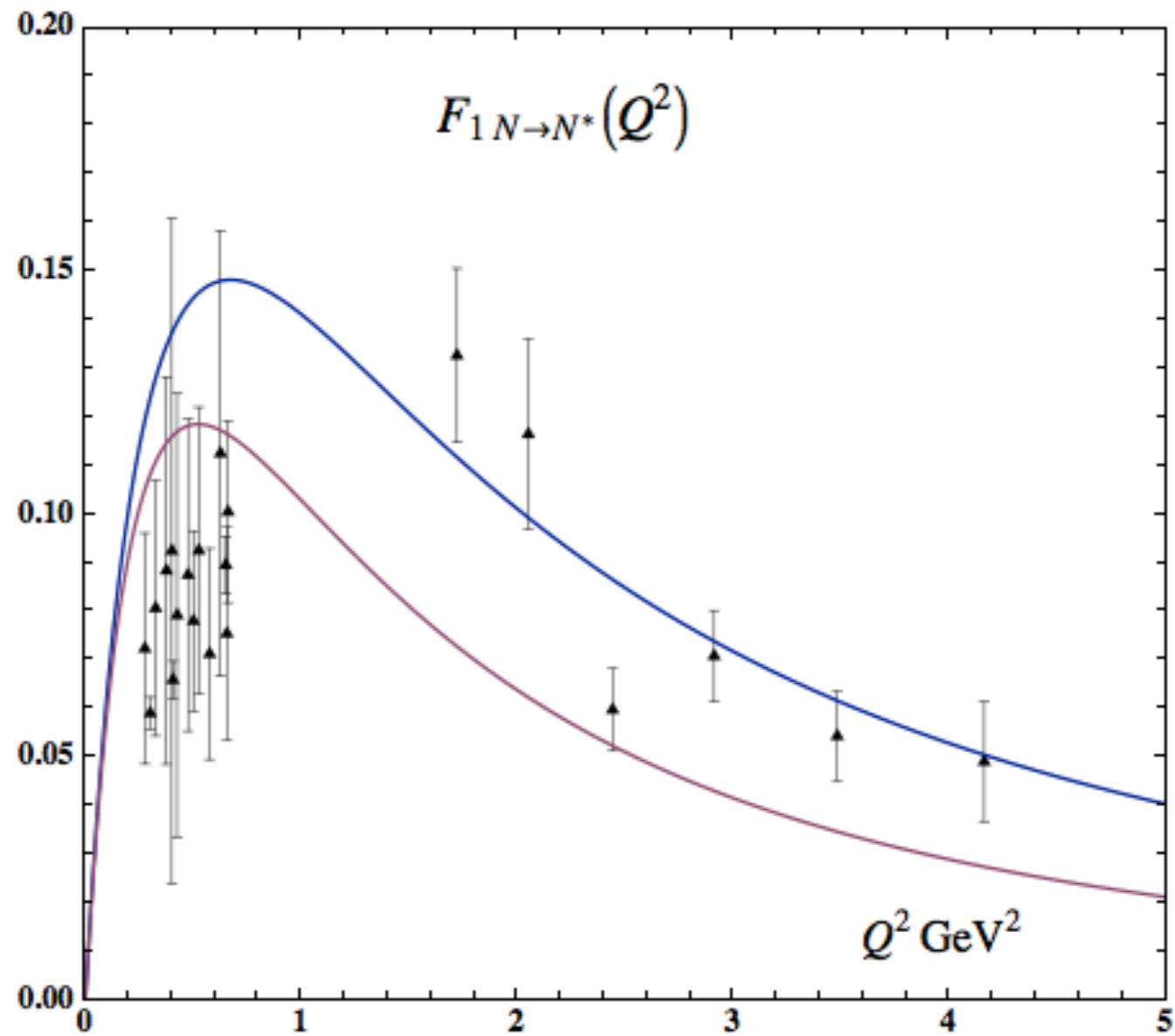
Hot Topics in QCD Phenomenology  
172

Stan Brodsky

SLAC  
NATIONAL ACCELERATOR LABORATORY

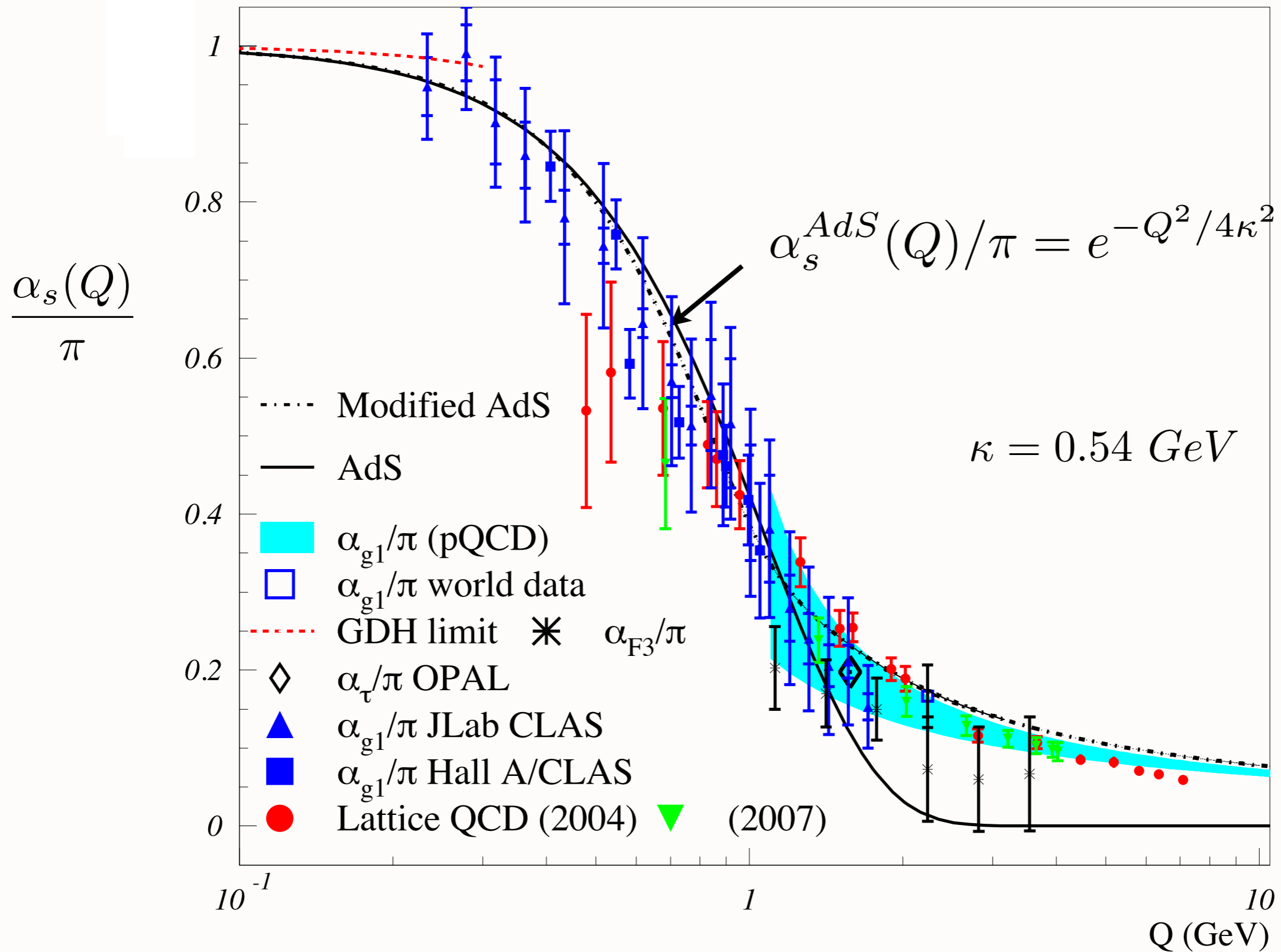
$$F_{1N \rightarrow N^*}(Q^2) = \frac{2\sqrt{2}}{3} \frac{\frac{Q^2}{M_\rho^2}}{\left(1 + \frac{Q^2}{M_\rho^2}\right) \left(1 + \frac{Q^2}{M_{\rho'}^2}\right) \left(1 + \frac{Q^2}{M_{\rho''}^2}\right)}$$

## Nucleon Transition Form Factor



# Running Coupling from Light-Front Holography and AdS/QCD

**Analytic, defined at all scales, IR Fixed Point**



# *Applications of Nonperturbative Running Coupling from AdS/QCD*

- **Sivers Effect in SIDIS, Drell-Yan**
- **Double Boer-Mulders Effect in DY**
- **Diffraction DIS**
- **Heavy Quark Production at Threshold**

*All involve gluon exchange at small  
momentum transfer*

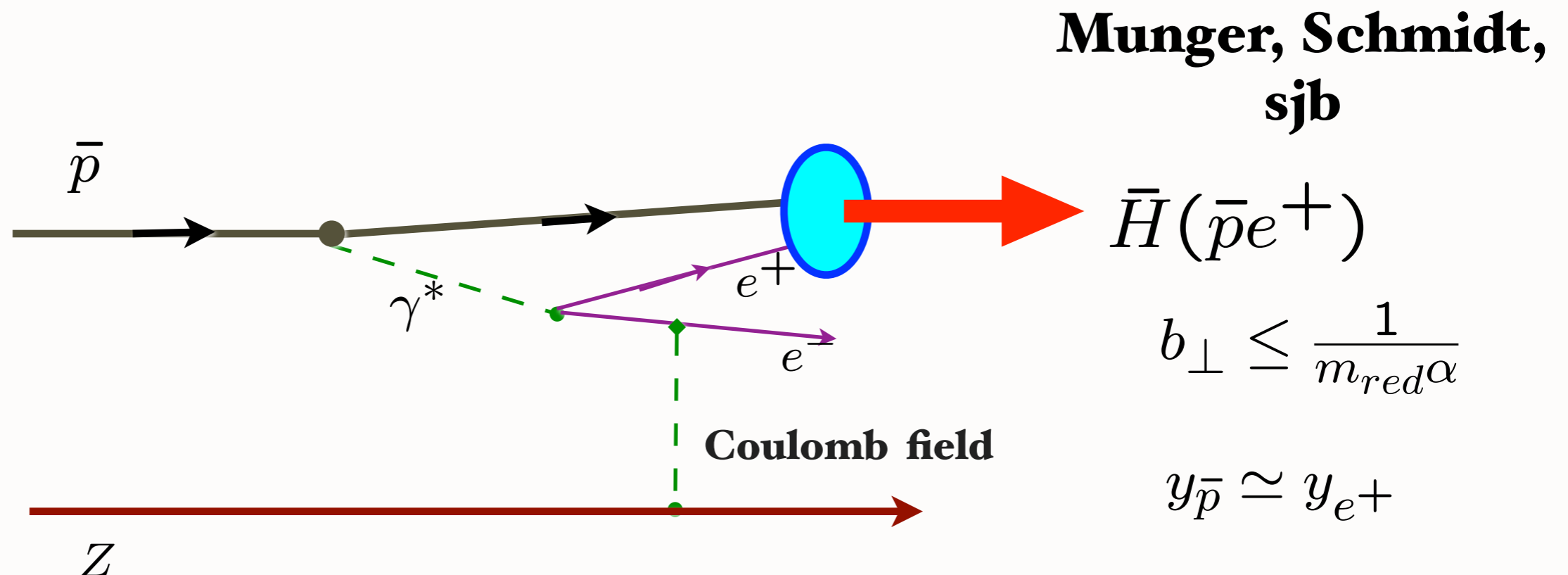
# Features of Soft-Wall AdS/QCD

- **Single-variable frame-independent radial Schrodinger equation**
- **Massless pion ( $m_q = 0$ )**
- **Regge Trajectories: universal slope in  $n$  and  $L$**
- **Valid for all integer  $J$  &  $S$ .**
- **Dimensional Counting Rules for Hard Exclusive Processes**
- **Phenomenology: Space-like and Time-like Form Factors**
- **LF Holography: LFWFs; broad distribution amplitude**
- **No large  $N_c$  limit required**
- **Add quark masses to LF kinetic energy**
- **Systematically improvable -- diagonalize  $H_{LF}$  on AdS basis**



# Formation of Relativistic Anti-Hydrogen

Measured at CERN-LEAR and FermiLab

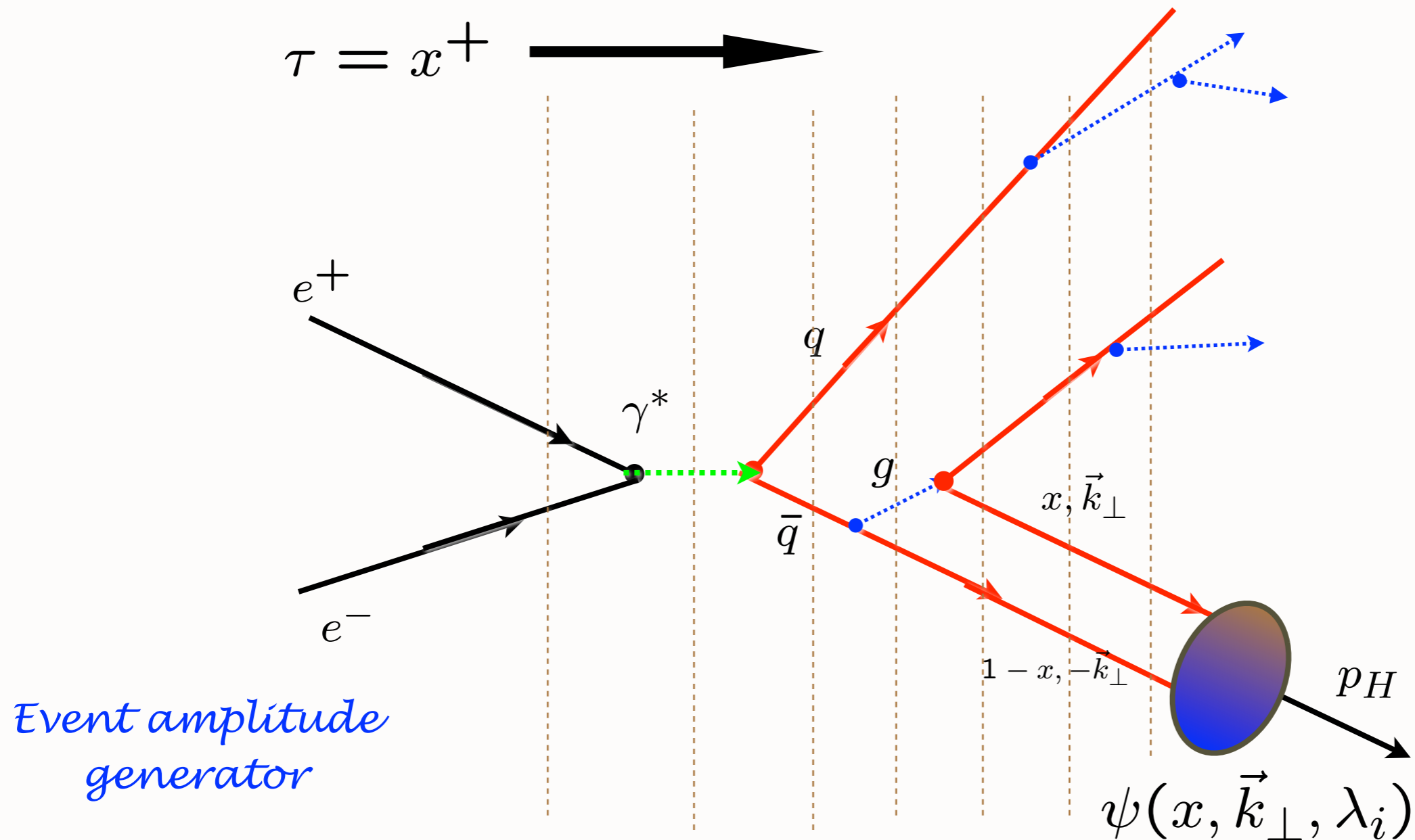


*Coalescence of off-shell co-moving positron and antiproton*

*Wavefunction maximal at small impact separation and equal rapidity*

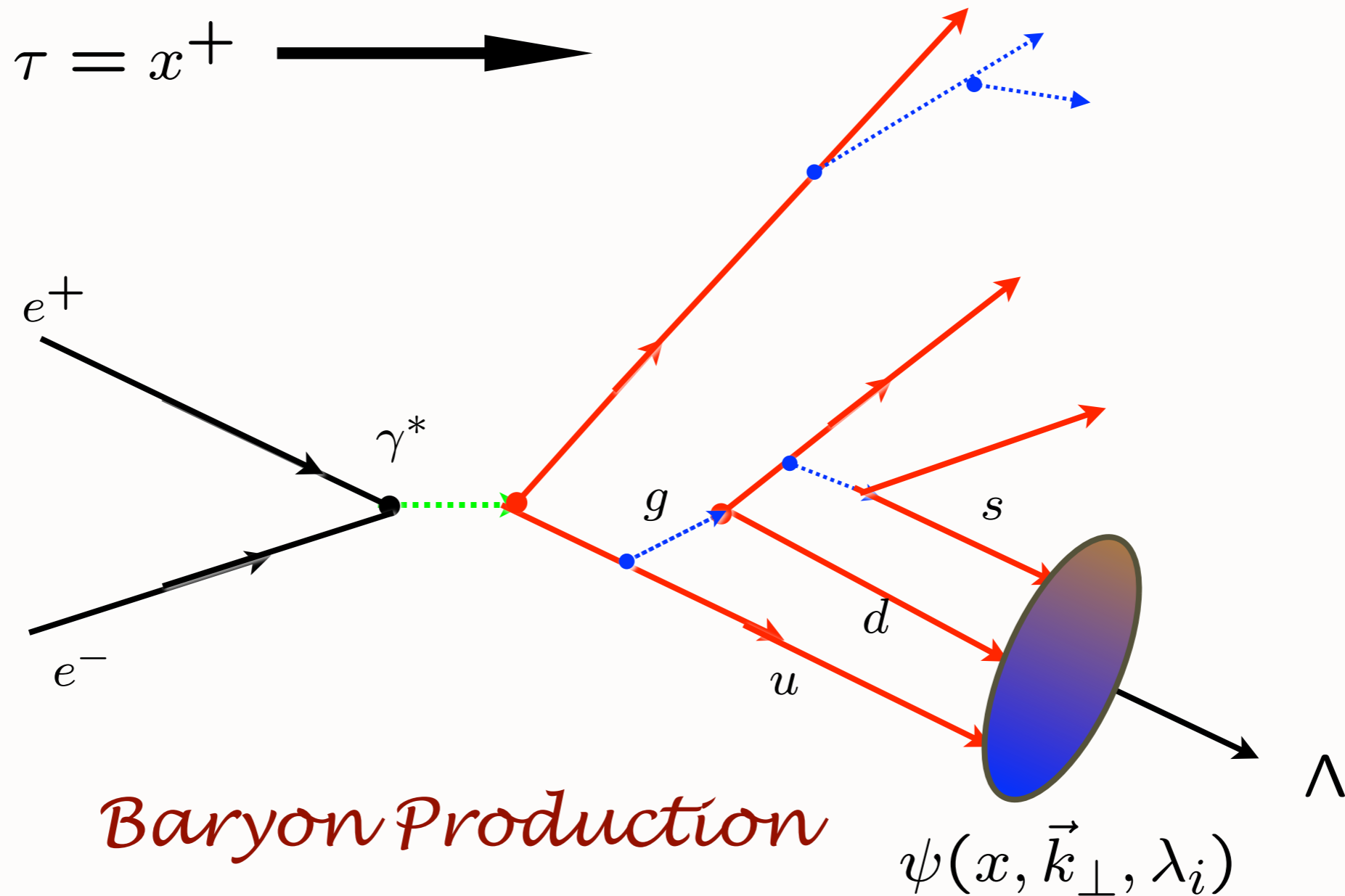
*“Hadronization” at the Amplitude Level*

# Hadronization at the Amplitude Level



**Construct helicity amplitude using Light-Front Perturbation theory; coalesce quarks via LFWFs**

# Hadronization at the Amplitude Level

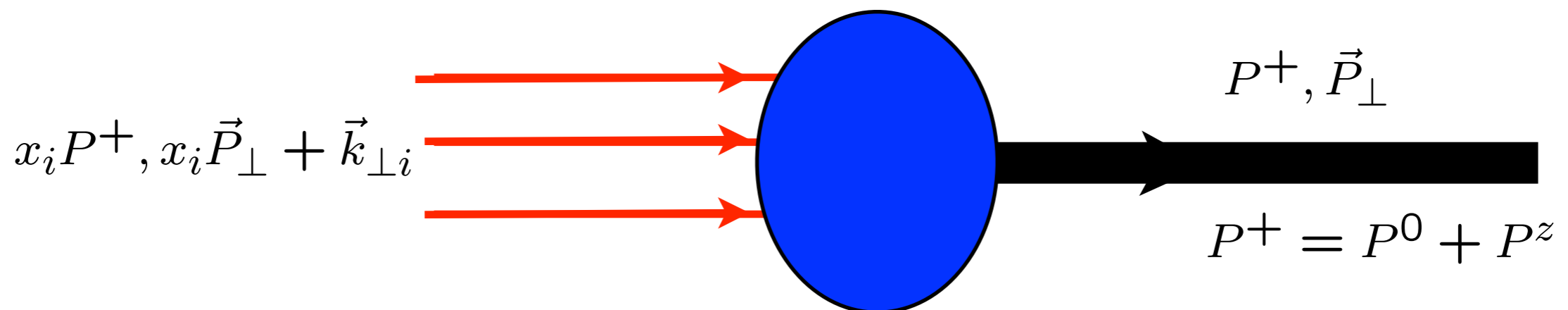


Construct helicity amplitude using Light-Front Perturbation theory; coalesce quarks via LFWFs

# Features of LF T-Matrix Formalism

## “Event Amplitude Generator”

- Same principle as antihydrogen production: off-shell coalescence
- coalescence to hadron favored at equal rapidity, small transverse momenta
- leading heavy hadron production: D and B mesons produced at large  $z$
- hadron helicity conservation if hadron LFWF has  $L^z = 0$
- Baryon AdS/QCD LFWF has aligned and anti-aligned quark spin



# “One of the gravest puzzles of theoretical physics”

## DARK ENERGY AND THE COSMOLOGICAL CONSTANT PARADOX

A. ZEE

*Department of Physics, University of California, Santa Barbara, CA 93106, USA  
Kavil Institute for Theoretical Physics, University of California,  
Santa Barbara, CA 93106, USA  
zee@kitp.ucsb.edu*

$$(\Omega_{\Lambda})_{QCD} \sim 10^{45}$$

$$(\Omega_{\Lambda})_{EW} \sim 10^{56}$$

$$\Omega_{\Lambda} = 0.76(\text{expt})$$

$$(\Omega_{\Lambda})_{QCD} \propto \langle 0 | q\bar{q} | 0 \rangle^4$$

*QCD Problem Solved if quark and gluon condensates reside within hadrons, not vacuum!*

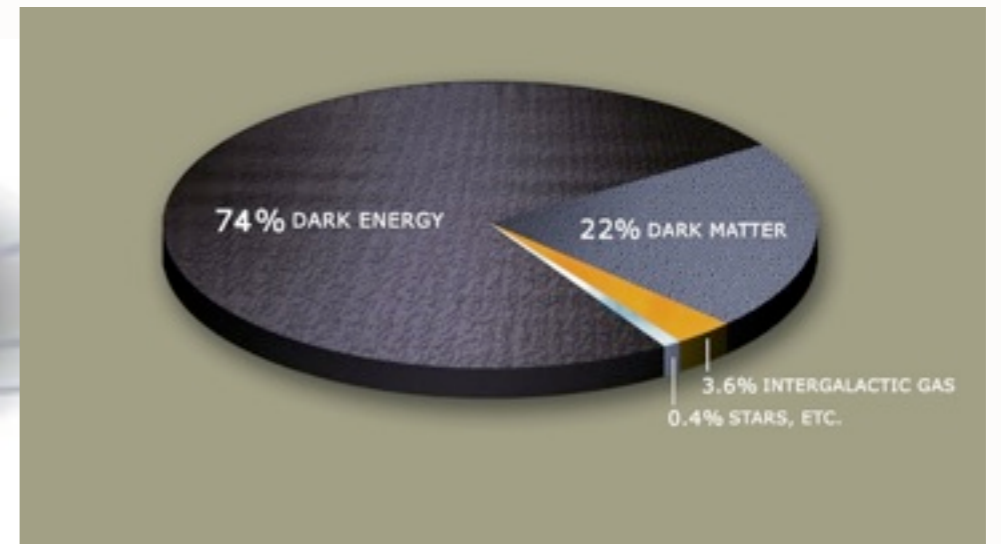
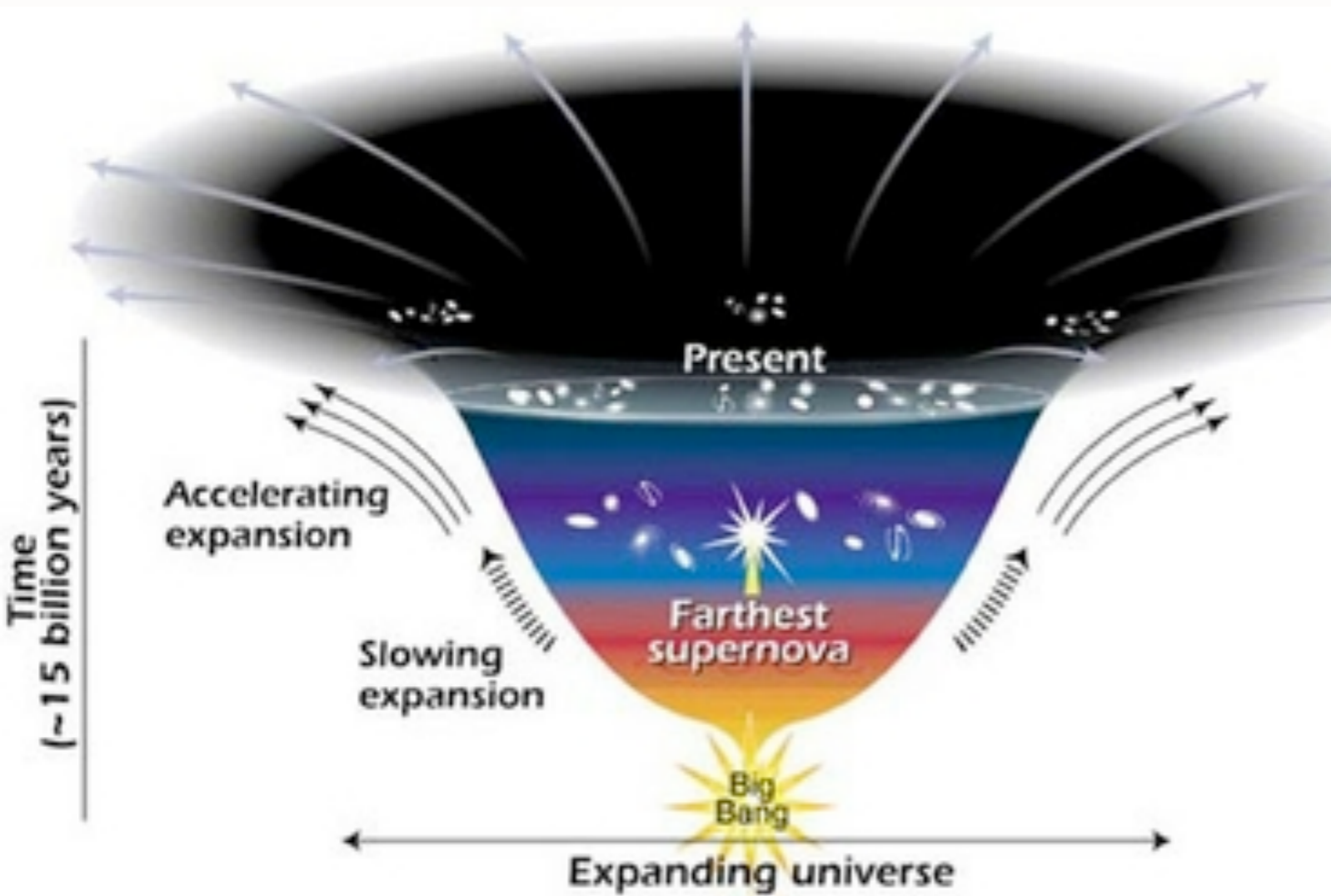
**R. Shrock, sjb** Proc.Nat.Acad.Sci. 108 (2011) 45-50

“Condensates in Quantum Chromodynamics and the Cosmological Constant”

**C. Roberts, R. Shrock, P. Tandy, sjb**

Phys.Rev. C82 (2010) 022201

“New Perspectives on the Quark Condensate”



$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R - \Lambda g_{\mu\nu} = (8\pi G_N)T_{\mu\nu}$$



Dark energy/cosmological constant causes accelerating expansion

$$\frac{1}{a} \frac{d^2}{dt^2} a = \Lambda/3 = (8\pi)G_N \rho_\Lambda/3$$

*If the vacuum energy  $\rho$  is due to QCD condensates*

$$\rho_\Lambda^{\text{QCD}} \simeq M_{\text{QCD}}^4 \simeq 10^{45} \rho_\Lambda^{\text{obs}} !$$

$$\Omega_\Lambda = \frac{\rho_\Lambda^{\text{obs}}}{\rho_c} \simeq 0.76$$

$$\rho_c = \frac{3H_0^2}{8\pi G_N}$$

# Gell-Mann Oakes Renner Formula in QCD

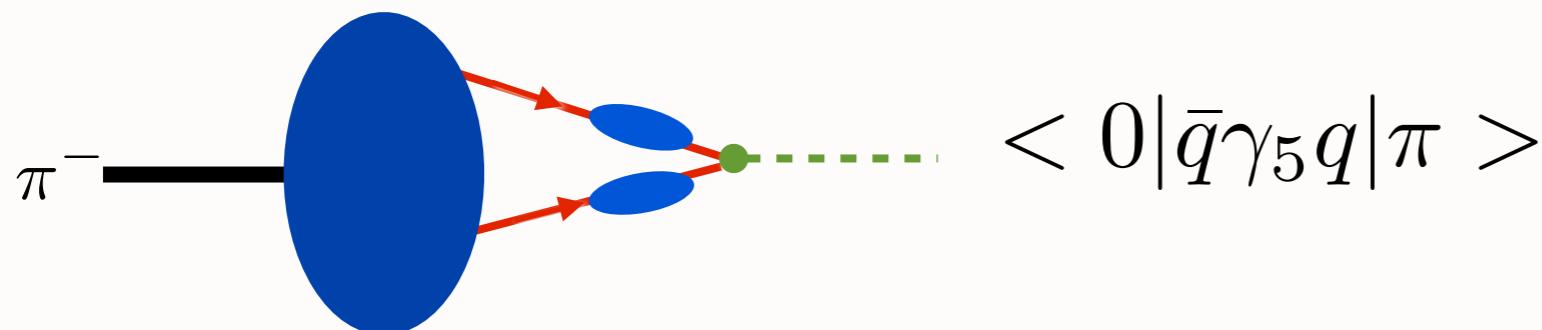
$$m_\pi^2 = -\frac{(m_u + m_d)}{f_\pi^2} \langle 0 | \bar{q}q | 0 \rangle$$

**current algebra:  
effective pion field**

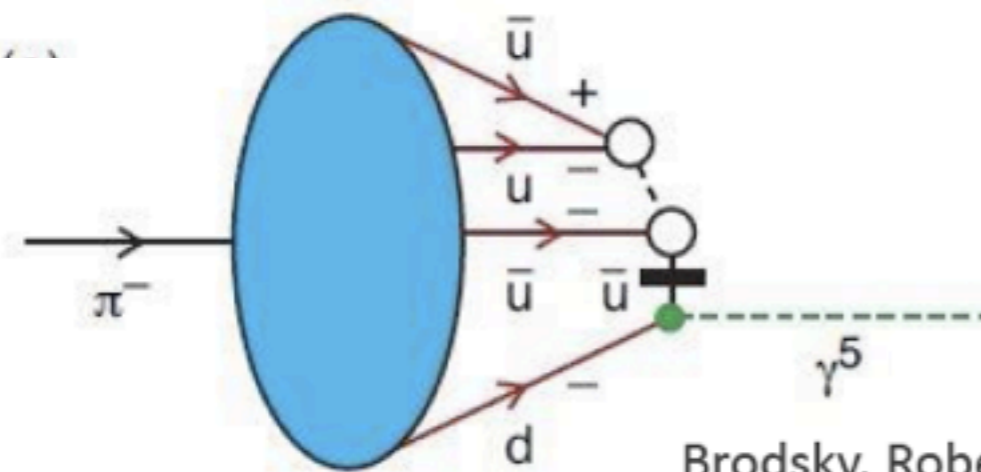
$$m_\pi^2 = -\frac{(m_u + m_d)}{f_\pi} \langle 0 | i\bar{q}\gamma_5 q | \pi \rangle$$

**QCD: composite pion  
Bethe-Salpeter Eq.**

*vacuum condensate actually is an "in-hadron condensate"*



Maris, Roberts, Tandy



# Paradigm shift: In-Hadron Condensates

Brodsky, Roberts, Shrock, Tandy, Phys. Rev. C82 (Rapid Comm.) (2010) 022201  
 Brodsky and Shrock, arXiv:0905.1151 [hep-th], to appear in PNAS

## ■ Resolution

- Whereas it might sometimes be convenient in computational truncation schemes to imagine otherwise, “condensates” do not exist as spacetime-independent mass-scales that fill all spacetime.
- *So-called* vacuum condensates can be understood as a property of hadrons themselves, which is expressed, for example, in their Bethe-Salpeter or light-front wavefunctions.
- No qualitative difference between  $f_\pi$  and  $\rho_\pi$

### Chiral limit

$$\kappa_\pi(0; \zeta) = - \langle \bar{q}q \rangle_\zeta^0$$



PHYSICAL REVIEW C **82**, 022201(R) (2010)

## New perspectives on the quark condensate

Stanley J. Brodsky,<sup>1,2</sup> Craig D. Roberts,<sup>3,4</sup> Robert Shrock,<sup>5</sup> and Peter C. Tandy<sup>6</sup>

<sup>1</sup>*SLAC National Accelerator Laboratory, Stanford University, Stanford, California 94309, USA*

<sup>2</sup>*Centre for Particle Physics Phenomenology: CP<sup>3</sup>-Origins, University of Southern Denmark, Odense 5230 M, Denmark*

<sup>3</sup>*Physics Division, Argonne National Laboratory, Argonne, Illinois 60439, USA*

<sup>4</sup>*Department of Physics, Peking University, Beijing 100871, China*

<sup>5</sup>*C.N. Yang Institute for Theoretical Physics, Stony Brook University, Stony Brook, New York 11794, USA*

<sup>6</sup>*Center for Nuclear Research, Department of Physics, Kent State University, Kent, Ohio 44242, USA*

(Received 25 May 2010; published 18 August 2010)

We show that the chiral-limit vacuum quark condensate is qualitatively equivalent to the pseudoscalar meson leptonic decay constant in the sense that they are both obtained as the chiral-limit value of well-defined gauge-invariant hadron-to-vacuum transition amplitudes that possess a spectral representation in terms of the current-quark mass. Thus, whereas it might sometimes be convenient to imagine otherwise, neither is essentially a constant mass-scale that fills all spacetime. This means, in particular, that the quark condensate can be understood as a property of hadrons themselves, which is expressed, for example, in their Bethe-Salpeter or light-front wave functions.

# *Light-Front vacuum: trivial, causal, frame-independent*

Warsaw  
July 6, 2012

Hot Topics in QCD Phenomenology  
185

Stan Brodsky

SLAC  
NATIONAL ACCELERATOR LABORATORY

# Summary on QCD 'Condensates'

- Condensates do not exist as space-time-independent phenomena
- Property of hadron wavefunctions: Bethe-Salpeter or Light-Front:  
“In-Hadron Condensates”
- Find:  $\frac{\langle 0|\bar{q}q|0 \rangle}{f_\pi} \rightarrow - \langle 0|i\bar{q}\gamma_5 q|\pi \rangle = \rho_\pi$   
 $\langle 0|\bar{q}i\gamma_5 q|\pi \rangle$  similar to  $\langle 0|\bar{q}\gamma^\mu\gamma_5 q|\pi \rangle$
- Zero contribution to cosmological constant! Included in hadron mass
- $Q_\pi$  survives for small  $m_q$  -- enhanced running mass from gluon loops / multiparton Fock states
- Light-Front Vacuum: Causal, trivial, no normal ordering needed

# *Fixed Target Physics with the LHC Beams*

- **7 TeV proton beam, nuclear beams**
- **Full Range of Nuclear and Polarized Targets**
- **Cosmic Ray simulations!**
- **Single-Spin Asymmetries, Transversity Studies,  $A_N$**
- **High- $x_F$  Dynamics at Forward and Backward Rapidities**
- **High- $x_F$  Nuclear Anomalies**
- **Production of ccc to bbb baryons**
- **Quark-Gluon Plasma in Nuclear Rest System--No Ellipse in LF**

# More Outstanding QCD Problems

- **Single inclusive high- $p_T$  hadrons -- wrong scaling !**
- **Quark Interchange dominance in hadron scattering reactions**
- **Quarkonium nuclear target dependence**
- **The Same-Side Ridge at CMS**
- **How to Find the Odderon?**
- **Signals of Hidden Color in the Deuteron**
- **Quark-Gluon Phase of Heavy Ion Collisions**
- **Quark-Gluon Phase in the Target Frame**
- **The Top/anti-Top Asymmetry**
- **Color Transparency and Opaqueness**
- ...

*Studies of QCD just beginning  
IHEP, GSI, LHeC, AFTER*

# QCD Myths

- **Anti-Shadowing is Universal**
- **ISI and FSI are higher twist effects and universal**
- **High transverse momentum hadrons arise only from jet fragmentation -- baryon anomaly!**
- **renormalization scale cannot be fixed**
- **QCD condensates are vacuum effects**
- **Infrared Slavery**
- **Nuclei are composites of nucleons only**
- **Real part of DVCS arbitrary**
- **heavy quarks only from gluon splitting**

# Hot Topics in QCD Phenomenology

- The nonperturbative origin of strange, charm and bottom quarks in the nucleon at large light-cone momenta
- The breakdown of pQCD factorization theorems due to the lensing effects of initial- and final-state interaction
- Important corrections to pQCD scaling for inclusive reactions due to processes in which hadrons are created at high transverse momentum directly in the hard processes and their relation to the baryon anomaly in high-centrality heavy-ion collisions
- The nonuniversality of quark distributions in nuclei;
- light-front holography -- a relativistic, color-confining, first approximation to QCD based on AdS/QCD and its correspondence to light-front quantization
- The principle of maximum conformality -- a method which determines the renormalization scale and gives scheme-independent predictions -- the elimination of the renormalization scale ambiguity using the PMC has important consequences for top quark production at colliders
- The replacement of quark and gluon vacuum condensates by "in-hadron condensates", and how this resolves the conflict between the QCD vacuum and the cosmological constant

# A Theory of Everything Takes Place

String theorists have broken an impasse and may be on their way to converting this mathematical structure -- physicists' best hope for unifying gravity and quantum theory -- into a single coherent theory.

## Frank and Ernest

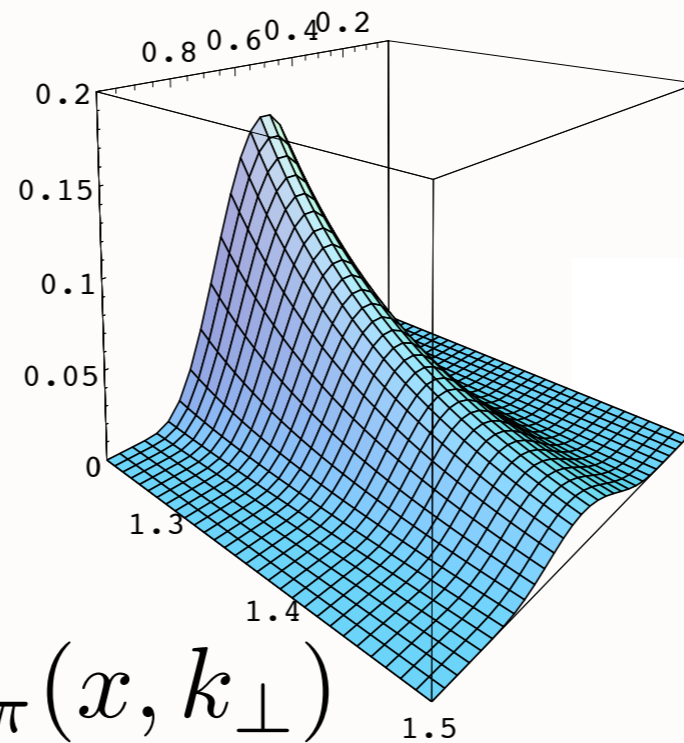
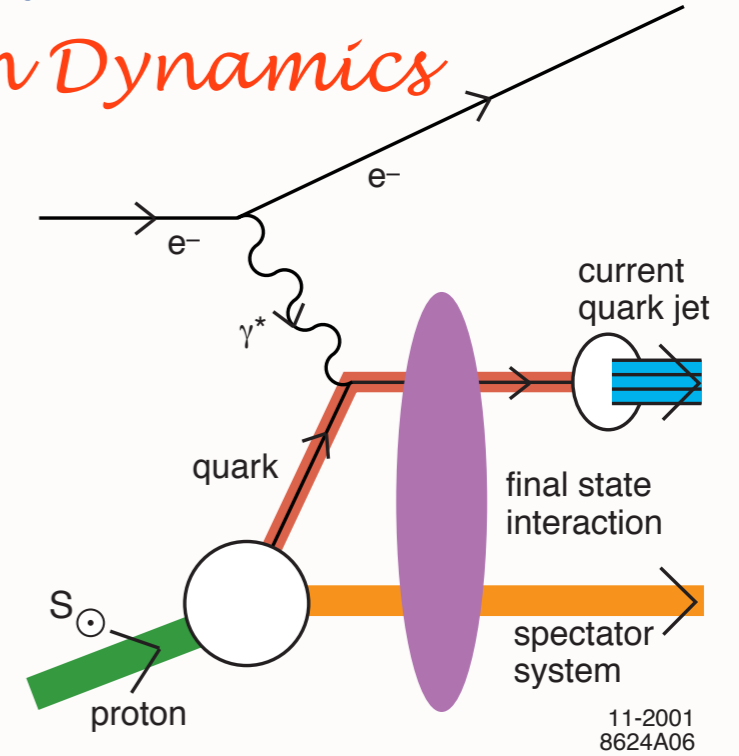
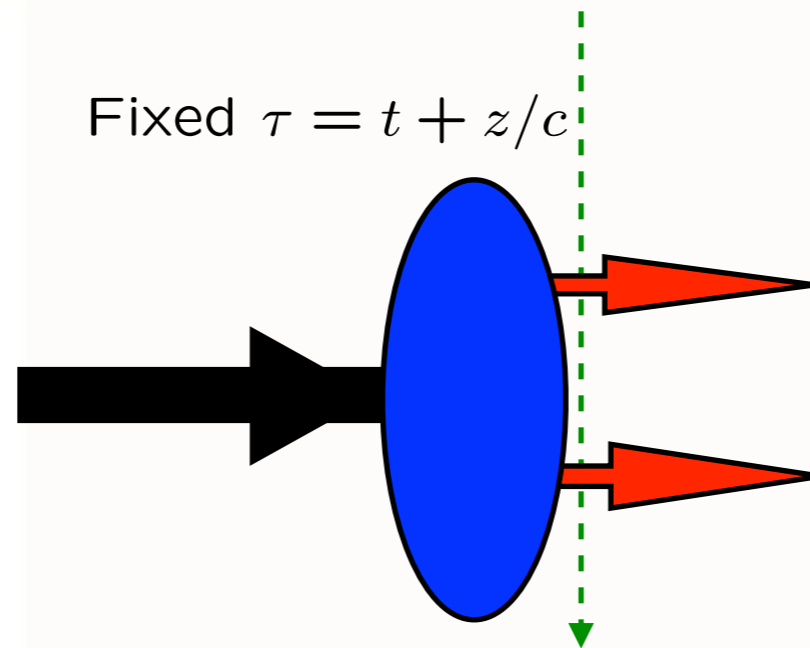
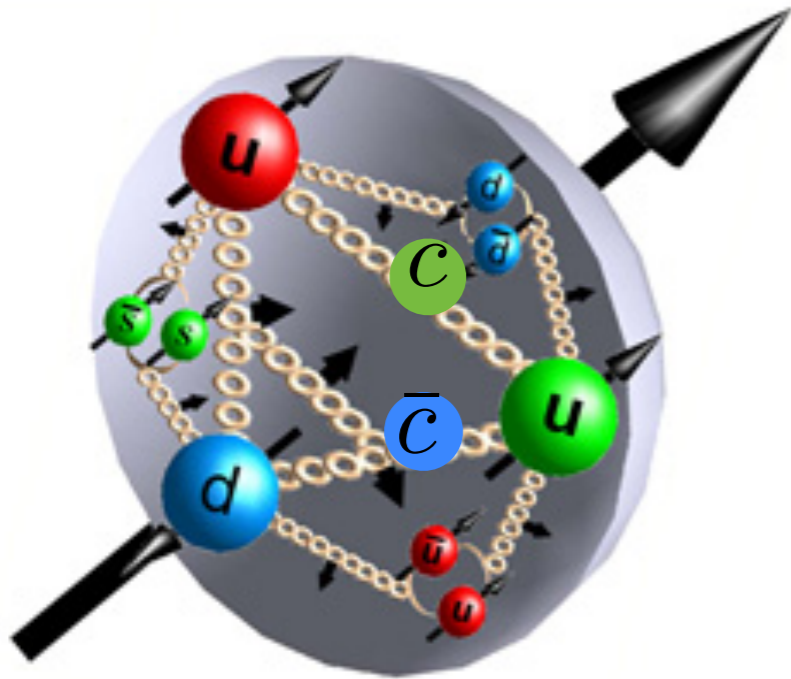


Copyright (c) 1994 by Thaves. Distributed from [www.thecomics.com](http://www.thecomics.com).

# Hadrons, AdS/QCD Duality, and the Physics of the Vacuum

University of Warsaw Workshop, July 3-6, 2012

## Novel Features of Hadron Dynamics



Stan Brodsky



NATIONAL  
ACCELERATOR  
LABORATORY

